



SUPP. 2008/2009

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UNIVERSITY OF SWAZILAND

SUPPLEMENTARY EXAMINATION PAPER

- PROGRAMME:** B.SC. AG. ECON. & AGBMNGT. YEAR 3 (NEW PROG.)  
B.SC. AN. SCI. YEAR 3 (NEW PROG.)  
B.SC. AGRON. YEAR 3 (NEW PROG.)  
B.SC. HORT. YEAR 3 (NEW PROG.)  
B.SC. LWM YEAR 3 (NEW PROG.)
- COURSE CODE:** AEM 303
- TITLE OF PAPER:** AGRICULTURAL STATISTICS
- TIME ALLOWED:** TWO (2) HOURS
- INSTRUCTIONS:**
1. ANSWER QUESTION ONE AND ANY TWO (2) OF THE OTHER QUESTIONS.
  2. QUESTION ONE (1) CARRIES 40 MARKS AND THE OTHER QUESTIONS CARRY 30 MARKS EACH.

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THE CHIEF INVIGILATOR**

**QUESTION 1** [40 marks total]

Assume you tested the yield of six cultivars of maize in a Randomized Complete Block design with four replications and got the following results:

**Mean Yield (tonnes/ha) of 6 maize cultivars.**

<u>Cultivar</u>	<u>Block</u>				<u>Total</u>
	<u>I</u>	<u>II</u>	<u>III</u>	<u>IV</u>	
A	6.2	5.8	6.1	5.9	24.0
B	5.4	5.6	5.3	5.3	21.6
C	4.8	5.1	5.2	4.9	20.0
D	5.2	4.9	4.9	5.0	20.0
E	4.4	4.0	3.9	3.7	16.0
F	<u>7.0</u>	<u>6.9</u>	<u>7.3</u>	<u>6.8</u>	<u>28.0</u>
Total	33.0	32.3	32.7	31.6	129.6

- i. Write the statistical model for this experiment. [4 marks]
- ii. Write appropriate hypotheses for the F tests. [3 marks]
- iii. Copy the following ANOVA table into your answer booklet and complete it, including the cv. Round the MS's, F's and cv to three decimal places. [15 marks]

Effect of cultivar on maize yield.

**ANOVA Table**

<u>Source</u>	<u>df</u>	<u>SS</u>	<u>MS</u>	<u>Calc.F</u>	<u>Table F</u>	
					<u>0.05</u>	<u>0.01</u>
Blocks						
Cultivars						
Error						
Total		21.520				

- iv. Do any appropriate mean separation test(s). [10 marks]
- v. Interpret the results. [8 marks]

**QUESTION 2** [30 marks total]

- (a) Describe why fractional factorials are useful, the types of experiments for which they would be appropriate, and when they are definitely not appropriate. [10 marks]
- (b) In studying the use of ovulated follicle in determining eggs laid by ring-necked pheasant, C. Kabat, I.O. Buss, and R.K. Meyer (1948) presented the following data in the Journal of Wildlife Management on fourteen (14) captive hens. Assume we want to determine whether or not there is any linear relationship between ovulated follicles and eggs laid by ring-necked pheasant. State appropriate hypotheses, test them with Spearman's rank correlation coefficient, and conclude. [20 marks]

Eggs laid	39	29	46	28	31	25	49	57	51	21	42	38	34	47
Ovulated Foll.	37	34	52	26	32	25	55	65	44	25	45	26	29	30

(Source: Steel, R.G.D. and Torrie, J.H. (1980). Principles and Procedures of Statistics. Second Ed. McGraw-Hill, Inc. Singapore. P. 277.)

QUESTION 3 [30 marks total]

- (a) Assume that in a test of six (6) bean cultivars in a single factor experiment in a Randomized Complete Block design with three (3) replications, the cultivar effect was significant ( $P < 0.05$ ), the error mean square (EMS) = 0.12, and the means and  $q_{\alpha}$  values are as given below. Perform an appropriate Duncan's New Multiple Range Test, including a brief conclusion.

[15 marks]

<u>Variety</u>	<u>Yield (tonnes/ha)</u>
BV1	1.5
BV2	0.8
BV3	1.0
BV4	0.5
BV5	1.2
BV6	1.6

$p$ = number of means for range being tested	2	3	4	5	6
$q_{\alpha}$ (5% level)	3.15	3.30	3.37	3.43	3.46

- (b) Assume you obtain the following data from a survey about the performance of sales personnel with different senses of humour. Assume performance is determined by the volume of sales; low, average, and high. Further assume that sense of humour is categorized into poor, average and good.

<u>Sales</u>	<u>Sense of humour</u>		
	<u>Poor</u>	<u>Average</u>	<u>Good</u>
<u>Volume</u>			
Low	80	82	62
Average	144	258	174
High	30	90	80

Test the internal consistency of the data by stating the appropriate hypotheses and testing them. State the conclusion.

[15 marks]

QUESTION 4 [30 marks total]

(a) List and discuss the uses of the analysis of covariance. [15 marks]

(b) Assume the effect of Nitrogen (N) and Phosphorus (P) fertilizer on yield of beans was studied in a replicated trial. Further assume that after the yield data was collected, a multiple linear regression of yield (kg/ha) on applied N and P fertilizer was calculated. Given the information in the table below, state the hypotheses being tested, and state whether or not the partial regression coefficients are significantly different from zero. Interpret the specific meaning of each partial regression coefficient, if appropriate.

[15 marks]

<u>Variable</u>	<u>Partial Regression Coefficient</u>	<u>calculated t</u>	<u>prob.</u>
N (kg/ha)	1.73	1.422	0.330
P (kg/ha)	1.43	2.814	0.026

Formulas and Half-formulas you may need.

$$\Sigma Y^2 - \frac{(\Sigma Y)^2}{n}, \quad \Sigma XY - \frac{(\Sigma X)(\Sigma Y)}{n}, \quad \frac{\Sigma xy}{\Sigma x^2}, \quad \frac{\Sigma xy}{\sqrt{(\Sigma x^2)(\Sigma y^2)}}$$

$$s^2_{y.x} = \frac{\Sigma Y^2 - \frac{(\Sigma xy)^2}{\Sigma x^2}}{n - 2}, \quad t_b = \frac{b}{\sqrt{\frac{s^2_{y.x}}{\Sigma x^2}}}$$

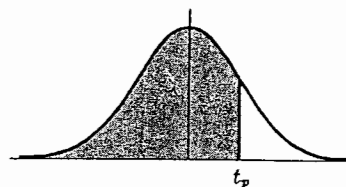
$$t_r = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}}, \quad \sum \frac{(O-E)^2}{E}, \quad \sum \frac{(|O-E|-0.5)^2}{E}, \quad \text{Adj. } SS_y = SS_y - \frac{(SCP)^2}{SS_x}$$

**Appendix E Points for the Distribution of F [5% (light type) and 1% (bold face type)]**

		f <sub>1</sub> , Degrees of freedom (for greater mean square)																									
f <sub>2</sub>		1	2	3	4	5	6	7	8	9	10	11	12	14	16	20	24	30	40	50	75	100	200	500	∞		
1	161	200	216	225	230	234	237	239	241	242	243	244	245	246	248	249	250	250	251	252	253	253	254	254	254	254	
	<b>4,052</b>	<b>4,999</b>	<b>5,403</b>	<b>5,625</b>	<b>5,764</b>	<b>5,859</b>	<b>5,928</b>	<b>5,981</b>	<b>6,022</b>	<b>6,056</b>	<b>6,082</b>	<b>6,106</b>	<b>6,142</b>	<b>6,169</b>	<b>6,208</b>	<b>6,234</b>	<b>6,261</b>	<b>6,286</b>	<b>6,302</b>	<b>6,323</b>	<b>6,334</b>	<b>6,352</b>	<b>6,361</b>	<b>6,366</b>	<b>6,366</b>	<b>6,366</b>	
2	18.51	19.00	19.16	19.25	19.30	19.33	19.36	19.37	19.38	19.39	19.40	19.41	19.42	19.43	19.44	19.45	19.46	19.47	19.47	19.47	19.48	19.49	19.49	19.50	19.50	19.50	19.50
	<b>98.49</b>	<b>99.00</b>	<b>99.17</b>	<b>99.25</b>	<b>99.30</b>	<b>99.33</b>	<b>99.36</b>	<b>99.37</b>	<b>99.39</b>	<b>99.40</b>	<b>99.41</b>	<b>99.42</b>	<b>99.43</b>	<b>99.44</b>	<b>99.45</b>	<b>99.46</b>	<b>99.47</b>	<b>99.48</b>	<b>99.48</b>	<b>99.48</b>	<b>99.49</b>	<b>99.49</b>	<b>99.50</b>	<b>99.50</b>	<b>99.50</b>	<b>99.50</b>	
3	10.13	9.55	9.28	9.12	9.01	8.94	8.88	8.84	8.81	8.78	8.76	8.74	8.71	8.69	8.66	8.64	8.62	8.60	8.58	8.57	8.56	8.54	8.54	8.54	8.53	8.53	
	<b>34.12</b>	<b>30.82</b>	<b>28.46</b>	<b>28.71</b>	<b>28.24</b>	<b>27.91</b>	<b>27.67</b>	<b>27.49</b>	<b>27.34</b>	<b>27.23</b>	<b>27.13</b>	<b>27.06</b>	<b>26.92</b>	<b>26.83</b>	<b>26.89</b>	<b>26.60</b>	<b>26.50</b>	<b>26.41</b>	<b>26.36</b>	<b>26.27</b>	<b>26.23</b>	<b>26.18</b>	<b>26.14</b>	<b>26.12</b>	<b>26.12</b>		
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.93	5.91	5.87	5.84	5.80	5.77	5.74	5.71	5.70	5.68	5.66	5.65	5.64	5.64	5.63	5.63	
	<b>21.20</b>	<b>18.00</b>	<b>16.69</b>	<b>16.36</b>	<b>16.52</b>	<b>16.21</b>	<b>14.98</b>	<b>14.80</b>	<b>14.66</b>	<b>14.54</b>	<b>14.45</b>	<b>14.37</b>	<b>14.24</b>	<b>14.15</b>	<b>14.02</b>	<b>13.93</b>	<b>13.83</b>	<b>13.74</b>	<b>13.69</b>	<b>13.61</b>	<b>13.57</b>	<b>13.52</b>	<b>13.48</b>	<b>13.46</b>	<b>13.46</b>		
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.78	4.74	4.70	4.68	4.64	4.60	4.56	4.53	4.50	4.46	4.44	4.42	4.40	4.38	4.37	4.36	4.36		
	<b>16.28</b>	<b>13.27</b>	<b>12.06</b>	<b>11.38</b>	<b>10.97</b>	<b>10.87</b>	<b>10.45</b>	<b>10.28</b>	<b>10.15</b>	<b>10.06</b>	<b>9.96</b>	<b>9.88</b>	<b>9.77</b>	<b>9.68</b>	<b>9.55</b>	<b>9.47</b>	<b>9.38</b>	<b>9.29</b>	<b>9.24</b>	<b>9.17</b>	<b>9.13</b>	<b>9.07</b>	<b>9.04</b>	<b>9.02</b>	<b>9.02</b>		
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.03	4.00	3.96	3.92	3.87	3.84	3.81	3.77	3.75	3.72	3.71	3.69	3.68	3.67	3.67		
	<b>13.74</b>	<b>10.82</b>	<b>9.78</b>	<b>9.15</b>	<b>8.76</b>	<b>8.47</b>	<b>8.26</b>	<b>8.10</b>	<b>7.98</b>	<b>7.87</b>	<b>7.79</b>	<b>7.72</b>	<b>7.60</b>	<b>7.52</b>	<b>7.39</b>	<b>7.31</b>	<b>7.23</b>	<b>7.14</b>	<b>7.09</b>	<b>7.02</b>	<b>6.99</b>	<b>6.94</b>	<b>6.90</b>	<b>6.88</b>	<b>6.88</b>		
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.63	3.60	3.57	3.52	3.49	3.44	3.41	3.38	3.34	3.32	3.29	3.28	3.25	3.24	3.23	3.23		
	<b>12.25</b>	<b>8.55</b>	<b>8.45</b>	<b>7.85</b>	<b>7.46</b>	<b>7.19</b>	<b>7.00</b>	<b>6.84</b>	<b>6.71</b>	<b>6.62</b>	<b>6.54</b>	<b>6.47</b>	<b>6.35</b>	<b>6.27</b>	<b>6.15</b>	<b>6.07</b>	<b>5.98</b>	<b>5.90</b>	<b>5.85</b>	<b>5.78</b>	<b>5.75</b>	<b>5.70</b>	<b>5.67</b>	<b>5.65</b>	<b>5.65</b>		
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.34	3.31	3.28	3.23	3.20	3.15	3.12	3.08	3.05	3.03	3.00	2.98	2.96	2.94	2.93	2.93		
	<b>11.26</b>	<b>8.85</b>	<b>7.59</b>	<b>7.01</b>	<b>6.63</b>	<b>6.37</b>	<b>6.19</b>	<b>6.03</b>	<b>5.91</b>	<b>5.82</b>	<b>5.74</b>	<b>5.67</b>	<b>5.56</b>	<b>5.48</b>	<b>5.36</b>	<b>5.28</b>	<b>5.20</b>	<b>5.11</b>	<b>5.06</b>	<b>5.00</b>	<b>4.96</b>	<b>4.91</b>	<b>4.88</b>	<b>4.86</b>	<b>4.86</b>		
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.13	3.10	3.07	3.02	2.98	2.93	2.90	2.86	2.82	2.80	2.77	2.76	2.73	2.72	2.71	2.71		
	<b>10.56</b>	<b>6.02</b>	<b>6.99</b>	<b>6.42</b>	<b>6.06</b>	<b>5.80</b>	<b>5.62</b>	<b>5.47</b>	<b>5.35</b>	<b>5.26</b>	<b>5.18</b>	<b>5.11</b>	<b>5.00</b>	<b>4.92</b>	<b>4.80</b>	<b>4.73</b>	<b>4.64</b>	<b>4.56</b>	<b>4.51</b>	<b>4.45</b>	<b>4.41</b>	<b>4.36</b>	<b>4.33</b>	<b>4.31</b>	<b>4.31</b>		
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.97	2.94	2.91	2.86	2.82	2.77	2.74	2.70	2.67	2.64	2.61	2.59	2.56	2.55	2.54	2.54		
	<b>10.04</b>	<b>7.56</b>	<b>6.55</b>	<b>6.99</b>	<b>6.54</b>	<b>6.28</b>	<b>6.10</b>	<b>5.95</b>	<b>5.85</b>	<b>5.76</b>	<b>5.68</b>	<b>5.61</b>	<b>5.50</b>	<b>5.42</b>	<b>5.31</b>	<b>5.23</b>	<b>5.15</b>	<b>5.06</b>	<b>4.98</b>	<b>4.91</b>	<b>4.82</b>	<b>4.75</b>	<b>4.68</b>	<b>4.65</b>	<b>4.65</b>		
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.86	2.82	2.79	2.74	2.70	2.65	2.61	2.57	2.53	2.50	2.47	2.45	2.42	2.41	2.40	2.40		
	<b>9.65</b>	<b>7.20</b>	<b>6.22</b>	<b>6.67</b>	<b>6.22</b>	<b>5.97</b>	<b>5.79</b>	<b>5.64</b>	<b>5.54</b>	<b>5.45</b>	<b>5.37</b>	<b>5.30</b>	<b>5.19</b>	<b>5.11</b>	<b>5.02</b>	<b>4.94</b>	<b>4.85</b>	<b>4.77</b>	<b>4.69</b>	<b>4.61</b>	<b>4.53</b>	<b>4.46</b>	<b>4.39</b>	<b>4.36</b>	<b>4.36</b>		
12	4.75	3.88	3.49	3.26	3.11	3.00	2.92	2.85	2.80	2.76	2.72	2.69	2.64	2.60	2.54	2.50	2.46	2.42	2.38	2.35	2.32	2.31	2.30	2.30	2.30		
	<b>8.33</b>	<b>6.93</b>	<b>6.95</b>	<b>6.41</b>	<b>6.06</b>	<b>5.81</b>	<b>5.63</b>	<b>5.48</b>	<b>5.38</b>	<b>5.30</b>	<b>5.22</b>	<b>5.14</b>	<b>5.06</b>	<b>4.98</b>	<b>4.89</b>	<b>4.81</b>	<b>4.72</b>	<b>4.64</b>	<b>4.56</b>	<b>4.48</b>	<b>4.40</b>	<b>4.32</b>	<b>4.25</b>	<b>4.21</b>	<b>4.21</b>		
13	4.67	3.80	3.41	3.18	3.02	2.92	2.84	2.77	2.72	2.67	2.63	2.60	2.55	2.51	2.46	2.42	2.38	2.34	2.32	2.28	2.26	2.24	2.22	2.21	2.21		
	<b>9.07</b>	<b>6.70</b>	<b>5.74</b>	<b>5.20</b>	<b>4.86</b>	<b>4.62</b>	<b>4.44</b>	<b>4.30</b>	<b>4.19</b>	<b>4.10</b>	<b>4.02</b>	<b>3.96</b>	<b>3.85</b>	<b>3.78</b>	<b>3.67</b>	<b>3.59</b>	<b>3.51</b>	<b>3.42</b>	<b>3.37</b>	<b>3.30</b>	<b>3.27</b>	<b>3.21</b>	<b>3.16</b>	<b>3.16</b>	<b>3.16</b>		

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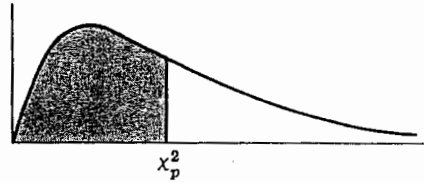
Percentile Values ( $t_p$ )  
for  
Student's  $t$  Distribution  
with  $\nu$  Degrees of Freedom  
(shaded area =  $p$ )



$\nu$	$t_{.995}$	$t_{.99}$	$t_{.975}$	$t_{.95}$	$t_{.90}$	$t_{.80}$	$t_{.75}$	$t_{.70}$	$t_{.60}$	$t_{.55}$
1	63.66	31.82	12.71	6.31	3.08	1.376	1.000	.727	.325	.158
2	9.92	6.96	4.30	2.92	1.89	1.061	.816	.617	.289	.142
3	5.84	4.54	3.18	2.35	1.64	.978	.765	.584	.277	.137
4	4.60	3.75	2.78	2.13	1.53	.941	.741	.569	.271	.134
5	4.03	3.36	2.57	2.02	1.48	.920	.727	.559	.267	.132
6	3.71	3.14	2.45	1.94	1.44	.906	.718	.553	.265	.131
7	3.50	3.00	2.36	1.90	1.42	.896	.711	.549	.263	.130
8	3.36	2.90	2.31	1.86	1.40	.889	.706	.546	.262	.130
9	3.25	2.82	2.26	1.83	1.38	.883	.703	.543	.261	.129
10	3.17	2.76	2.23	1.81	1.37	.879	.700	.542	.260	.129
11	3.11	2.72	2.20	1.80	1.36	.876	.697	.540	.260	.129
12	3.06	2.68	2.18	1.78	1.36	.873	.695	.539	.259	.128
13	3.01	2.65	2.16	1.77	1.35	.870	.694	.538	.259	.128
14	2.98	2.62	2.14	1.76	1.34	.868	.692	.537	.258	.128
15	2.95	2.60	2.13	1.75	1.34	.866	.691	.536	.258	.128
16	2.92	2.58	2.12	1.75	1.34	.865	.690	.535	.258	.128
17	2.90	2.57	2.11	1.74	1.33	.863	.689	.534	.257	.128
18	2.88	2.55	2.10	1.73	1.33	.862	.688	.534	.257	.127
19	2.86	2.54	2.09	1.73	1.33	.861	.688	.533	.257	.127
20	2.84	2.53	2.09	1.72	1.32	.860	.687	.533	.257	.127
21	2.83	2.52	2.08	1.72	1.32	.859	.686	.532	.257	.127
22	2.82	2.51	2.07	1.72	1.32	.858	.686	.532	.256	.127
23	2.81	2.50	2.07	1.71	1.32	.858	.685	.532	.256	.127
24	2.80	2.49	2.06	1.71	1.32	.857	.685	.531	.256	.127
25	2.79	2.48	2.06	1.71	1.32	.856	.684	.531	.256	.127
26	2.78	2.48	2.06	1.71	1.32	.856	.684	.531	.256	.127
27	2.77	2.47	2.05	1.70	1.31	.855	.684	.531	.256	.127
28	2.76	2.47	2.05	1.70	1.31	.855	.683	.530	.256	.127
29	2.76	2.46	2.04	1.70	1.31	.854	.683	.530	.256	.127
30	2.75	2.46	2.04	1.70	1.31	.854	.683	.530	.256	.127
40	2.70	2.42	2.02	1.68	1.30	.851	.681	.529	.255	.126
60	2.66	2.39	2.00	1.67	1.30	.848	.679	.527	.254	.126
120	2.62	2.36	1.98	1.66	1.29	.845	.677	.526	.254	.126
$\infty$	2.58	2.33	1.96	1.645	1.28	.842	.674	.524	.253	.126

Source: R. A. Fisher and F. Yates, *Statistical Tables for Biological, Agricultural and Medical Research* (5th edition), Table III, Oliver and Boyd Ltd., Edinburgh, by permission of the authors and publishers.

Percentile Values ( $\chi^2_p$ )  
for  
the Chi-Square Distribution  
with  $\nu$  Degrees of Freedom  
(shaded area =  $p$ )



$\nu$	$\chi^2_{.995}$	$\chi^2_{.99}$	$\chi^2_{.975}$	$\chi^2_{.95}$	$\chi^2_{.90}$	$\chi^2_{.75}$	$\chi^2_{.50}$	$\chi^2_{.25}$	$\chi^2_{.10}$	$\chi^2_{.05}$	$\chi^2_{.025}$	$\chi^2_{.01}$	$\chi^2_{.005}$
1	7.88	6.63	5.02	3.84	2.71	1.32	.455	.102	.0158	.0039	.0010	.0002	.0000
2	10.6	9.21	7.38	5.99	4.61	2.77	1.39	.575	.211	.103	.0506	.0201	.0100
3	12.8	11.3	9.35	7.81	6.25	4.11	2.37	1.21	.584	.352	.216	.115	.072
4	14.9	13.3	11.1	9.49	7.78	5.39	3.36	1.92	1.06	.711	.484	.297	.207
5	16.7	15.1	12.8	11.1	9.24	6.63	4.35	2.67	1.61	1.15	.831	.554	.412
6	18.5	16.8	14.4	12.6	10.6	7.84	5.35	3.45	2.20	1.64	1.24	.872	.676
7	20.3	18.5	16.0	14.1	12.0	9.04	6.35	4.25	2.83	2.17	1.69	1.24	.989
8	22.0	20.1	17.5	15.5	13.4	10.2	7.34	5.07	3.49	2.73	2.18	1.65	1.34
9	23.6	21.7	19.0	16.9	14.7	11.4	8.34	5.90	4.17	3.33	2.70	2.09	1.73
10	25.2	23.2	20.5	18.3	16.0	12.5	9.34	6.74	4.87	3.94	3.25	2.56	2.16
11	26.8	24.7	21.9	19.7	17.3	13.7	10.3	7.58	5.58	4.57	3.82	3.05	2.60
12	28.3	26.2	23.3	21.0	18.5	14.8	11.3	8.44	6.30	5.23	4.40	3.57	3.07
13	29.8	27.7	24.7	22.4	19.8	16.0	12.3	9.30	7.04	5.89	5.01	4.11	3.57
14	31.3	29.1	26.1	23.7	21.1	17.1	13.3	10.2	7.79	6.57	5.63	4.66	4.07
15	32.8	30.6	27.5	25.0	22.3	18.2	14.3	11.0	8.55	7.26	6.26	5.23	4.60
16	34.3	32.0	28.8	26.3	23.5	19.4	15.3	11.9	9.31	7.96	6.91	5.81	5.14
17	35.7	33.4	30.2	27.6	24.8	20.5	16.3	12.8	10.1	8.67	7.56	6.41	5.70
18	37.2	34.8	31.5	28.9	26.0	21.6	17.3	13.7	10.9	9.39	8.23	7.01	6.26
19	38.6	36.2	32.9	30.1	27.2	22.7	18.3	14.6	11.7	10.1	8.91	7.63	6.84
20	40.0	37.6	34.2	31.4	28.4	23.8	19.3	15.5	12.4	10.9	9.59	8.26	7.43
21	41.4	38.9	35.5	32.7	29.6	24.9	20.3	16.3	13.2	11.6	10.3	8.90	8.03
22	42.8	40.3	36.8	33.9	30.8	26.0	21.3	17.2	14.0	12.3	11.0	9.54	8.64
23	44.2	41.6	38.1	35.2	32.0	27.1	22.3	18.1	14.8	13.1	11.7	10.2	9.26
24	45.6	43.0	39.4	36.4	33.2	28.2	23.3	19.0	15.7	13.8	12.4	10.9	9.89
25	46.9	44.3	40.6	37.7	34.4	29.3	24.3	19.9	16.5	14.6	13.1	11.5	10.5
26	48.3	45.6	41.9	38.9	35.6	30.4	25.3	20.8	17.3	15.4	13.8	12.2	11.2
27	49.6	47.0	43.2	40.1	36.7	31.5	26.3	21.7	18.1	16.2	14.6	12.9	11.8
28	51.0	48.3	44.5	41.3	37.9	32.6	27.3	22.7	18.9	16.9	15.3	13.6	12.5
29	52.3	49.6	45.7	42.6	39.1	33.7	28.3	23.6	19.8	17.7	16.0	14.3	13.1
30	53.7	50.9	47.0	43.8	40.3	34.8	29.3	24.5	20.6	18.5	16.8	15.0	13.8
40	66.8	63.7	59.3	55.8	51.8	45.6	39.3	33.7	29.1	26.5	24.4	22.2	20.7
50	79.5	76.2	71.4	67.5	63.2	56.3	49.3	42.9	37.7	34.8	32.4	29.7	28.0
60	92.0	88.4	83.3	79.1	74.4	67.0	59.3	52.3	46.5	43.2	40.5	37.5	35.5
70	104.2	100.4	95.0	90.5	85.5	77.6	69.3	61.7	55.3	51.7	48.8	45.4	43.3
80	116.3	112.3	106.6	101.9	96.6	88.1	79.3	71.1	64.3	60.4	57.2	53.5	51.2
90	128.3	124.1	118.1	113.1	107.6	98.6	89.3	80.6	73.3	69.1	65.6	61.8	59.2
100	140.2	135.8	129.6	124.3	118.5	109.1	99.3	90.1	82.4	77.9	74.2	70.1	67.3

Source: Catherine M. Thompson, *Table of percentage points of the  $\chi^2$  distribution*, Biometrika, Vol. 32 (1941), by permission of the author and publisher.