

1720

2nd SEM. 2013/2014



Page 1 of 5

UNIVERSITY OF SWAZILAND

FINAL EXAMINATION PAPER

PROGRAMME: BSc. in Agricultural Economics and Agribusiness
Management Year III

COURSE CODE: AEM 306

TITLE OF PAPER: QUANTITATIVE METHODS FOR AGRIBUSINESS DECISIONS

TIME ALLOWED: 2: 00 HOURS

INSTRUCTION: 1. THIS PAPER CONSISTS OF **FIVE** QUESTIONS.
2. ANSWER ANY **FOUR** QUESTIONS.
3. EACH QUESTIONS CARRIES 25 POINTS

DO NOT OPEN THIS PAPER UNTIL PERMISSION HAS BEEN GRANTED BY THE
CHIEF INVIGILATOR

QUESTION 1. (25 points)

1.1 Evaluate the following determinant using the Laplace expansion

$$A = \begin{vmatrix} 10 & 2 & 1 \\ 2 & 0 & 4 \\ 1 & 2 & 6 \end{vmatrix}$$

(6 points)

1.2 Explain Leontief input-output model in Economics?

(6 points)

1.3 A company has two inter-acting branches, A_1 and A_2 . Branch A_1 consumes E0.5 of its own output and E0.3 of A_2 output for every E1 it produces. Branch A_2 consumes E0.6 of A_1 output and E0.4 of its own output per E1 of output. The company wants to know how much each branch should produce per month in order to meet exactly a monthly external demand of E 50,000 for A_1 product and E 40,000 for A_2 product.

Construct the consumption matrix and determine the production schedule for the above external demand. **(13 points)**

QUESTION 2. (25 points)

2.1 A manufacturer knows that if x (hundred) products are demanded in a particular week (i) the total cost function (E000) is $14 + 3x$, and (ii) the total revenue function (E 000) is $19x - 2x^2$.

a) Derive the total profit function. **(4 points)**

b) Find the profit break-even points. **(4 points)**

c) Calculate the level of demand that maximizes profit and the amount of profit obtained.

(4 points)

2.2 Monthly sales revenue in thousands of Emalangeni is given by

$$TR(x_1, x_2) = 7x_1 + 4x_2 + 2x_1x_2 - x_1^2 - x_2^2 + 2$$

Where x_1 is inventory in thousands of Emalangeni and x_2 is floor space in thousands of square feet. Costs in thousands of Emalangeni as a function of inventory and floor space are given by

$$TC(x_1, x_2) = x_1 + x_1x_2 + x_2 + 10.$$

What is the maximum profit? Verify this is indeed the maximum profit? **(13 points)**

QUESTION3.(25 points)

3.1 Given cost and income functions of a sugar producer

$$C(x) = x^2 + 3x + 10$$

and $I(x) = 2x - x^2$ respectively where x is daily production

in tons and $I(x)$ and $C(x)$ are measured in E.

a) For which value of x will the income be maximized?(**4 points**)

b) Determine the gross profit and the value of x which will maximize the gross profit.(**4 points**)

c) The producer is taxed at a rate of 33% on the value of x for which it is a maximum. Determine his net profit and the value of x for which it is a maximum.(**4 points**)

3.2 Calculate the definite integrals.

a) $\int_0^1 x^3 + 5x + 2dx$ (**3 points**)

b) $\int_0^1 e^x dx$ (**3 points**)

3.3 The total revenue obtained (in E000) from selling x hundred items in a particular day is given by R , which is a function of variable x .

Given that $\frac{dR}{dx} = 20 - 4x$:

- a) Determine the total revenue function R (**3 points**)
- b) Find the number of items sold in one day that will maximize the total revenue and evaluate this total revenue?(**4 points**)

QUESTION 4.(25 points)

4.1 The demand and the supply for a certain product (in hundreds) in terms of its price (in cents) are given by the following equations:

$$D(P) = -x^2 + 14 \quad (\text{demand})$$

$$S(P) = x^2 - x + 2 \quad (\text{supply})$$

Find a) the consumers surplus(**4 points**)

b) the producers` surplus, when the market is in equilibrium.(**4 points**)

4.2 Use the Lagrange –multiplier method to find the stationery value of Z and use the bordered Hessian to determine if the stationary value of Z is a maximum or a minimum.

$$Z = 3x - y - xy, \text{ subject to } x + y = 8. \quad (\mathbf{9 \text{ points}})$$

4.3. Use the graphical procedure to solve the following linear programming problem

$$\text{Maximize } Z = 4x_1 + 5x_2,$$

$$\text{Subject to } -x_1 + 2x_2 \leq 4$$

$$x_1 + x_2 \leq 2$$

$$x_1 + x_2 \leq 3 \text{ and}$$

$$x_1 \geq 0, x_2 \geq 0.$$

(8 points)

124

QUESTION 5 (25 points)

5.1 Find the point of supply elasticity ϵ_s from supply function $Q = p^2 + 5$, and determine whether the supply is elastic at $p = 4$. (10 points)

5.2 A furniture manufacture makes three types of table; provincial x_1 , contemporary x_2 and modern x_3 . The provincial model requires 2 hours for sanding and 3 hours for staining. Its profit margin is 36. The contemporary model requires 2 hours for sanding and 2 hours for staining. Its profit margin is 28. The modern model requires 4 hours for sanding and 1 hour for staining while contributing a profit margin of 32.

- a) Formulate the linear programming problem and show production should be allocated to maximize if 60 hours are available for sanding and 8 hours for staining.
- b) Using the graphical approach of linear programming find the optimal solution to this problem. (15 points)