## UNIVERSITY OF SWAZILAND

FACULTY OF COMMERCE
DEPARTMENT OF BUSINESS ADMINISTRATION
MAIN EXAMINATION PAPER
MAY, 2012
(FULL TIME / IDE STUDENTS)

| TITLE OF PAPER | $:$ | MANAGEMENT SCIENCE |
| :--- | :--- | :--- |
| COURSE CODE | $:$ | BA 412 |
| TIME ALLOWED | $:$ | THREE (3) HOURS |
| TOTAL MARKS | $:$ | 100 MARKS |
| INSTRUCTIONS | $:$ | (1) TOTAL NUMBER OF QUESTIONS IN THIS |
|  |  |  |
|  |  | (2) THE PAPER IS SIX (6) |

NOTE: MAXIMUM MARKS WILL BE AWARDED FOR GOOD QUALITY LAYOUT, ACCURACY, AND PRESENTATION OF WORK.

THIS PAPER MUST NOT BE OPENED UNTIL PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR.

## SECTION A (COMPULSORY) - 50 MARKS

Q1. Foster Generators has production facilities in Cleveland, Bedford and York. Production capabilities for these plants over the next 3 month planning period for one particular type of generator are as follows:

| Plant Location | 3 Month Production Capacity |
| :--- | :--- |
| Cleveland | 5000 |
| Bedford | 6000 |
| York | 2500 |

The firm distributes its generators through four regional distribution centers located in Boston, Chicago, St. Louis, and Lexington; the 3 month forecast of demand for the distribution centers are as follows:

| Distribution Center | 3 Month Demand Forecast |
| :--- | :--- |
| Boston | 6000 |
| Chicago | 4000 |
| St. Louis | 2000 |
| Lexington | 1500 |

Management would like to know how much of its production should be shipped from each plant to each distribution center. The cost (in \$) for each unit shipped via each route is given in the following table:

| Destination / Origin | Boston | Chicago | St. Louis | Lexington |
| :--- | :--- | :--- | :--- | :--- |
| Cleveland | 3 | 2 | 7 | 6 |
| Bedford | 7 | 5 | 2 | 3 |
| York | 2 | 5 | 4 | 5 |
|  |  |  |  |  |

(i) Draw the transportation tableau
(5 Marks).
(ii) Use both the Minimum cost method and the Stepping-Stone Method to obtain the optimal solution. (15 Marks).

Q2. (a) Prentice-Hall wants to assign recently hired college graduates: Jones, Smith, Andy and Wilson to regional sales districts in Omaha, Dallas and Miami. But the firm also has an opening in New York and would send one of the three there if it were more economical than a move to Omaha, Miami, or Dallas. It will cost $\$ 10$ to relocate Jones to New York, $\$ 8$ to relocate Smith there and $\$ 15$ to move Wilson.

Based on the following cost table, find the optimal assignment of personnel to offices? (15 Marks)

|  | Office | Omaha | Miami |
| :--- | :---: | :---: | :---: |
| Hiree | 8 | 11 | Dallas |
| Jones | 5 | 16 | 12 |
| Smith | 5 | 10 | 13 |
| Wilson |  |  | 23 |

(b) The Electrocomp Corporation manufactures two electrical products: air conditioners and large fans. The assembly process for each is similar in that both require a certain amount of wiring and drilling. Each air conditioner takes 3 hours of wiring and 2 hours of drilling. Each fan must go through 2 hours of wiring and 1 hour of drilling. During the next production period, 240 hours of wiring time are available and up to 140 hours of drilling time may be used. Each air conditioner sold yields a profit of $\$ 25$. Each fan assembled may be sold for a $\$ 15$ profit. Formulate and solve this LP production mix situation to find the best combination of air conditioners and fans that yields the highest profit. Use the corner point graphical approach.
(15 Marks)

## SECTION B (ANSWER ANY TWO OUESTIONS) - 50 MARKS

Q3.Consider a project having the following seven activities:

| Activity | Immediate <br> Predecessor | Optimistic <br> Time (weeks) | Most likely <br> Time (weeks) | Pessimistic <br> Time <br> (weeks) |
| :---: | :---: | :---: | :---: | :---: |
| A | none | 2 | 3 | 4 |
| B | A | 4 | 4 | 8 |
| C | A | 3 | 5 | 7 |
| D | B | 5 | 5 | 5 |
| E | B, C | 3 | 6 | 7 |
| F | D | 4 | 5 | 9 |
| G | E, F | 3 | 3 | 7 |
|  |  | $\cdot$ |  |  |

a) Draw the network and find the expected project completion time. Marks)
b) What is the critical path?

Marks)
c) What is the probability that the project will be completed in less than 24 weeks? ( 5 Marks)

Q4. Info-tech is a large firm of consultants for business computer systems. The firm requires a supply of floppy disks for the system programmes. The disks are purchased from an outside supplier and it is estimated that the annual usage will be 20,000 over the foreseeable future. The cost of placing each order for the disks is E32. For any disk in stock it is estimated that the annual holding cost is equal to $1 \%$ of its cost. The disks cost E0.80. No stock-out is permitted and the rest of usage may be assumed constant.
(a) What is the optimal order size and how many orders should be placed in a year? (6 Marks)
(b) What is the total relevant inventory cost per annum?

Marks)
(c) If the demand has been underestimated and the true demand is 24,200 disks per annum, what would the effect of keeping to the order quantity calculated in (a) and still meeting demand, rather than using the new optimal order level?
(7 Marks)
(d) What does your answer in (c) tell us about the sensitivity of your model to change demand? (6 Marks)

Q5. Floyd, Vusi and Okocha, who work for a firm of investment consultants, have been approached by one of their clients with regard to the investment of a sum of E100, 000 over a period of two years. After a thorough survey of the available opportunities, two alternatives ( $A$ and $B$ ) are proposed, one involving a small amount of risk, the other being risk free. Investment A will lead to a return of either $8 \%, 10 \%$ or $12 \%$ in each year, but due to the nature of the investment, there will be some correlation between year 1 and year 2 returns. This is shown by the following table which gives the probability of various returns in year 2 given returns in year 1.

|  |  | YEAR 2 |  |  |
| :---: | :---: | :---: | :---: | :---: |
| YEAR 1 | $8 \%$ | $10 \%$ | $12 \%$ |  |
|  |  |  |  |  |
| $8 \%$ | 0.6 | 0.3 | 0.1 |  |
| $10 \%$ | 0.2 | 0.5 | 0.3 |  |
| $12 \%$ | 0.1 | 0.2 | 0.7 |  |

At this stage, the three different returns in year 1 are considered to be equally likely. Investment B will produce a certain return of $9.5 \%$ per year. You may ignore the effects of taxation, and you may assume that the interest earned in year 1 is re-invested for the second year.

Assuming that the whichever alternative is chosen, the investment will be made for the full two year period:
a) Draw a decision tree to represent the alternative courses of action and outcomes. (10 marks)
b) On the basis of the expected value of returns, which investment would you recommend (7 marks)
c) What is the probability that investment B produces a greater return that investment A? (8 marks)

Q6. A company has 3 products, $A, B$ and $C$ of which it can introduce only 1 . The level of demand for each course of action might be low, medium, or high. If the company decides to introduce product $A$, the net income that would result from the levels of demand possible are estimated as E20, E40, and E50 respectively. Similarly, if product B is chosen, net income is estimated at E80, E70, and -E10 and product C, E10, E100, and E40 respectively. The likelihood of low, medium and high performance are, $0.1,0.6$, and 0.3 respectively.

## Calculate

a) Maximum payoff
b) Minimax opportunity loss
c) Expected payoff with perfect information

TABLE 75.1
Leaming curve coefficients

| Unit Nember | $70 \%$ |  | $75 \%$ |  | 88\% |  | 85\% |  | 30\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Unit | Total | Urit | Total | 4 l | Total |
|  | Tinue | Time | Time | Time | Time | Time | Time | Time | Tine | Time |
| 1 | 1000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| 2 | 700 | 1.700 | 750 | 1.750 | . 800 | 1.800 | . 850 | 1.850 | . 900 | 1.500 |
| 3 | . 568 | 2268 | .134 | 2384 | . 702 | 2502 | .73 | 2623 | . 846 | 2746 |
| 4 | . 490 | 2758 | 562 | 2885 | . 840 | 3.142 | . 728 | 3345 | . 810 | 3.556 |
| 5 | . 477 | 3.195 | 513 | 3,459 | .596 | 3.738 | .696 | 4.031 | . 783 | 4.339 |
| 6 | 358 | 3.593 | . 475 | 3.934 | . 562 | 4.299 | . 657 | 4.688 | . 762 | 5.101 |
| 7 | 387 | 3.560 | . 446 | 4.380 | 534 | 4.834 | . 63 | 5322 | . 744 | 5.845 |
| 8 | 343 | 4,303 | . 422 | 4.802 | . 512 | 5.346 | . 614 | 5.936 | . 729 | 6.574 |
| 9 | 323 | 4.626 | . 402 | 5.204 | . 483 | 5.839 | 597 | 6533 | . 716 | 7.250 |
| 10 | 306 | 4.932 | 335 | 5.589 | . 471 | 6.315 | .588 | 7.116 | .705 | 7.994 |
| 11 | . 291 | 5.273 | 370 | 5.958 | . 462 | . 6.77 | . 570 | 7.685 | . 695 | 8.689 |
| 12 | . 278 | 5.501 | 357 | 6.315 | 449 | 727 | . 558 | 8.24 | . 685 | 9374 |
| 13 | 267 | 5.769 | 345 | 6.660 | . 438 | 7685 | . 548 | 8.792 | . 67 | 10.052 |
| 14 | 257 | 6.026 | 334 | 6.99 | . 428 | 8.052 | 509 | 9331 | . 670 | 10.721 |
| 15 | 248 | 6.774 | 325 | 7319 | . 418 | 8.511 | . 500 | 2851 | . 683 | 11.384 |
| 16 | 240 | 6.514 | 316 | 7.635 | . 410 | 8.520 | . 522 | 10.383 | . 656 | 12040 |
| 17 | 233 | 6.747 | 309 | 7.944 | . 402 | 9.322 | . 515 | 10.898 | . 650 | 12.890 |
| 18 | 225 | 6.973 | 301 | 8.245 | 394 | 9.716 | . 508 | 11.405 | . 644 | 13.334 |
| 19 | .200 | 7.192 . | 295 | 8.540 | 388 | 10.104 | . 501 | 11.907 | . 639 | 13.974 |
| 20 | 214 | 7.407 | 288 | 8888 | 381 | 10.485 | . 495 | 12402 | . 634 | 14.808 |
| 21 | . 209 | 7.615 | . 283 | 2.111 | 375 | 10.850. | . 490 | 12892 | . 630 | 15.237 |
| 22 | . 204 | 7.819 | 271 | 9.388 | 370 | 11.230 | . 484 | 13376 | . 625 | 15.862 |
| 23 | . 199 | 8.018 | 272 | 2660 | 364 | 11.594 | . 479 | 13.855 | . 621 | 15.483 |
| 24 | .195 | 8.213 | 267 | 92.928 | . 359 | 11.954 | . 475 | 14.331 | . 617 | 17.100 |
| 25 | . 191 | 8.404 | 283 | 12.191 | 355 | 12309 | . 470 | 14.801 | . 613 | 17.713 |
| 26 | . 187 | 8.591 | 25 | 10.449 | 350 | 12.659 | . 456 | 15.267 | . 609 | 18.323 |
| 27 | . 183 | 8.74 | 256 | 10704 | 346 | 13.005 | . 462 | 15.728 | . 606 | 18.929 |
| 28 | . 180 | 8.954 | 251 | 10.955 | 342 | 13.347 | . 458 | 16.186 | . 603 | 19.531 |
| 29 | . 17 | 9.131 | 247 | 11.202 | - 338 | $13 \mathrm{E} \times 5$ | . 454 | 16.540 | . 599 | 20.131 |
| 30 | . 174 | 9.305 | 244 | 11.446 | . 335 | 14.020 | . 450 | 17.081 | . 596 | 20.727 |

Areas under the standardized normal curve, from $-\infty$ to $+z$


| $z$ | . 00 | . 01 | 12 | 03 | 04 | 05 | 06 | . 67 | 88 | 09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0. | . 5000 | . 5040 | . 5080 | 5120 | . 5160 | . 5198 | . 5239 | . 5279 | . 5319 | . 5259 |
| . 1. | . 5398 | . 5438 | . 5478 | . 5511 | . 5557 | . 5596 | . 5636 | . 5675 | . 5714 | . 5753 |
| 2. | . 5793 | . 5832 | . 5871 | . 5910 | . 5948 | . 5987 | . 6026 | . 6064 | . 6103 | . 6141 |
|  | . 6179 | . 6211 | , 6255 | . 6293 | . 6331 | . 6368 | . 6406 | . 6443 | . 6480 | . 6517 |
|  | . 6554 | . 6591 | . 6628 | . 6664 | . 6700 | . 6736 | . 6772 | . 6808 | . 6844 | . 6879 |
| 5. | . 6915 | . 6950 | . 6985 | . 7019 | . 7054 | . 7088 | . 7123 | . 7157 | . 7150 | . 7224 |
| . 6 | . 7257 | . 7291 | . 7324 | . 7357 | . 7389 | . 7422 | . 7454 | . 7486 | . 7517 | . 7549 |
| . 7. | . 7580 | . 7611 | . 7642 | . 7673 | . 7703 | . 7734 | .7764 | . 7794 | . 7823 | . 7852 |
| . 8. | . 7881 | . 7910 | . 7939 | . 7967 | . 7995 | . 8023 | . 8051 | 8078 | .8106 | . 8133 |
| . 9. | . 8159 | . 8186 | . 8212 | .8238 | . 8264 | . 8289 | . 8315 | . 8340 | . 8365 | . 8389 |
| 1.0. | . 8413 | . 8438 | 8461 | 8485 | . 6508 | 8531 | . 8554 | . 8577 | . 8599 | . 8621 |
| 1.1 | . 8643 | . 8665 | . 8688 | . 8708 | . 8729 | . 8749 | . 8770 | . 8790 | . 8810 | . 8830 |
| 1.2 | . 8849 | . 8869 | . 8888 | 8907 | . 8925 | . 8944 | . 8962 | . 8980 | .8997 | . 9015 |
| 1.3. | . 9032 | . 5049 | .9066 | 9082 | . 9099 | . 9115 | . 9131 | . 9147 | . 9162 | . 917 |
| 1.4 | . 9192 | . 9207 | . 9272 | . 9236 | . 9251 | . 9265 | . 9279 | . 9292 | . 9306 | . 9319 |
| 1.5. | . 9332 | . 9345 | . 9357 | . 9370 | . 3382 | . 9394 | . 9406 | . 9418 | . 9429 | . 9441 |
| 1.6 . | . 9452 | 9463 | . 9474 - | . 9484 | . 9495 | . 9505 | . 9515 | . 9525 | . 9535 | . 9545 |
| 1.7. | .9554 | . 9564 | . 9573 | . 9582 | . 9591 | .9599. | 9608 | 9616 | . 9625 | . 9633 |
| 1.8 | . 5641 | . 9649 | . 9656 | .9664 | . 9671 | . 9678 | .9686 | . 9693 | . 9699 | . 9706 |
| 1.9. | . 9713 | . 9719 | . 9726 | . 9732 | . 9738 | . 9744 | . 9750 | . 9756 | . 9761 | . 9767 |
| 20. | . 9772 | . 9778 | . 9783 | . 9788 | . 9793 | . 9798 | . 9803 | . 9808 | . 9812 | . 9817 |
| 21 | 3821 | . 9826 | . 9830 | 9834 | . 9838 | . 9842 | . 9846 | . 9850 | . $9854{ }^{\text {- }}$ | . 9857 |
| 22. | . 9861 | . 9864 | . 9668 | . 9871 | . 9875 | . 9878 | . 9881 | . 9884 | . 9887 | . 9890 |
| 23. | . 9893 | . 9898 | . 8898 | . 5801 | . 9904 | . 9906 | . 9809 | . 9911 | . 9913 | . 9976 |
| 24 | . 9918 | . 9920 | . 9922 | . 9925 | . 9927 | . 9928 | . 9931 | . 9932 | . 9934 | . 9936 |
| . 25. | . 9938 | . 9940 | . 9941 | . 9943 | . 9945 | . 9946 | . 9948 | . 3949 | . 3951 | . 9952. |
| 2.6. | . 9953 | . 9955 | . 9956 | . 9957 | . 9959 | . 9960 | .9961 | . 9962 | . 9963 | . 9964 |
| 27 | . 9965 | . 9966 | . 9967 | . 2968 | . 9969 | . 9970 | . 9971 | . 9972 | . 9973 | . 9974 |
| 28 | . 9974 | . 9975 | . 9976 | 9977 | . 9977 | . 9978 | . 9979 | . 9979 | . 3980 | . 9981 |
| 2.9 | . 9981 | . 9982 | . 9982 | . 9983 | . 9884 | . 9984 | . 9985 | . 9885 | . 9886 | . 9986 |
| 3.0 | . 9987 | . 9897 | 9987 | . 9988 | . 9988 | . 9988 | . 9989 | . 9889 | . 9990 | . 9990 |
| 3.1 . | . 9990 | . 9991 | . 9991 | . 5991 | . 9991 | . 9992 | . 8982 | . 9992 | . 9899 | . 9993 |
| 3.2 | . 9993 | . 9993 | . 9994 | . 9994 | . 9994 | . 9994 | . 9994 | . 9995 | . 9985 | . 9995 |
| 3.3 . | . 9995 | . 9895 | . 9995 | . 9996 | . 9936 | . 9996 | .9996 | 9996 | . 9996 | . 9997 |
| 3.4. | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9898 |

