

UNIVERSITY OF SWAZILAND

BACHELOR OF SCIENCE

SUPPLEMENTARY EXAMINATION 2007

TITLE OF PAPER : PHYSICAL CHEMISTRY

COURSE NUMBER : C202

TIME : 3 HOURS

INSTRUCTIONS : THERE ARE SIX QUESTIONS

: ANSWER ANY FOUR QUESTIONS

: BEGIN THE ANSWER TO EACH QUESTION ON
A SEPARATE SHEET OF PAPER

: DATA SHEETS ARE PROVIDED WITH THIS
EXAMINATION PAPER

DO NOT OPEN THIS PAPER UNTIL THE INVIGILATOR INSTRUCTS YOU TO DO
SO.

Question 1(25 marks)

- a) Write short notes on Van der Waals equation [10]

Use diagrams, equations or plots to clarify your notes where necessary.

- b) A real gas equation of state for a gas is given by:

$$(P+5an^2/V^2)(V-3nb)=nRT \quad (1)$$

- (i) Derive an expression for $V_{m,c}$, T_c and P_c . [6]
(ii) Find an expression for the Boyle's temperature, T_B . [4]
(iii) Estimate the temperature at which oxygen behaves as an ideal gas, T_B given the constants: $a=6.493 \text{ L}^2\text{atmmol}^{-2}$, $b=5.622 \times 10^{-2} \text{ Lmol}^{-1}$ [2]
(iv) Estimate the radii of real gas molecules using equation (1) for real gases given a critical molar volume of $250 \text{ cm}^3\text{mol}^{-1}$ [2]

QUESTION 2 [25 marks]

- a) Using examples and/or diagrams compare and contrast the following terms

- i) reversible and irreversible expansion [5]
ii) path and state functions [5]
iii) change in internal energy and change in enthalpy [5]

- b) 4 moles of butane occupies 24 L at 310 K.

- i) Derive an expression for reversible isothermal expansion. [5]
ii) Calculate the work done and heat involved when the gas expands isothermally against a constant external pressure of 100 torr until its volume has doubled. [2]
iii) Calculate the efficiency of the system in 1 b (ii) above. [3]

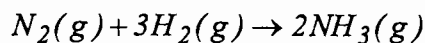
Question 3 [25 Marks]

- a) Derive the integrated Gibbs-Helmholtz equation [3]

$$\frac{\Delta G_2}{T_2} - \frac{\Delta G_1}{T_1} = \Delta H \left(\frac{1}{T_2} - \frac{1}{T_1} \right)$$

from the fundamental thermodynamic equation $dG = VdP - SdT$

- b) Given the reaction:



Calculate the change in Gibbs free energy ΔG^θ

- i) at 298K [5]
ii) at 500K [5]
iii) Comment on the significance of the values obtained in (i) and (ii). [2]

c)

(i) Using an appropriate Master Equation derive the Maxwell's relation

$$(\delta S/\delta V)_T = (\delta P/\delta T)_V \quad [5]$$

(ii) Using the Maxwell's relation in (i) find the expression for internal energy change with volume under isothermal conditions for real gases using van der Waal's relation:

$$(P + an^2/V^2)(V - nb) = nRT \quad [5]$$

Question 4 [25 Marks]

- a) Compare and contrast **Any One Pair** of the following concepts:
- i) Statistical view and the thermodynamic view of entropy [10]
 - ii) Adiabatic and Isothermal expansion [10]
 - iii) Second and Third law of thermodynamics [10]

For each concept include the origin or a short derivation showing its origin, an example where applicable and the role or implication of each of the concepts in thermodynamics.

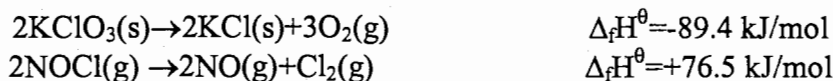
- b) 1.00 mol of perfect gas at 27°C is expanded isothermally from an initial pressure of 3.00 atm to a final pressure of 1.00 atm. Calculate q , w , ΔS_{sys} , ΔS_{surr} and ΔS_{tot} if the expansion is done:
- (1) reversibly, and [5]
 - (2) against a constant external pressure of 1.00 atm. [5]
 - (3) adiabatically against a constant pressure of 1.00 atm. [5]

Question 5 [25 Marks]

- a) Write short notes on **any two** of the following
- i) enthalpy change [5]
 - ii) internal energy change [5]
 - iii) Hess's Law [5]
- b) To Calibrate a calorimeter a 0.120 g naphthalene, $C_{10}H_8(s)$, was burnt at constant volume and it caused the temperature of the calorimeter to rise by 3.05 K. Then 0.10 g of an unknown compound was burned in the same calorimeter, causing a temperature rise of 2.05 K.
- i) Calculate the heat capacity of the calorimeter [3]
 - ii) Is the unknown compound phenol, $C_6H_5OH(s)$ or ethanol, $CH_3CH_2OH(l)$ whose enthalpies of combustion are $\Delta_c H^\ominus = -3054 \text{ kJ mol}^{-1}$ and $-1368 \text{ kJ mol}^{-1}$ respectively. [4]

c) Calculate the standard enthalpies of formation of:

- i) $KClO_3(s)$ from the enthalpy of formation of KCl [4]
 - ii) $NOCl(g)$ from the enthalpy of formation of NO [4]
- Given the attached table and the following information:



QUESTION 6 [25 MARKS]

- a) Write short notes on any Two of the following: [10]
- i) Phase rule
 - ii) Eutectic temperature
 - iii) Freezing point depression
 - iv) Boiling point elevation
 - v) Azeotrope

- b) i) Using the chemical potential expression:

$$\mu_A = \mu_A^* + RT \ln \chi_A$$

where μ_A^* is the chemical potential of the pure solvent A, derive the expression for the boiling point elevation in terms of the boiling point of the pure solvent T, its enthalpy of evaporation and the molality of the solute m_s . [5]

- c) i) What is the approximate relative molecular mass of compound X if 1.00g of X added to 20.0 g benzene leads to a freezing point depression of 1.51°C ? [5]
- ii) Why is the freezing point depression preferred to boiling point elevation for the determination of relative molecular masses ? [2]
- iii) Why would benzene be a better solvent to use than ethanol ? [3]

Useful Relations	General Data		
$(RT)_{298.15K} = 2.4789 \text{ kJ/mol}$	speed of light	c	$2.997925 \times 10^8 \text{ ms}^{-1}$
$(RT/F)_{298.15K} = 0.025693 \text{ V}$	charge of proton	e	$1.60219 \times 10^{-19} \text{ C}$
T/K: 100.15 298.15 500.15 1000.15	Faraday constant	$F = Le$	$9.64846 \times 10^4 \text{ C mol}^{-1}$
T/Cm ⁻¹ : 69.61 207.22 347.62 695.13	Boltzmann constant	k	$1.38066 \times 10^{-23} \text{ J K}^{-1}$
1mmHg = 133.222 N m^{-2}	Gas constant	$R = Lk$	$8.31441 \text{ J K}^{-1} \text{ mol}^{-1}$
$hc/k = 1.43878 \times 10^{-2} \text{ m K}$			$8.20575 \times 10^{-2} \text{ dm}^3 \text{ atm K}^{-1} \text{ mol}^{-1}$
1atm			
$-1.01325 \times 10^5 \text{ Nm}^{-2}$	Planck constant	h	$6.62618 \times 10^{-34} \text{ Js}$
-760 torr		$h = \frac{h}{2\pi}$	$1.05459 \times 10^{-34} \text{ Js}$
$= 1 \text{ bar}$			
	Avogadro constant	$L \text{ or } N_{AV}$	$6.02214 \times 10^{23} \text{ mol}^{-1}$
SI-units:	Atomis mass unit	u	$1.66054 \times 10^{-27} \text{ kg}$
$1 L = 1000 \text{ ml} = 1000 \text{ cm}^3 = 1 \text{ dm}^3$	Electron mass	m_e	$9.10939 \times 10^{-31} \text{ kg}$
$1 \text{ dm} = 0.1 \text{ m}$	Proton mass	m_p	$1.67262 \times 10^{-27} \text{ kg}$
$1 \text{ cal (thermochemical)} = 4.184 \text{ J}$	Neutron mass	m_n	$1.67493 \times 10^{-27} \text{ kg}$
dipole moment: $1 \text{ Debye} = 3.33564 \times 10^{-30} \text{ C m}$	Vacuum permittivity	$\epsilon_0 = \mu_0^{-1} \text{ c}^{-2}$	$8.854188 \times 10^{-12} \text{ J}^{-1} \text{ C}^2 \text{ m}^{-1}$
force: $1 \text{ N} = 1 \text{ J m}^{-1} = 1 \text{ kgms}^{-2} = 10^5 \text{ dyne}$ pressure: $1 \text{ Pa} = 1 \text{ Nm}^{-2} = 1 \text{ Jm}^{-3}$	Vacuum permeability	μ_0	$4\pi \times 10^{-7} \text{ Js}^2 \text{ C}^{-2} \text{ m}^{-1}$
$1 \text{ J} = 1 \text{ Nm}$	Bohr magneton	$\mu_B = \frac{e\hbar}{2m_e}$	$9.27402 \times 10^{-24} \text{ JT}^{-1}$
power: $1 \text{ W} = 1 \text{ J s}^{-1}$	Nuclear magneton	$\mu_N = \frac{e\hbar}{2m_p}$	$5.05079 \times 10^{-27} \text{ JT}^{-1}$
magnetic flux: $1 \text{ T} = 1 \text{ Vsm}^{-2} = 1 \text{ JCs m}^{-2}$ current: $1 \text{ A} = 1 \text{ Cs}^{-1}$			
Prefixes:	Gravitational constant	G	$6.67259 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$
p nano	Gravitational acceleration	g	9.80665 ms^{-2}
10^{-12} pico	Bohr radius	a_0	$5.29177 \times 10^{-11} \text{ m}$

	M_f	$\Delta H_f^\circ/\text{kJ/mol}$	M_f	$\Delta H_f^\circ/\text{kJ/mol}$	gases (298-2000K)	$a/\text{J K}^{-1}\text{mol}^{-1}$	$b/10^3 \text{ J K}^{-2}\text{mol}^{-1}$	$c/10^5 \text{ J Kmol}^{-1}$
H ₂ O(l)	18.015	-241.8	O ₂ (g)	47.998	+142.7			
H ₂ O(l)	18.015	-285.8	NO(g)	30.006	+90.2	He, Ne, Ar, Kr, Xe	20.78	0
H ₂ O(l)	18.015	-187.8	NO ₂ (g)	46.006	+33.2	H ₂	27.28	3.26
NH ₃ (g)	17.031	-46.1	N ₂ O(g)	44.012	+8.2	O ₂	29.96	4.18
NH ₃ (l)	32.045	+50.8	SO ₂ (g)	64.063	-286.8	N ₂	28.58	3.77
NH ₃ (l)	43.028	+264.1	H ₂ S(g)	34.080	-20.8	Cl ₂	37.03	0.87
N ₂ H ₄ (l)	43.028	+294.1	SF ₆ (g)	146.054	-1209	CO ₂	44.23	8.78
HNO ₂ (l)	63.013	-174.1	HF(g)	20.006	-271.1	H ₂ O	30.54	10.29
NH ₂ OH(l)	33.030	-114.2	HCl(g)	36.461	-92.3	NH ₃	25.10	25.10
NH ₂ Cl(l)	53.482	-314.4	HCl(l)	36.461	-178.2	CH ₄	23.64	47.88
HgCl ₂ (s)	271.50	-224.3	HBr(g)	80.917	+36.4	C(S)	18.88	4.77
H ₂ SO ₄ (l)	98.078	-814.0	HI(g)	127.912	+28.5			
H ₂ SO ₄ (aq)	98.078	-909.3	CO ₂ (g)	44.010	-393.5			
NaCl(s)	58.443	-411.0	CO(g)	28.011	-110.5			
NaOH(s)	39.997	-426.7	Al ₂ O ₃ (s)	101.945	-1675.7			
KCl(s)	74.555	-435.9	SiO ₂ (s)	60.085	-910.9			
KBr(s)	119.011	-392.2	FeS(s)	87.91	-100.0			
KI(s)	166.006	-327.8	FeS ₂ (s)	119.876	-178.2			
DIATOMICS		0	AgCl(s)	143.323	-127.1			
Enthalpies of fusion and evaporation $\Delta H_m^\circ/\text{kJ/mol}$ at the transition temperature								
	T_f/K	Fusion ^a	T_b/K	Evaporation ^b				
He	3.5	0.021	4.22	0.084	C ₂ H ₂ (g)	26.038	+228.8	-1300
Ar	83.81	1.188	87.29	6.508	C ₂ H ₄ (g)	28.054	+52.30	-1411
H ₂	13.96	0.117	20.36	0.9163	C ₂ H ₆ (g)	30.070	-84.84	-1580
N ₂	63.15	0.719	77.35	5.586	C ₃ H ₆ (g)	42.081	53.35	-2081
O ₂	54.36	0.444	90.18	6.820	C ₃ H ₈ (g)	42.081	20.5	-2058
Cl ₂	172.12	8.408	239.05	20.410	C ₄ H ₁₀ n-butane (g)	56.124	-128.11	-2677
Br ₂	265.90	10.573	332.35	28.45	C ₄ H ₁₂ n-pentane (g)	72.151	-146.4	-3536
I ₂	386.75	15.52	456.39	41.80	C ₄ H ₁₂ cyclohexane (l)	84.163	-156.2	-3920
Hg	234.29	2.292	628.73	58.296	C ₆ H ₁₄ n-hexane (l)	86.178	-198.7	-4183
Ag	1234	11.30	2436	250.63	C ₆ H ₆ benzene (l)	78.115	+48.99	-3268
Na	370.95	2.601	1158	98.01	C ₈ H ₁₈ n-octane (l)	114.233	-248.6	-5471
CO ₂	217.0	8.33	194.64	25.23	C ₁₀ H ₁₈ n-decane (l)	128.175	+78.53	-5157
H ₂ O	273.15	6.008	373.15	40.656 (44.016 at 298.15 K)	C ₁₀ H ₈ naphthalene (l)	128.175	-238.0	-728.1
NH ₃	185.40	5.652	236.73	23.351	CH ₃ OH (l)	44.054	-198.0	-1193
H ₂ S	187.61	2.377	212.80	18.873	CH ₃ CHO (g)	46.070	-277.0	-1388
CH ₄	90.88	0.941	111.88	8.18	CH ₃ CH ₂ OH (l)	80.053	-484.2	-874.5
C ₂ H ₆	88.85	2.86	184.55	14.7	CH ₃ COOH (l)	86.107	-488.6	-2231
C ₂ H ₄	278.85	10.59	353.25	30.8	CH ₃ COOC ₂ H ₅ (l)	88.114	-165.0	-3054
CH ₃ OH	175.25	3.159	337.22	35.27 (37.99 at 298.15K)	CH ₃ COOH (s)	94.114	-31.1	-3393
					NH ₂ CO.NH ₂ urea (s)	75.056	-333.0	-832.2
					CH ₂ (NH ₂) ₂ CO ₂ H, glycine (s)	75.088	-537.2	-884.4
					C ₆ H ₁₂ O ₆ , α -D-glucose (s)	180.159	-1274	-2802
					C ₆ H ₁₂ O ₆ , β -D-glucose (s)	180.159	-1288	-2808
					C ₁₂ H ₂₂ O ₁₁ , sucrose (s)	342.303	-2222	-5645
					CH ₃ CH(OH)COOH	90.079	-694.0	-1344
					lactic acid (s)			

^a Sublimation: ^b Various pressures: ^c at 1atm

Source: American Institute of Physics handbook, McGraw-Hill.

Heat capacities at 25°C

	$C_{p,m}$ JK ⁻¹ mol ⁻¹	$C_{p,m}$ JK ⁻¹ mol ⁻¹
He, Ne, Ar, Kr, Xe	12.47	20.78
H ₂	20.50	28.81
O ₂	21.01	29.33
N ₂	20.83	29.14
CO ₂	28.83	37.14
NH ₃	27.17	35.48
CH ₄	27.43	35.74
NO ₂		77.28
NO		37.20

F.P Depression, B.P. Elevation

Solvent	F.P °C	K _f °C kg mol ⁻¹	B.P (°C, 101kNm ⁻²)	K _b °C kg mol ⁻¹
Water	0	1.86	100.0	0.52
Benzene	5.51	5.10	80.1	2.60
Acetic Acid	16.6	3.90	118.1	3.10
Cyclohexane	6.5	20.2	81.4	2.79
Camphor	177.7	40.0	205	-
Nitrobenzene	5.7	6.9	210.9	5.24
Ethanol	-177		78.5	1.22
Chloroform	-64		61.3	3.63

Third Law entropies at 25°C, Sm⁰/J K⁻¹ mol⁻¹

Solids		Liquids		Gases	
Ag	42.68	Hg	76.02	H ₂	130.6
C(Gr)	5.77	Br ₂	152.3	N ₂	192.1
C(d)	2.44			O ₂	205.1
Cu	33.4			Cl ₂	223.0
Zn	41.6	H ₂ O	70.0		
I ₂	116.7			CO ₂	213.7
S(Rh)	31.9	HNO ₃	155.6	HCl	186.8
AgCl	96.2	C ₂ H ₅ OH	161.0	H ₂ S	205.6
AgBr	104.6	CH ₃ OH	126.7	NH ₃	192.5
CuSO ₄ ·5H ₂ O	305.4	C ₆ H ₆	49.03	CH ₄	186.1
HgCl ₂	144	CH ₃ COOH	159.8	C ₂ H ₆	229.4
Sucrose	360.2	C ₆ H ₁₂	298.2	CH ₃ CHO	265.7

Standard molar Gibbs free energy and molar entropy of formation at 298.15 K

	M_r	$\Delta G_f^\ominus/\text{kJ/mol}$	$S_f^\ominus/\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$		M_r	$\Delta G_f^\ominus/\text{kJ/mol}$	$S_f^\ominus/\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$
H ₂ O(g)	18.015	-228.57	188.83	O ₃ (g)	47.998	163.2	238.93
H ₂ O(l)	18.015	-120.35	109.6	NO(g)	30.006	86.55	210.76
H ₂ O ₂ (l)	34.015	-120.35	109.6	NO ₂ (g)	46.006	51.31	240.06
NH ₃ (g)	17.031	-16.45	192.45	N ₂ O ₄ (g)	92.012	97.89	304.29
N ₂ H ₄ (l)	32.045	149.43	121.21	SO ₂ (g)	64.063	-300.19	248.22
N ₃ H(l)	43.028	327.3	140.6	H ₂ S(g)	34.080	-33.56	205.79
N ₃ H(g)	43.028	328.1	238.97	SF ₆ (g)	146.054	-1105.3	291.82
HNO ₃ (l)	63.013	-80.71	155.60	HF(g)	20.006	-273.2	173.78
NH ₂ OH(s)	33.030			HCl(g)	36.461	-95.30	186.91
NH ₄ Cl(s)	53.492	-202.87	94.6	HCl(aq)	36.461	-131.23	56.5
HgCl ₂ (s)	271.50	-178.6	146.0	HBr(g)	80.917	-53.45	198.70
H ₂ SO ₄ (l)	98.078	-690.00	156.90	HI(g)	127.912	1.70	206.59
H ₂ SO ₄ (aq)	98.078	-744.53	20.1	CO ₂ (g)	44.010	-394.36	213.74
NaCl(s)	58.443	-384.14	72.13	CO(g)	28.011	-137.17	197.67
NaOH(s)	39.997	-379.49	64.46	Al ₂ O ₃ (s)	101.945	-1582.3	50.92
KCl(s)	74.555	-409.14	82.59	SiO ₂	60.09	-856.64	41.84
KBr(s)	119.011	-380.66	95.90	FeS(g)	87.91	-100.4	60.29
KI(s)	166.006	-324.89	106.32	FeS ₂ (s)	119.975	-166.9	52.93
				AgCl(s)	143.323	-109.79	96.2
He(g)	4.003	0	126.15	Hg(g)	200.59	31.82	174.96
Ar(g)	39.95	0	154.84	Hg(l)	200.59	0	76.02
H ₂ (g)	2.016	0	130.684	Ag(g)	107.87	245.65	173.00
N ₂ (g)	28.013	0	191.61	Ag(s)	107.87	0	42.55
O ₂ (g)	31.999	0	205.138	Na(g)	370.95	76.76	153.71
O ₃ (g)	47.998	163.2	238.93	Na(s)	22.99	0	51.21
Cl ₂ (g)	70.91	0	223.07				
Br ₂ (g)	159.82	3.110	245.46				
Br ₂ (l)	159.82	0	152.23				
I ₂ (g)	253.81	19.33	260.69				
I ₂ (s)	253.81	0	116.135				
organic compounds							
CH ₄ (g) methane	16.043	-50.72	186.26				
C ₂ H ₂ (g) ethyne	26.038	209.20	200.94				
C ₂ H ₄ (g) ethane	28.05	68.15	219.56				
C ₂ H ₆ (g) ethane	30.070	-32.82	229.60				
C ₃ H ₆ cyclopropane(g)	42.081	104.45	237.55				
C ₃ H ₈ propane(g)	42.081	62.78	267.05				
C ₄ H ₁₀ n-butane (g)	58.124	-17.03	310.23				
C ₅ H ₁₂ n-pentane(g)	72.151	-8.20	348.40				
C ₆ H ₁₂ cyclohexane (l)	84.163	26.8					
C ₆ H ₁₄ n-hexane (l)	86.178		204.3				
C ₆ H ₆ benzene (l)	78.115	124.3	173.3				
C ₆ H ₆ benzene (g)	78.115	129.72	269.31				
C ₈ H ₁₈ n-octane (l)	114.233	6.4	361.1				
C ₁₀ H ₈ naphthalene (l)	128.175						
CH ₃ OH (g)	32.042	-161.96	239.81				
CH ₃ OH (l)	32.042	-166.27	126.8				
CH ₃ CHO (g)	44.054	-128.86	250.3				
CH ₃ CHO (l)	46.07	-174.78	160.7				
CH ₃ COOH (l)	60.053	-389.9	159.8				
CH ₃ COOC ₂ H ₅ (l)	88.107	-332.7	259.4				
C ₆ H ₅ OH (g)	94.114	-50.9	146.0				
C ₆ H ₅ NH ₂ (l)	93.129						
CH ₂ (NH ₂)CO ₂ H, glycine (s)	75.068	-373.4	103.5				
C ₆ H ₁₂ O ₆ , α-D-glucose (s)	180.159						
C ₆ H ₁₂ O ₆ , β-D-glucose (s)	180.159	-910	212				
C ₁₂ H ₂₂ O ₁₁ , sucrose (s)	342.303	-1543	360.2				
CH ₃ CH(OH)COOH	90.079						
Lactic acid (s)							

Source: American Institute of Physics handbook, McGraw-Hill.

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
	IA	IIA	IIIB	IVB	VB	VIB	VII B	VIII	VIII	IB	IB	IIIA	IIIA	IVA	VA	VIA	VIA	VIIA	
Period 1	1 H 1.008																		
2	3 Li 6.94	4 Be 9.01											5 B 10.81	14 Si 28.09					
3	11 Na 22.99	12 Mg 24.31											13 Al 26.9						
4	19 K 39.10	20 Ca 40.08	21 Sc 44.96	22 Ti 47.90	23 V 50.94	24 Cr 52.01	25 Mn 54.9	26 Fe 55.85	27 Co 58.71	28 Ni 58.71	29 Cu 63.54	30 Zn 65.37	31 Ga 69.7	32 Ge 72.59	33 As 74.92				
5	37 Rb 85.47	38 Sr 87.62	39 Y 88.91	40 Zr 91.22	41 Nb 91.22	42 Mo 95.94	43 Tc 98.9	44 Ru 101.1	45 Rh 102.9	46 Pd 106.4	47 Ag 107.9	48 Cd 112.4	49 In 114.8	50 Sn 118.7	51 Sb 121.8	52 Te 127.6			
6	55 Cs 132.9	56 Ba 137.3	71 Lu 174.9	72 Hf 178.5	73 Ta 180.9	74 W 183.8	75 Re 186.2	76 Os 190.2	77 Ir 192.2	78 Pt 195.1	79 Au 196.9	80 Hg 200.6	81 Tl 204.4	82 Pb 207.2	83 Bi 208.9	84 Po 210	85 At 210		
7	87 Fr 223	88 Ra 226.0	103 Lr 257	104 Unq	105 Unp	106 Unh	107 Uns	108 Uno	109 Une										



	57	58	59	60	61	62	63	64	65	66	67	68	69	70
Lanthanides	La 138.9	Ce 140.1	Pr 140.9	Nd 144.2	Pm 146.9	Sm 150.9	Eu 151.3	Gd 157.3	Tb 158.9	Dy 162.5	Ho 164.9	Er 167.3	Tm 168.9	Yb 173.0
Actinides	Ac 227.0	Th 232.0	Pa 231.0	U 238.0	Np 237.1	Pu 239.1	Am 241.1	Cm 247.1	Bk 249.1	Cf 251.1	Es 254.1	Fm 257.1	Md 258.1	No 255

Numbers below the symbol indicates the atomic masses; and the numbers above the symbol indicates the atomic numbers.
 SOURCE: International Union of Pure and Applied Chemistry, I. Mills, ed., Quantities, Units, and Symbols in Physical Chemistry, Blackwell Scientific publications, Boston, 1988, pp 86-98.