

**UNIVERSITY OF SWAZILAND
BACHELOR OF SCIENCE
SUPPLEMENTARY EXAMINATION 2007**

TITLE OF PAPER : PHYSICAL CHEMISTRY

COURSE CODE : C402

TIME : 3 HOURS

TOTAL MARKS : 100 MARKS

INSTRUCTIONS :

- THERE ARE SIX QUESTIONS**
- ANSWER FOUR QUESTIONS ONLY**
- EACH QUESTION IS 25 WORTH MARKS**
- A PERIODIC TABLE AND DATA SHEETS ARE PROVIDED WITH THIS EXAMINATION PAPER**
- NO FORM OF ANY PAPER SHOULD BE BROUGHT INTO NOR TAKEN OUT OF THE EXAMINATION ROOM**
- BEGIN THE ANSWER TO EACH QUESTION ON A SEPARATE SHEET OF PAPER**
- ALL CALCULATIONS/WORKOUT DETAILS SHOULD BE SUBMITTED WITH YOUR ANSWER SHEET(S)**

DO NOT OPEN THIS EXAMINATION PAPER UNTIL PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR.

Question 1 [25 Marks]

- a) i) Derive and calculate the root mean square speed of CO₂ molecules at 298 K. [5]
- ii) Given the Maxwell Boltzmann distribution of molecular speeds what is the probability that the CO₂ molecules travel within ± 1 m/s of its root mean square speed at 25°C. [4]
- a) Write the general Ficks first law for flux, J_x , for the following transport phenomena in gases:
- (i) thermal conductivity [3]
(ii) viscosity [3]
(ii) Diffusion [3]
- b) The pressure gradient of Argon, Ar, at 25°C and 100 kPa is 0.1 atm cm⁻¹. Assuming ideal gas behaviour,
- i) Calculate the diffusion constant. [3]
ii) Calculate the flow of gas, J_x , due to diffusion. [4]

Useful equation: $D = \frac{1}{3} \lambda \bar{c}$

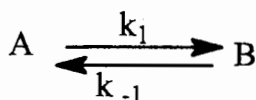
Question 2 [25 Marks]

- a) Write short notes on any Two the following terms:
- i) half life [5]
ii) relaxation time [5]
iii) pseudo first order rate constant [5]
- b) The composition of a liquid phase reaction $A \rightleftharpoons B$ was followed as a function of time by a spectroscopic method with the following results:

T/min	0	10	20	30	40	00
[B]/mol dm ⁻³	0	0.089	0.153	0.200	0.230	0.312

- i) What is the order of the reaction? [5]
ii) What is the value of the rate constant? [3]
iii) What is the half life of the reaction? [2]

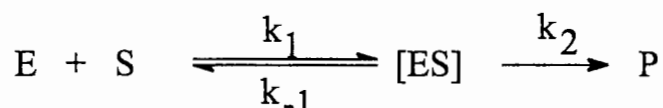
- c) Show that the rate law for the reaction



Is given by: $[A]_t = [A]_o \left[\frac{k_{-1} + k_1 \text{EXP}[-(k_1 + k_{-1})]t}{k_1 + k_{-1}} \right]$ [5]

Question 3 [25 Marks]

The mechanism for enzyme catalysed reactions as proposed by V. Henri (1903) is:



- a) i) Using the steady state approximation and the Lineweaver-Burk treatment show that Michaelis-Menten equation is: [6]

$$\frac{1}{V_o} = \frac{K_m}{V_{max}} \frac{1}{S} + \frac{1}{V_{max}}$$

- ii) Briefly explain and define the role of the following in enzyme kinetics:

- a) V_{max} [3]
 b) Michaelis constant, K_m [3]
 c) k_2 [3]

- b) The following data refer to an enzyme catalysed reaction:

$V_o / 10^{-5} \text{ mol dm}^{-3} \text{ s}^{-1}$	13	20	29	38
$[S] / 10^{-3} \text{ mol dm}^{-3}$	2.0	4.0	8.0	20

The enzyme concentration is 2.0 g/dm^3 and the molecular weight is $50\,000 \text{ g/mol}$

Calculate:

- i) Michaelis constant, K_m [5]
 ii) V_{max} [3]
 iii) The number of substrate molecules converted into product per unit time, when the enzyme is fully saturated with substrate. [2]

Question 4 [25 Marks]

- (a) Sketch the appropriate viscosity plots showing its change with temperature for both gases and liquids. Give an account of the differences between the two plots. [10]

Useful relations:

$$\eta = \frac{1}{3} m \lambda \bar{c} [A]; \eta = C \exp\left(\frac{\Delta E_{vis}}{RT}\right), \bar{c} = \sqrt{\frac{8RT}{\pi MW}}, \lambda = \kappa T / \sqrt{2} \sigma P \text{ and } 1 \text{ Poise} = 1 \text{ P} = 0.1 \text{ Nm}^{-2}\text{s}$$

- (b) Viscosity of gases flowing in tubes is given by Poiseuille's formula:

$$\eta = \frac{\pi R^4 (P_1^2 - P_2^2)}{16 l P_0 V} t$$

The viscosity of carbon dioxide was measured by comparing its rate of flow through a long narrow tube with that of argon. For the same pressure differential, the same volume of carbon dioxide passed through the tube in 55 s as that of argon in 83 s. The viscosity of argon at 25°C is 208 μP;

- i) what is the viscosity of carbon dioxide? [2]
 ii) Estimate the molecular diameter of carbon dioxide. [2]

- (c) Given the distribution function for the flow of particles in liquids:

$$F(x) = \frac{\exp(-x^2/4Dt)}{\sqrt{\pi Dt}}$$

- i) Find expressions for root mean square distance in 3-dimensions [4]
 useful relation: $\langle r^2 \rangle = \langle x^2 \rangle + \langle y^2 \rangle + \langle z^2 \rangle$; $\langle x^2 \rangle = \langle y^2 \rangle = \langle z^2 \rangle$

- (ii) The diffusion coefficient of a molecule MH_2Cl_2 in octane at 24.8°C is $5 \times 10^{-10} \text{ m}^2\text{s}^{-1}$, estimate the 3-dimensional root mean square displacement, r_{rms} , for the molecule after 2500 seconds. [3]

- (iii) Give an account on the use of diffusion coefficients in chemistry [4]

Question 5 [25 Marks]

- a) The Kohlrausch equation for strong electrolytes states:

$$\Lambda_m(c) = \Lambda_m^0 - K\sqrt{c}$$

and the Ostwald dilution law for weak electrolytes states:

$$K_{eq} = \frac{\left(\frac{\Lambda'_m}{\Lambda_m^0}\right)^2}{1 - \left(\frac{\Lambda'_m}{\Lambda_m^0}\right)} c \text{ where } \Lambda_m^0 = \nu_+ \lambda_+^0 + \nu_- \lambda_-^0$$

Using diagrams, where necessary, explain the concentration dependence of molar conductivities shown by strong and weak electrolytes. [10]

- b) The resistances of a series of aqueous NaCl solutions, formed by successive dilution of a sample, were measured in a cell with a cell constant 0.2063 cm^{-1} . The following values were found:

C/mol L ⁻¹	0.0050	0.0010	0.0050	0.010	0.020	0.050
R/Ω	3314	1669	342.1	174.1	89.08	37.14

The viscosity of water is $1.00 \times 10^{-3} \text{ kg m}^{-1} \text{ s}^{-1}$.

- i) Verify that the molar conductivity follows Kohlrausch's law and [3]
 - ii) find the limiting molar conductivity, Λ_m° . [2]
 - iii) Determine the Kohlrausch coefficient κ . [2]
- c) Given the transport number of Na^+ ion in 0.005 M solution is 0.3930 and using the information calculated in 'd' above, calculate:
- i) the molar conductivities [2]
 - ii) mobilities [2]
 - iii) diffusion coefficients [2]
 - iv) hydrodynamic radii [2]
- of Na^+ and Cl^- ions in solution.

Useful equations:

$$\kappa = \left(\frac{l}{R}\right) \frac{l}{A}; t_{\pm} = \frac{\lambda_{\pm}}{\lambda_{+} + \lambda_{-}} = \frac{\lambda_{\pm}}{\Lambda_m^\circ} = \frac{u_{\pm}}{u_{+} + u_{-}}; \Lambda_m^\circ = \nu_{+} \lambda_{+} + \nu_{-} \lambda_{-}; \lambda_{\pm} = z u_{\pm} F, t_{+} + t_{-} = 1,$$

$$D = \frac{kT}{6\pi\eta a} \quad \text{and} \quad D = \frac{ukT}{ze} = \frac{uRT}{zF}.$$

Question 6 [25 Marks]

- a) Distinguish in some detail between physisorption and chemisorption [10]
- b) The Langmuir adsorption isotherm for non-dissociative adsorption of single species is given by:

$$\theta = \frac{kP}{1 + kP}$$

Outline the kinetic arguments used to derive the adsorption isotherm above [5]

- c) The data below are for the chemisorption of hydrogen on copper powder at 25°C..

P/Torr	0.19	0.97	1.90	4.05	7.50	11.95
V _a /cm ³	0.042	0.163	0.221	0.321	0.411	0.471

- i) Confirm that they fit the Langmuir isotherm at low coverages. [6]
- ii) Find the value of K for the adsorption equilibrium and the adsorption volume corresponding to complete coverage. [4]

C402 EXAMINATION SUPPLEMENTARY
INFORMATION

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2007

Useful standard integrals:

$$I_n = \int_0^{\infty} x^n e^{-ax^2} dx$$

n	0	1	2	3	4
I_n	$\frac{1}{2} \left(\frac{\pi}{a}\right)^{1/2}$	$\frac{1}{2a}$	$\frac{1}{4} \left(\frac{\pi}{a^3}\right)^{1/2}$	$\frac{1}{2a^2}$	$\frac{3}{8} \left(\frac{\pi}{a^5}\right)^{1/2}$

$$i_n = \int_0^{\infty} x^n e^{-ax} dx$$

n	1	2	3	4	5
i_n	$\frac{(\pi/a)^{1/2}}{2a}$	$\frac{1}{a^2}$	$\frac{3(\pi/a)^{1/2}}{4a^2}$	$\frac{2}{a^3}$	$\frac{15(\pi/a)^{1/2}}{8a^3}$

<u>Useful Relations</u>	<u>General Data</u>	
$(RT)_{298.15K} = 2.4789 \text{ kJ/mol}$	c	$2.997\ 925 \times 10^8 \text{ ms}^{-1}$
$(RT/F)_{298.15K} = 0.025\ 693 \text{ V}$	e	$1.602\ 19 \times 10^{-19} \text{ C}$
T/K: 100.15 298.15 500.15 1000.15	F=Le	$9.648\ 46 \times 10^4 \text{ C mol}^{-1}$
T/Cm ⁻¹ : 69.61 207.22 347.62 695.13	k	$1.380\ 66 \times 10^{-23} \text{ J K}^{-1}$
1mmHg=133.222 N m ⁻²	R=Lk	$8.314\ 41 \text{ J K}^{-1} \text{ mol}^{-1}$
hc/k=1.438 78x10 ⁻² m K		$8.205\ 75 \times 10^{-2} \text{ dm}^3 \text{ atm K}^{-1} \text{ mol}^{-1}$
1atm 1 cal 1 eV 1cm ⁻¹		
1.01325x10⁵ Nm⁻² 4.184 J 1.602 189x10 ⁻¹⁹ J 0.124x10 ⁻³ eV	h	$6.626\ 18 \times 10^{-34} \text{ Js}$
760torr 96.485 kJ/mol 1.9864x10 ⁻²³ J	$\hbar = \frac{h}{2\pi}$	$1.054\ 59 \times 10^{-34} \text{ Js}$
SI-units:	L or N_{AV}	$6.022\ 14 \times 10^{23} \text{ mol}^{-1}$
1 L = 1000 ml = 1000cm³ = 1 dm³	u	$1.660\ 54 \times 10^{-27} \text{ kg}$
1 dm = 0.1 m	m_e	$9.109\ 39 \times 10^{-31} \text{ kg}$
1 cal (thermochemical) = 4.184 J	m_p	$1.672\ 62 \times 10^{-27} \text{ kg}$
dipole moment: 1 Debye = 3.335 64x10 ⁻³⁰ C m	m_n	$1.674\ 93 \times 10^{-27} \text{ kg}$
force: 1N=1J m⁻¹ = 1kgms⁻² = 10⁵ dyne pressure: 1Pa=1Nm⁻² = 1Jm⁻³	$\epsilon_0 = \mu_0^{-1} \text{c}^{-2}$	$8.854\ 188 \times 10^{-12} \text{ J}^{-1} \text{ C}^2 \text{ m}^{-1}$
1J = 1 Nm	μ₀	$4\pi \times 10^{-7} \text{ Js}^2 \text{ C}^{-2} \text{ m}^{-1}$
power: 1W = 1J s ⁻¹	$\mu_B = \frac{eh}{2m_e}$	$9.274\ 02 \times 10^{-24} \text{ JT}^{-1}$
magnetic flux: 1T=1Vsm ⁻² =1JCs ⁻²	$\mu_N = \frac{eh}{2m_p}$	$5.05079 \times 10^{-27} \text{ JT}^{-1}$
Prefixes:	G	$6.67259 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$
p nano 10 ⁻⁹	g	9.80665 ms^{-2}
n micro 10 ⁻⁶		
m milli 10 ⁻³		
c centi 10 ⁻²		
d deci 10 ⁻¹		
k kilo 10 ³		
M mega 10 ⁶		
G giga 10 ⁹		
	a₀	$5.291\ 77 \times 10^{-11} \text{ m}$

THE PERIODIC TABLE OF ELEMENTS

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
	IA	IIA	IIIB	IVB	VB	VIB	VII B	VIII B	VIII B	IB	II B	IIIB	IIIA	IVA	VA	VIA	VIIA	VIIIA
Period 1	1 H 1.008																	2 He 4.003
2	3 Li 6.94	4 Be 9.01											5 B 10.81	6 C 12.01	7 N 14.01	8 O 16.00	9 F 19.00	10 Ne 20.18
3	11 Na 22.99	12 Mg 24.31											13 Al 26.9	14 Si 28.09	15 P 30.97	16 S 32.06	17 Cl 35.45	18 Ar 39.95
4	19 K 39.10	20 Ca 40.08	21 Sc 44.96	22 Ti 47.90	23 V 50.94	24 Cr 52.01	25 Mn 54.9	26 Fe 55.85	27 Co 58.71	28 Ni 58.71	29 Cu 63.54	30 Zn 65.37	31 Ga 69.7	32 Ge 72.59	33 As 74.92	34 Se 78.96	35 Br 79.91	36 Kr 83.80
5	37 Rb 85.47	38 Sr 87.62	39 Y 88.91	40 Zr 91.22	41 Nb 91.22	42 Mo 95.94	43 Tc 98.9	44 Ru 101.1	45 Rh 102.9	46 Pd 106.4	47 Ag 107.9	48 Cd 112.4	49 In 114.8	50 Sn 118.7	51 Sb 121.8	52 Te 127.6	53 I 126.9	54 Xe 131.3
6	56 Cs 132.9	56 Ba 137.3	71 Lu 174.9	72 Hf 178.5	73 Ta 180.9	74 W 183.8	75 Re 186.2	76 Os 190.2	77 Ir 192.2	78 Pt 195.1	79 Au 196.9	80 Hg 200.6	81 Tl 204.4	82 Pb 207.2	83 Bi 208.9	84 Po 210	85 At 210	86 Rn 222
7	87 Fr 223	88 Ra 226.0	103 Lr 257	104 Unq	105 Unp	106 Unh	107 Uns	108 Uno	109 Une									

Lanthanides	57 La 138.9	58 Ce 140.1	59 Pr 140.9	60 Nd 144.2	61 Pm 146.9	62 Sm 150.9	63 Eu 151.3	64 Gd 157.3	65 Tb 158.9	66 Dy 162.5	67 Ho 164.9	68 Er 167.3	69 Tm 168.9	70 Yb 173.0
Actinides	89 Ac 227.0	90 Th 232.0	91 Pa 231.0	92 U 238.0	93 Np 237.1	94 Pu 239.1	95 Am 241.1	96 Cm 247.1	97 Bk 249.1	98 Cf 251.1	99 Es 254.1	100 Fm 257.1	101 Md 258.1	102 No 255

Numbers below the symbol indicates the atomic masses; and the numbers above the symbol indicates the atomic numbers.

SOURCE: International Union of Pure and Applied Chemistry, 1 mills, ed., Quantities, Units, and symbols in Physical Chemistry, Blackwell Scientific publications, Boston.