

UNIVERSITY OF SWAZILAND
FINAL EXAMINATION (SEM-I) DEC, 2010

Title of Paper : THEORY OF COMPUTATION

Course number: CS211

Time allowed : Three (3) hours.

Instructions : (1) Read all the questions in Section-A and Section-B before you start answering any question.

(2) Answer **all** questions in Section-A and **any two** questions of section-B. Maximum mark is 100.

(3) Use correct notation and show all your work on the script.

This paper should not be opened until the invigilator has granted permission.

SECTION-A (Maximum marks 50)

Note: Answer **all** questions in this section.

Q1 (marks 6 + 6 +12). The following languages are given on symbol set $\{0, 1\}$. Assume that $u, v, w \in \{0, 1\}^*$.

(i). $L1 = \{uvw, u = 0 \text{ or } 00 \text{ and } v = 1 \text{ or } 11\}$

(ii). $L2 = \{1w1\} \cup \{0w0\}$

(iii). $L3 = \{w, (|w| \bmod 4) \neq 0\}$

The following set of words is given -

$\{\lambda, 0, 1, 01, 001, 0100, 00011, 1111101, 0001111, 00000011, 101111010, 010101\}$

(a). From the above set, write all the words belonging to $L1$, all the words belonging to $L2$ and all the words belonging to $L3$.

(b). Write three regular expressions representing $L1$, $L2$ and $L3$ respectively.

(c). Design three deterministic finite acceptors (**dfa**'s) accepting $L1$, $L2$, and $L3$ respectively.

Q2 (marks 6 + 8 + 12). A non deterministic finite acceptor (**nfa**) M is given. Assume q_0 as the initial state, q_3 as the final state. The transition table is given as -

	0	1
q_0	$\{q_1, q_3\}$	$\{q_1\}$
q_1	$\{q_2\}$	$\{q_1, q_2\}$
q_2	$\{q_3\}$	$\{q_0\}$
q_3		$\{q_0\}$

(a). Write the Machine M in correct notation and draw its transition digraph..

(b). Compute $\delta^*(q_0, w)$, where $w = 0000, 1111, 1000$ and 1001 .

(c). Find an equivalent **dfa** of M showing all your steps.

SECTION-B (Maximum marks 50)

Note: Answer **any two** questions in this section.

Q3(a) (marks 4+5). Explain with examples the language of simple variable identifiers in PASCAL programming language. Assume that a valid identifier always starts with a letter and can have zero or more letters, digits, and underscores ($_$) characters only. Write a corresponding right linear grammar.

Q3(b) (marks 4+4+8). Assuming n, m and $k \geq 0$, find Context Free Grammars (CFG) G_1 and G_2 that generate the following languages. -

(i). $L(G_1) = \{a^k b^m c^n, \text{ such that either } k = m, \text{ or } n = m\}$

(ii). $L(G_2) = \{a^m b^k c^m\}$.

Write left most derivations, using G_1 for -

1. $w_1 = aa, (k = 2, m = 0, n = 0),$
2. $w_2 = aaabbbc, (k = 3, m = 3, n = 1),$
3. $w_3 = aaaabbbbcccc, (k = 4, m = 4, n = 4) \text{ and}$
4. $w_4 = \lambda. (k = 0, m = 0, n = 0).$

and using G_2 for -

1. $w_4 = aaaabbbb, (m = 4, k = 0),$
2. $w_5 = bbb, (m = 0, k = 3),$
3. $w_6 = aaabbbccc (m = 3, k = 3) \text{ and}$
4. $w_4 = \lambda. (k = 0, m = 0).$

Include production number at each step of your derivation.

Q4(a) (marks 15). Design a deterministic pushdown automaton (**dpda**) to recognize the language -

$$L = \{w \in a^n b^m, \text{ such that } n > m \text{ and } w \text{ always starts with an } a \}$$

Clearly describe the conditions when your **dpda** accepts and rejects words of L . Write instantaneous descriptions for $w_1 = aaaabb$ and $w_2 = aaabbb$.

Q4(b) (marks 3 + 7). Design a non deterministic pushdown automaton (**npda**) to recognize the language generated by the grammar G , where –

$$G = (\{S, T, B\}, \{a, b\}, S, P).$$

The set of productions P is

$$\begin{aligned} \{ & S \longrightarrow TB \\ & T \longrightarrow aTb \mid ab \\ & B \longrightarrow bB \mid b \} \end{aligned}$$

Q5 (marks 15 + 5 + 5). Write the design of a Turing Machine (**TM**) to compute –

$$F(x, y) = x + y.$$

Assume x and y to be nonzero positive integers in unary representation. Clearly write the steps as to how your TM accomplishes the computations. Also write the instantaneous descriptions using the value of x as 11 and y as 111 for your Turing Machine.

$$q_0 \ x \ 0 \ y \ \vdash^* \ q_f \ x \ 0 \ y \ 0 \ F(X, Y)$$

What is the final configuration when your TM has computed the result and has stopped.

(End of Examination Paper)