

UNIVERSITY OF SWAZILAND

FACULTY OF SCIENCE

DEPARTMENT OF ELECTRONIC ENGINEERING

MAIN EXAMINATION 2005

TITLE OF PAPER: ELECTRONIC MATERIALS & DEVICES II

COURSE NUMBER: E 450

TIME ALLOWED : THREE HOURS

ANSWER ANY FOUR QUESTIONS . ALL CARRY EQUAL MARKS

THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY  
THE INVIGILATOR.

**Question One.**

- (a) Show that for a p-n-p transistor in normal operation, the common emitter current gain can be expressed as:

$$h_{FE} = \frac{\tau_B}{\tau_N}$$

where  $\tau_B$  and  $\tau_N$  are the hole life time and hole transit time in the base respectively.

Hints: Assume a linear decrease in the hole distribution in the base.

Neglect the reverse saturation current  $I_{CO}$ .

Electron emitter current  $I_{nE}$  is small compared to the recombination current  $I_{pr}$ .

(11 marks)

- (b) An n-p-n transistor at 300 K has common emitter d.c. current gain  $\beta_0 = 100$ , and its  $\beta$  cut-off frequency is 20.4 MHz. Assuming that its emitter efficiency  $\gamma = 1$  and that the base is uniformly doped and  $D_B = 12 \text{ cm}^2 \text{ s}^{-1}$ , calculate:

- |       |                                       |           |
|-------|---------------------------------------|-----------|
| (i)   | the current gain $\beta$ at 100 MHz.  | (5 marks) |
| (ii)  | the $\alpha$ cut-off frequency.       | (3 marks) |
| (iii) | the current gain bandwidth frequency. | (2 marks) |
| (iv)  | the base width.                       | (4 marks) |

**Question Two.**

- (a) Given below is the expression for the emitter current due to holes in a drift transistor.

$$I_{PE} = \frac{qAn_i^2}{G_B} [\exp(V_{EB}/V_T) - 1], \text{ where } G_B \text{ is the base Gummel number.}$$

Write down the equivalent expression for the electron current in terms of the emitter Gummel number. Hence derive equations for the emitter efficiency and the common emitter current gain of the transistor in terms of the Gummel numbers. (10 marks)

- (b) The donor concentration in the base region of a silicon p-n-p transistor is given as:  $N_d(x) = 2 \times 10^{18} \exp(-x/\lambda) \text{ m}^{-3}$ , where  $\lambda = 1.2 \mu\text{m}$ . The transistor has base width  $W_B = 4.5 \mu\text{m}$ , emitter width  $W_E = 2.5 \mu\text{m}$  and a uniform dopant concentration  $N_a = 5 \times 10^{18} \text{ m}^{-3}$  in the emitter.

Calculate:

- (i) the base Gummel number.
- (ii) the emitter Gummel number.
- (iii) the common emitter current gain.

Assume  $D_B = 8 \times 10^{-4} \text{ m}^2\text{s}^{-1}$ ,  $D_E = 2.5 \times 10^{-4} \text{ m}^2\text{s}^{-1}$ ,  $\tau_B = 2 \times 10^{-7} \text{ s}$ ,  $\tau_E = 1.5 \times 10^{-8} \text{ s}$ , and  $T = 300 \text{ K}$ .

$$\text{Given: } G_B = \int_0^{W_B} \frac{N_d(x)}{D_B} dx. \quad (15 \text{ marks})$$

**Question Three.**

(a) Explain the terms *saturation voltage* and *pinch off voltage* of a junction field effect transistor. (10 marks)

(b) An double gate silicon n-channel junction field effect transistor at 300 K has the following parameters:

$N_a = 3 \times 10^{24} \text{ m}^{-3}$ ,  $N_d = 10^{21} \text{ m}^{-3}$ , channel length  $L = 20 \mu\text{m}$ , total channel thickness  $2a = 4 \mu\text{m}$ , channel width  $Z = 100 \mu\text{m}$ , electron mobility  $\mu_n = 0.1 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ .

$n_i = 1.5 \times 10^{16} \text{ m}^{-3}$ . Calculate:

- (i) the built-in-voltage. (3 marks)
- (ii) the pinch-off voltage. (3 marks)
- (iii) the drain conductance with gate voltage  $V_G = 0$ . (3 marks)
- (iv) the transconductance with drain voltage  $V_D = 0.5 \text{ V}$  and  $V_G = -1 \text{ V}$ . (3 marks)
- (v) the transconductance in the linear region with  $V_D = 0.5 \text{ V}$  and  $V_G = -1 \text{ V}$ . (3 marks)

**Question Four.**

(a) (i) Give details of the Float-Zone method in the fabrication of single crystal silicon wafer with the help of a schematic diagram of the set up. State the advantages of this technique over the Czochralski method of wafer preparation. (10 marks)

(ii) What is zone refining? Explain. (4 marks)

(iii) Explain the process of neutron transmutation doping mentioning its importance (4 marks)

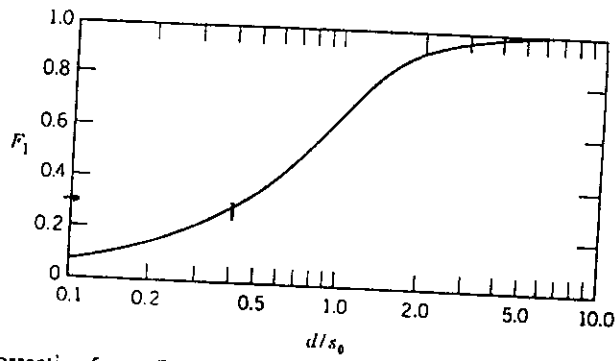
(b) A silicon crystal doped with phosphorus is pulled from its melt. Calculate how many grams of phosphorus should be added to 1 kg of silicon to get a donor concentration of  $10^{16} \text{ cm}^{-3}$  during the initial growth. The distribution coefficient of phosphorus is 0.35. Atomic weight of phosphorus is 30.97, density of silicon is  $2.53 \text{ g cm}^{-3}$ . (7 marks)

**Question Five.**

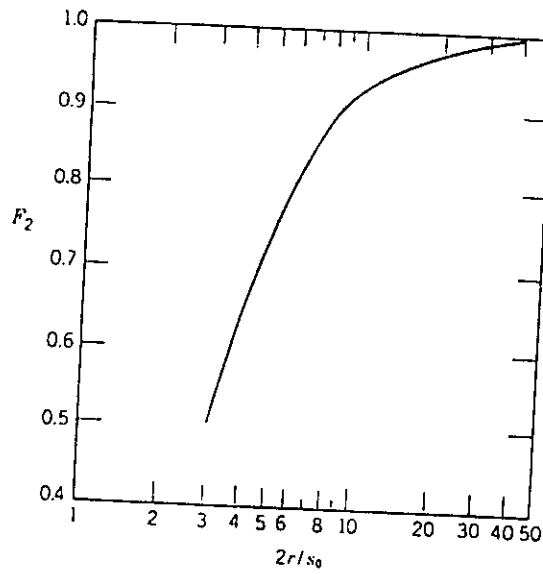
- (a) With the help of a schematic diagram describe briefly the photoconductivity decay method for finding the minority carrier life time of semiconductors. (10 marks)
- (b) The dark resistance of a sample is  $220 \Omega$ . When illuminated with light the resistance decreases to  $200 \Omega$ . If a  $2.5 \text{ mA}$  current is passed through the sample the time constant of the voltage decay is  $0.4 \mu\text{s}$ . Ignoring surface recombination, calculate
- (i) the bulk life time. (4 marks)
  - (ii) the sample voltage  $0.2 \mu\text{s}$  after the removal of the light. (4 marks)
- (c) Four point probe method is used in a semiconductor wafer of diameter of  $2.0 \text{ cm}$  and thickness  $0.25 \text{ m}$ . Readings at the centre of the wafer are  $V = 50 \text{ mV}$  and  $I = 0.5 \text{ mA}$ . The spacing between the probes is  $0.4 \text{ mm}$ . Calculate:
- (i) the resistivity. (5 marks)
  - (ii) sheet resistance of the wafer. (2 marks)

[see appendix A for correction factors]

# APPENDIX A.



Correction factor  $F_1$  for a thin wafer placed on a nonconducting surface as a function of  $d/s_0$ .



Correction factor  $F_2$  for probes centered on a circular wafer of finite diameter  $2r$  as a function of the ratio  $2r/s_0$ .

# APPENDIX **B**

## PHYSICAL CONSTANTS

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Quantity	Symbol	Value
Angstrom unit	$\text{\AA}$	$1 \text{\AA} = 10^{-8} \text{ cm} = 10^{-10} \text{ m}$
Avogadro number	$N$	$6.023 \times 10^{23}/\text{mol}$
Boltzmann constant	$k$	$8.620 \times 10^{-5} \text{ eV/K} = 1.381 \times 10^{-23} \text{ J/K}$
Electronic charge	$q$	$1.602 \times 10^{-19} \text{ C}$
Electron rest mass	$m_e$	$9.109 \times 10^{-31} \text{ kg}$
Electron volt	$\text{eV}$	$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$
Gas constant	$R$	$1.987 \text{ cal/mole-K}$
Permeability of free space	$\mu_0$	$1.257 \times 10^{-6} \text{ H/m}$
Permittivity of free space	$\epsilon_0$	$8.850 \times 10^{-12} \text{ F/m}$
Planck constant	$h$	$6.626 \times 10^{-34} \text{ J-s}$
Proton rest mass	$m_p$	$1.673 \times 10^{-27} \text{ kg}$
$h/2\pi$	$\hbar$	$1.054 \times 10^{-34} \text{ J-s}$
Thermal voltage at 300 K	$V_T$	$0.02586 \text{ V}$
Velocity of light in vacuum	$c$	$2.998 \times 10^{10} \text{ cm/s}$
Wavelength of 1-eV quantum	$\lambda$	$1.24 \text{ }\mu\text{m}$

**TABLE 4.2**  
Properties of Ge, Si and GaAs at 300 K

Property	Ge	Si	GaAs
Atomic/molecular weight	72.6	28.09	144.63
Density (g cm <sup>-3</sup> )	5.33	2.33	5.32
Dielectric constant	16.0	11.9	13.1
Effective density of states			
Conduction band, $N_C$ (cm <sup>-3</sup> )	$1.04 \times 10^{19}$	$2.8 \times 10^{19}$	$4.7 \times 10^{17}$
Valence band $N_V$ (cm <sup>-3</sup> )	$6.0 \times 10^{18}$	$1.02 \times 10^{19}$	$7.0 \times 10^{18}$
Electron affinity (eV)	4.01	4.05	4.07
Energy gap, $E_g$ (eV)	0.67	1.12	1.43
Intrinsic carrier concentration, $n_i$ (cm <sup>-3</sup> )	$2.4 \times 10^{13}$	$1.5 \times 10^{10}$	$1.79 \times 10^6$
Lattice constant (Å)	5.65	5.43	5.65
Effective mass			
Density of states $m_e^*/m_0$	0.55	1.18	0.068
$m_h^*/m_0$	0.3	0.81	0.56
Conductivity $m_e/m_0$	0.12	0.26	0.09
$m_h/m_0$	0.23	0.38	
Melting point (°C)	937	1415	1238
Intrinsic mobility			
Electron (cm <sup>2</sup> V <sup>-1</sup> sec <sup>-1</sup> )	3900	1350	8500
Hole (cm <sup>2</sup> V <sup>-1</sup> sec <sup>-1</sup> )	1900	480	400