

**UNIVERSITY OF SWAZILAND**  
**SUPPLEMENTARY EXAMINATIONS JULY 2007**

**FACULTY OF SCIENCE**

**DEPARTMENT OF ELECTRONIC ENGINEERING**

**TITLE OF PAPER: ANALOGUE ELECTRONICS III**

**COURSE NUMBER: E511**

**TIME ALLOWED: THREE HOURS**

**INSTRUCTIONS:**

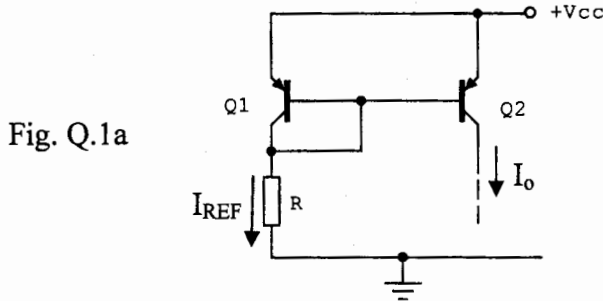
1. Answer any **FOUR (4)** of the following five questions.
2. Each question carries 25 marks.
3. Unless otherwise stated,  $V_{BE(ON)} = 0.7 \text{ V}$  and  $V_T = 0.025 \text{ V}$ .
4. If you think not enough data has been given in any question you may assume reasonable values.
5. A sheet containing some useful equations is attached at the end of the examination paper.

**THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION  
HAS BEEN GIVEN BY THE INVIGILATOR**

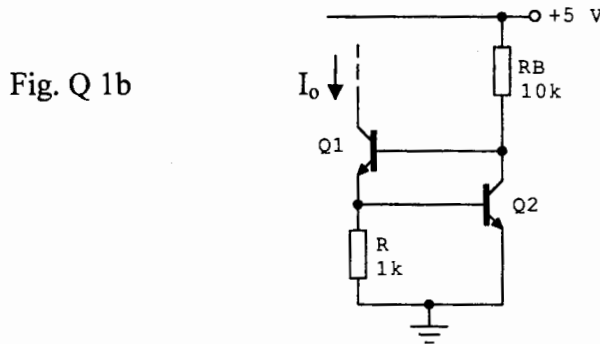
**THIS PAPER CONTAINS EIGHT (8) PAGES INCLUDING THIS PAGE**

**QUESTION ONE**

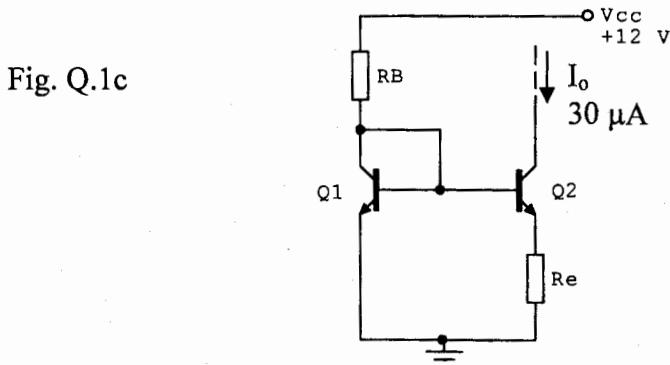
- (a) In the circuit shown in Fig Q.1a, the transistors may be assumed to be matched with each with a current gain  $\beta$ .
- (i) Obtain an accurate expression for the relationship between the currents  $I_{REF}$  and  $I_o$ . (3 marks)
  - (ii) If  $\beta=120$ , evaluate the error in assuming that  $I_{REF} = I_o$ . (2 marks)
  - (iii) Name two possible applications of this circuit as a circuit building block. (2 marks)
  - (iv) What are the drawbacks when using this circuit in the applications you mentioned in (iii)? (4 marks)



- (b) Consider the circuit shown in Fig. Q.1b.
- (i) What is the voltage at the base of transistor Q1? (2 marks)
  - (ii) Evaluate the current in resistor  $R_B$ . (1 mark)
  - (iii) If the effects of finite  $\beta$  values are ignored, and the transistors are assumed to be operating in the active region, show that the current  $I_o$  is independent of the supply voltage and hence evaluate  $I_o$ . (4 marks)

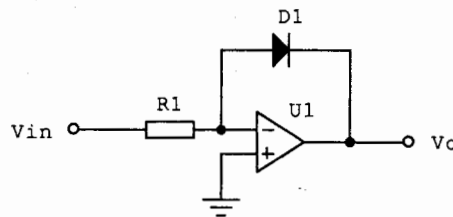


- (c) For the the Widlar current source shown in Fig. Q1c. determine the required values of resistors so that the circuit gives a constant output current  $I_o$  of  $30 \mu A$ . The transistors are matched and specified to have  $V_{BE} = 0.7 V$  at  $1 mA$ . (7 marks)



**QUESTION TWO**

- (a) A diode has  $V_D = 0.7$  V at 1 mA and is characterized by  $n = 1$ . It is connected in series with a  $100\text{-}\Omega$  resistor to a 3.3 V dc supply. Using iterative analysis and the exponential diode model, give an accurate estimate (to 4 significant figures) of the current through the diode. (12 marks)
- (b) For the circuit in Fig. Q.2b,
- Explain why the current in R1 is equal to the forward current in the diode. (3 marks)
  - Hence or otherwise, obtain an expression for  $V_o$  in terms of  $V_{in}$  and the diode parameters. (5 marks)
  - Over what range of values of  $V_{in}$  will the circuit perform as expected? (1 mark)
  - The diode is replaced with an NPN BJT with a grounded base and the collector connected to where the anode of the diode was and the emitter to the output. Show that the relationship between the  $V_o$  and  $V_{in}$  is of the same form as found in b(ii). (4 marks)

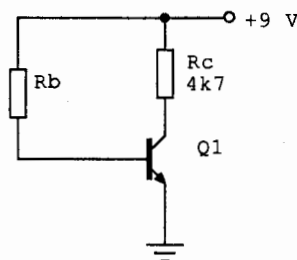
**Fig. Q.2b**

**QUESTION THREE**

- (a) For the BJT in Fig.Q.3a assume that  $\beta=150$ .
- (i) Find the value the bias resistor  $R_b$  for the BJT to be on the edge of saturation (EOS). Assume  $V_{CE(EOS)} = 0.3 \text{ V}$  (6 marks)

What would happen to the operation mode of the transistor in each of the following alterations:

- (ii) The power supply voltage is reduced. (2 marks)
- (iii) the BJT is replaced with one of  $\beta=200$ . (2 marks)
- (iv)  $R_b$  is increased from the value you evaluated in a(i). (2 marks)



**Fig. Q. 3a**

- (b) (i) "The Early Effect limits the output resistance of a BJT". Explain this statement. (7 marks)
- (ii) Calculate the collector current and output resistance of a BJT with  $V_A = 80 \text{ V}$ ,  $I_b = 13.5 \mu\text{A}$ ,  $\beta = 180$  and  $V_{CE} = 6 \text{ V}$ . (6 marks)

## QUESTION FOUR

- (a) The n-channel enhancement mode MOSFET current mirror in Fig. Q4a are identical with  $V_t = 1 \text{ V}$  and  $\frac{1}{2} \frac{W}{L} \mu C_{ox} = 0.2 \text{ mA/V}^2$ .

- (i) Determine  $V_{GS}$ . (6 marks)
- (ii) Determine  $I_o$ . (2 marks)
- (iii) Determine the allowable range of  $V_o$  for the mirror to function properly. (2 marks)

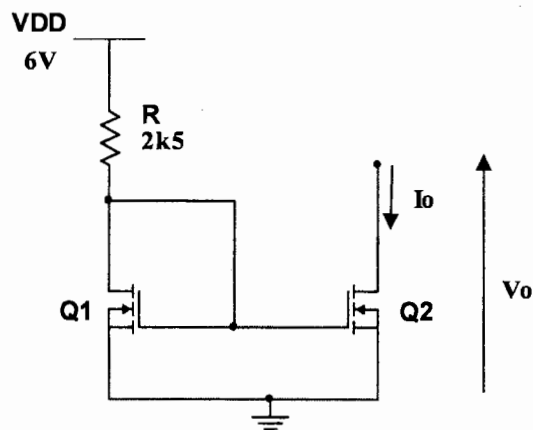


Fig Q 4a

- (b) For the circuit shown in Fig. Q 4b, estimate the value of the voltage  $V_o$ . You may neglect the effect of finite base currents. (4 marks)

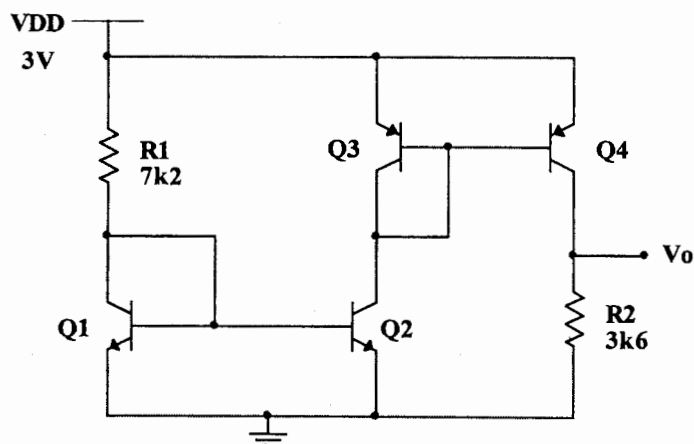


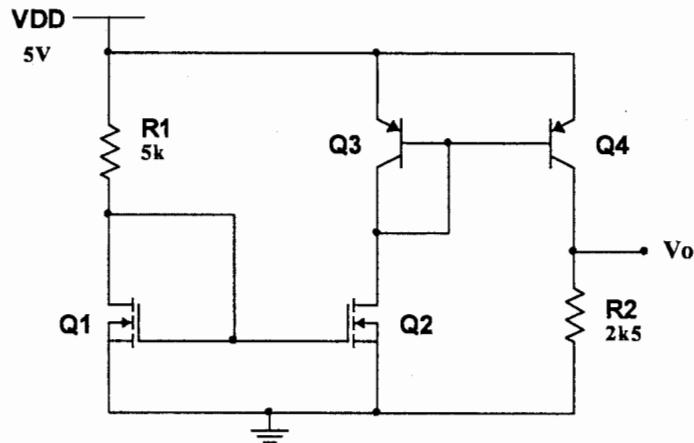
Fig. Q4b

**Question Four (Continued)**

(c) For the circuit shown in Fig. Q.4c the BJTs have a finite  $\beta = 100$  and the MOSFETS

have  $V_t = 1$  V and  $\frac{1}{2} \frac{W}{L} \mu C_{ox} = 0.1$  mA/V<sup>2</sup>.

- (i) Assuming that Q1 and Q2 are in saturation mode, estimate the value of the current through R1. (2 marks)
- (ii) Show that Q1 and Q2 actually operate in the saturation mode. (5 marks)
- (iii) Find the value of the output voltage  $V_o$ . (4 marks)



## QUESTION FIVE

- (a) (i) Sketch a CMOS logic gate realization of the function

$$Y = B(\bar{A} + D) + \bar{C} \quad (7 \text{ marks})$$

- (ii) How many transistors does it need?
- (2 marks)

- (b) A differential amplifier circuit with a differential input and a single-ended output is shown in Fig. Q5b. The transistors used are matched with
- $V_A = 100 \text{ V}$
- and
- $\beta = 100$
- .

- (i) Estimate the gain  $\frac{v_o}{v_1 - v_2}$ . (8 marks)
- (ii) Find the differential input resistance. (3 marks)
- (iii) What values of emitter degeneration resistors,  $R_E$ , are required to double the differential input resistance? (2 marks)
- (iv) Find the new gain after (b)(iii) is implemented. (3 marks)

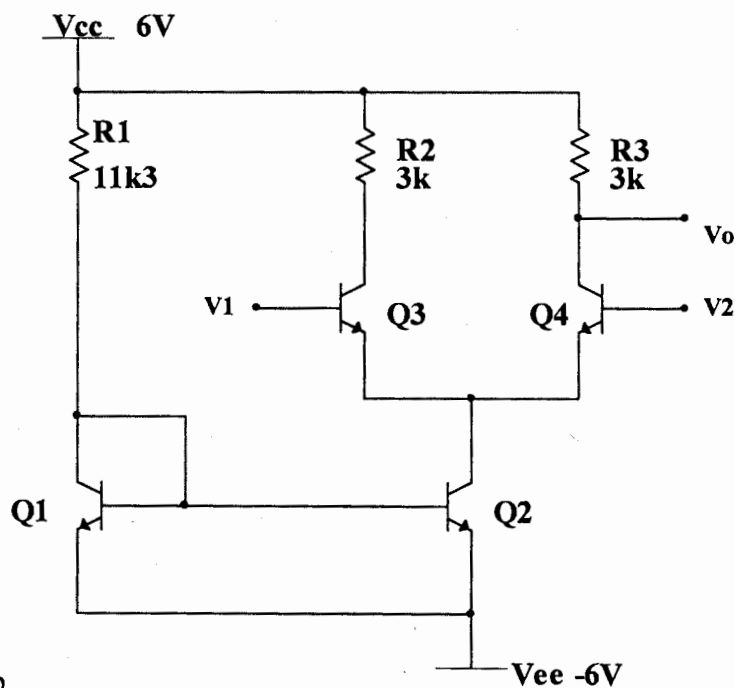


Fig. Q.5b

== END OF EXAMINATION PAPER, SOME USEFUL EQUATIONS FOLLOW ==

**SOME USEFUL MOSFET EQUATIONS**

$$i_D = k_n' \frac{W}{L} \left[ (v_{GS} - V_t) v_{DS} - \frac{1}{2} v_{DS}^2 \right] \text{ in triode region}$$

$$i_D = \frac{1}{2} k_n' \frac{W}{L} (v_{GS} - V_t)^2 \text{ in saturation region}$$

$$i_D = \frac{1}{2} k_n' \frac{W}{L} (v_{GS} - V_t)^2 (1 + \lambda v_{DS}) \text{ in saturation region with Channel Modulation effect}$$

**BJT EBERS-MOLL EQUATIONS**

$$i_E = \frac{I_s}{\alpha_F} (e^{v_{BE}/V_T} - 1) - I_s (e^{v_{BC}/V_T} - 1)$$

$$i_C = I_s (e^{v_{BE}/V_T} - 1) - \frac{I_s}{\alpha_R} (e^{v_{BC}/V_T} - 1)$$

$$i_B = \frac{I_s}{\beta_F} (e^{v_{BE}/V_T} - 1) + \frac{I_s}{\beta_R} (e^{v_{BC}/V_T} - 1)$$