

**UNIVERSITY OF SWAZILAND**  
**FIRST SEMESTER EXAMINATION 2007/2008**

**FACULTY OF SCIENCE**  
**DEPARTMENT OF ELECTRONIC ENGINEERING**

**TITLE OF PAPER: ELECTRICAL CIRCUITS**

**COURSE NUMBER: E310**

**TIME ALLOWED: THREE HOURS**

**INSTRUCTIONS:**

- 1. Answer any FOUR (4) of the following six questions.**
- 2. Each question carries 25 marks.**

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BY THE INVIGILATOR**

**THIS PAPER CONTAINS SIX (5) PAGES INCLUDING THIS PAGE**

**QUESTION 1**

(a) For the circuit of Fig. 1, solve for the current through  $R_2$ .

[12 marks]

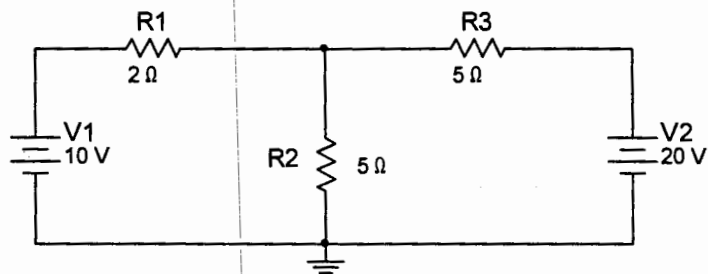


Fig. 1

(b) For the circuit of Fig. 2, find the value of  $R$  for maximum power to  $R$ . Determine the maximum power to  $R$ .

[13 marks]

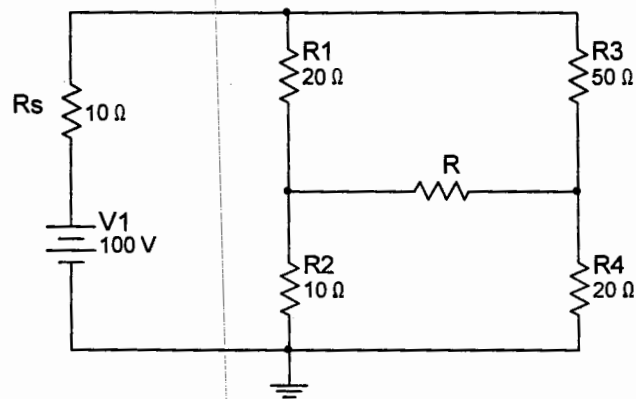


Fig. 2

**QUESTION 2**

- (a) In the circuit of Fig. 3, the switch is moved from position 1 to position 2 at  $t = 0$ . Find  $v_c(t)$  for  $t > 0$ . Assume steady state conditions exist at  $t = 0^-$ .

[13 marks]

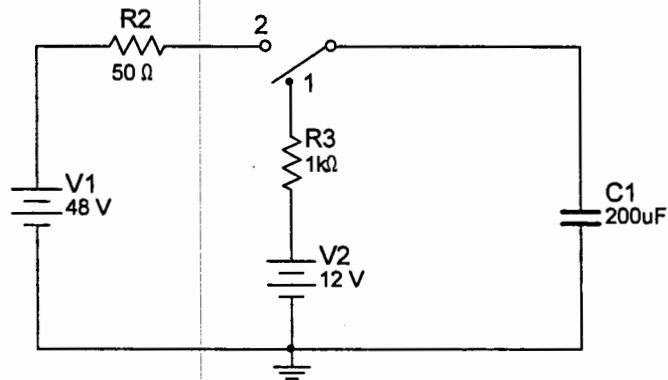


Fig. 3

- (b) In the circuit of Fig. 4, the switch is moved from position 1 to position 2 at  $t = 0$ . Solve for the current through the inductor  $L1$  for  $t > 0$ . Assume steady state conditions exist at  $t = 0^-$ .

[12 marks]

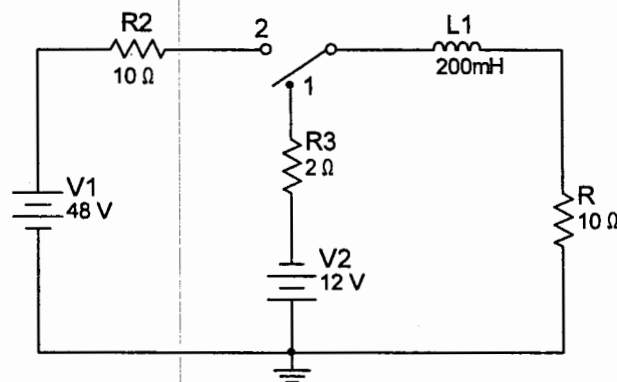


Fig. 4

**QUESTION 3**

(a) Calculate the current in R2 and L1 in the circuit of Fig. 5.

[10 marks]

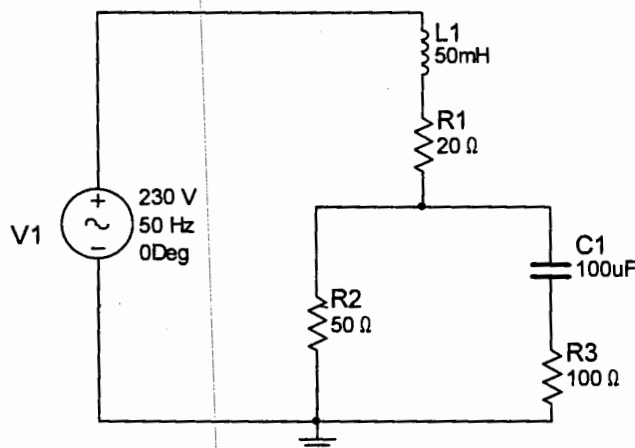


Fig. 5

(b) The loading of a factory on a 400-V, 50-Hz system includes:

10-kW heating load (unity power factor)

10-kW induction motors (0.7 lagging power factor)

2-KW lighting load (0.85 lagging power factor)

- (i) Establish the power triangle for the total loading on the supply.
- (ii) Determine the power factor capacitor required to raise the power factor to unity.
- (iii) Determine the change in supply current from the uncompensated to the compensated system. Assume a single-phase system.

(15 marks)

**QUESTION 4**

(a) A series R-L-C circuit is designed to resonate at  $f_o = 10$  kHz, have a bandwidth of  $0.1 f_o$ , and draw 5 W from a 100-V source at resonance.

- (i) Determine the value of R.
- (ii) Find the values of L and C.
- (iii) Determine the Q of the circuit.

[16 marks]

(b) For the circuit of Fig. 6, determine the circuit impedance at resonance.

[9 marks]

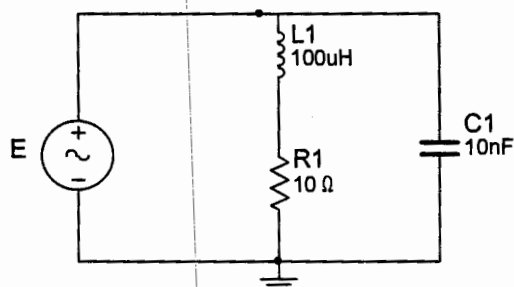


Fig. 6

**QUESTION 5**

- (a) Three impedances each  $R = 75 \Omega$  and  $L = 400 \text{ mH}$  connected in series, are Y-connected to a 400-V (line-to-line), 50-Hz three-phase source. Calculate the line currents, the power factor, and total three-phase real and reactive power.  
[13 marks]
- (b) Determine the output voltage from each secondary winding of the transformer in Fig. 7. Determine also the total primary current, assuming that the transformer is 100% efficient. The numbers of turns on each winding are  $N_p = 375$ ,  $N_{s1} = 750$ , and  $N_{s2} = 500$ .  $R_1 = 75 \Omega$  and  $R_2 = 75 \Omega$ .

[12 marks]

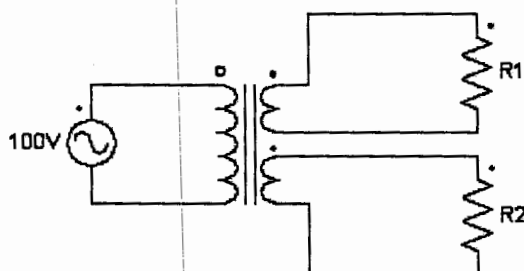


Fig. 7

**QUESTION 6**

- (a) For the circuit of Fig. 8, find the transformation ratio required to deliver maximum power to the speaker. Find the maximum power delivered to the speaker.

[10 marks]

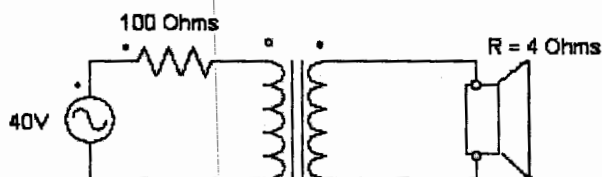


Fig. 8

- (b) The magnetic core shown in Fig. 9 has a 1 mm air gap halfway on the right side. It has uniform 2-cm square cross section. The mean core length is 42 cm, there are 900 turns and the relative permeability  $\mu_r = 800$ . Calculate the coil current required to produce a flux of  $800 \mu\text{Wb}$  in the air gap.  
( $\mu_0 = 4\pi \times 10^{-7} \text{ Wb/A.m}$ )

[15 marks]

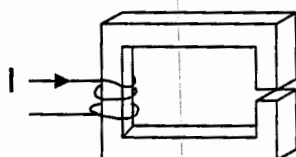


Fig. 9