

UNIVERSITY OF SWAZILAND

FACULTY OF SCIENCE

DEPARTMENT OF ELECTRONIC ENGINEERING

MAIN EXAMINATION 2007/2008.

TITLE OF PAPER: ELECTRONIC MATERIALS & DEVICES II

COURSE NUMBER: E450

TIME ALLOWED : THREE HOURS

INSTRUCTIONS TO CANDIDATES:

USEFUL DATA AND FORMULAE ARE ATTACHED
ANSWER ANY FOUR QUESTIONS . ALL QUESTIONS CARRY EQUAL MARKS

THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE
INVIGILATOR.

Question One.

- (a) (i) Distinguish between **transit time** (τ_B) and **life time** (τ_N) of a charge carrier in the base of a Bipolar Junction Transistor (BJT).
State why the transit time is generally much less than the life time. (3 + 1 marks)
- (ii) Calculate the common emitter current gain of a BJT having transit time of $10 \mu\text{s}$ and life time of $0.1 \mu\text{s}$. (2 marks)

- (b) Given below are the Ebers- Moll equations of a bipolar junction transistor.

$$I_E = -I_{ES} \left[\exp\left(\frac{V_{EB}}{V_T}\right) - 1 \right] + \alpha_I I_{CS} \left[\exp\left(\frac{V_{CB}}{V_T}\right) - 1 \right]$$

$$I_C = -\alpha_N I_{ES} \left[\exp\left(\frac{V_{EB}}{V_T}\right) - 1 \right] - I_{CS} \left[\exp\left(\frac{V_{CB}}{V_T}\right) - 1 \right]$$

- (i) Write down the reciprocity relation in transistors stating what each term represent. (3 marks)
- (ii) Show how the proportionality factor I_{CS} can be expressed in terms of the reverse saturation currents at the collector - base junction. (6 marks)
(Hint: Rearrange the Ebers-Moll equation with emitter leads open)
- (c) A p-n-p transistor has $I_{ES} = -2 \mu\text{A}$, $I_{CS} = -3 \mu\text{A}$ and $\alpha_N = 0.95$. It is connected to a battery with positive to the emitter and negative to the collector. The base is open circuited. Calculate the emitter current. (10 marks)

(Hint: Modify the E-M equations for a reverse biased C-B junction and let $I_B + I_C = 0$)

Question Two.

(a) A p-n-p diffusion transistor with abrupt junctions is operating under normal active mode.

- (i) Draw the biasing arrangement showing the emitter, base and collector currents. (3 marks)
- (ii) Write down the emitter, base and collector currents in terms of the current components due to electron and hole flow across the transistor. (3 marks)
- (iii) Draw the energy band diagram of the transistor. (3 marks)

(b) Small signal common base current gain of a p-n-p diffusion transistor is given as:

$$\alpha(\omega) = \frac{\alpha_0}{1 + \frac{j\omega}{\omega_\alpha}}, \text{ where symbols have their usual meanings.}$$

- (i) Write down the values of α_0 and ω_α in terms of the life time and transit time of the holes in the base. (2 marks)
- (ii) Given that the beta cut - off frequency $f_\beta = f_\alpha (1 - \alpha_0)$, show that the common emitter current gain can be expressed as:

$$\beta(\omega) = \frac{\beta_0}{1 + \frac{jf}{f_\beta}} \quad (5 \text{ marks})$$

- (iii) Define current gain band width frequency f_T (2 marks)
 - (iv) Show that $f_T = \alpha_0 f_\alpha$ (Take $\beta_0 \gg 1$) (3 marks)
- (c)
- (i) What is meant by maximum frequency f_{\max} of a transistor? (2 marks)
 - (ii) A transistor has current gain bandwidth frequency of 408 MHz, collector junction capacitance 3 pF and base resistance 25 Ω . Calculate the maximum frequency f_{\max} of the transistor (2 marks)

Question Three

- (a) (i) Draw a schematic diagram showing the structure and biasing of a Junction Field effect Transistor (JFET). (4marks)
- (ii) Explain how the channel of a JFET get pinched-off by increasing the drain voltage (no gate voltage applied). (4marks)
- (ii) (i) Define *drain conductance* and *transconductance* of a JFET. (2 marks)
- (ii) Show that the drain conductance in the linear region can be expressed as:

$$G_D = G_0 \left[1 - \left(\frac{V_i - V_G}{V_P} \right)^{1/2} \right]$$

$$\text{given: } I_D = G_0 \left\{ V_D - \frac{2}{3} V_P \left[\left(\frac{V_i - V_G + V_D}{V_P} \right)^{3/2} - \left(\frac{V_i - V_G}{V_P} \right)^{3/2} \right] \right\} \quad (10 \text{ marks})$$

- (iii) What is *threshold voltage* V_{th} a JFET? Show that $V_{th} = V_i - V_p$ (5 marks)

Question Four.

- (a) (i) With the help of a schematic diagram, explain the Float-Zone method in the fabrication of single crystal silicon ingots. (8 marks)
- (ii) Describe how silicon wafers are prepared for device fabrication from the ingots. (4 marks)
- (iv) What is zone refining? Explain. (3 marks)
- (b) (i) What is epitaxial growth of semiconductors? (2 marks)
- (ii) With the help of a schematic diagram describe the molecular beam epitaxy method for growing doped AlGaAs layers on GaAs. (8 marks)

Question Five.

- (a) (i) Draw schematic diagram of the four-point probe set up for measurement of resistivity of a semiconductor sample. (3 marks)
- (ii) A 0.2 mm thick semiconductor wafer has diameter of 2.0 cm. It is placed on an insulating plate. Four point probe readings at the centre of the wafer are $V = 50$ mV and $I = 0.5$ mA. The spacing between the probes is 0.4 mm. Determine the resistivity and sheet resistance of the wafer. (see appendix C for correction factors). (9 marks)
- (b) (i) Draw a labeled schematic diagram of the Haynes-Shockley experimental set up for finding the drift mobility of minority carriers in an n-type semiconductor. (5 marks)
- (ii) The following data were obtained in a Hanes - Shockley experiment. at 300 K
- | | | |
|---|---|------------------------|
| Length of the sample | = | 2.5 cm. |
| Spacing between the emitter and collector | = | 1.0 cm |
| Voltage applied across the sample | = | 20 V |
| Time of arrival of the pulse at the collector | = | 1.5×10^{-4} s |
- Calculate the mobility of the minority carriers in the sample.
 - Use Einstein's equation to find the diffusion coefficient of the carriers.
- (8 marks)

APPENDIX ASome useful equations.

$$I_D = G_0 \left\{ V_D - \frac{2}{3} V_P \left[\left(\frac{V_i - V_G + V_D}{V_P} \right)^{3/2} - \left(\frac{V_i - V_G}{V_P} \right)^{3/2} \right] \right\}$$

$$f_{\max} = \left[\frac{f_T}{8\pi r_B C_c} \right]^{1/2}$$

$$W_B = W_{B0} - \left[\frac{2\epsilon_S}{qN_d} (V_i - V_{CB}) \right]^{1/2}$$

For a BJT,

$$\omega_a = \frac{2.43 D_B}{\omega_B^2} \left[1 + \left(\frac{\eta}{2} \right)^{4/3} \right]$$

$$\frac{I_{NE}}{I_{PE}} = \frac{N_D D_E L_B \tanh(W_B / L_B)}{N_a D_B L_E \tanh(W_E / L_E)}$$

Drift Transistors:

$$\alpha(\omega) = \frac{\alpha_0}{1 + j\omega / \omega_a} \exp\left(-j \frac{m\omega}{\omega_a}\right)$$

van der Pauw, Hall effect.:

$$\rho = \frac{\pi d}{2 \ln 2} \left(\frac{V_{DC}}{I_{AB}} + \frac{V_{BC}}{I_{AD}} \right) f$$

$$R_H = \frac{V_{BD} d}{I_{AC} B} = \mu_H \rho$$

APPENDIX B

PHYSICAL CONSTANTS

Quantity	Symbol	Value
Angstrom unit	\AA	$1 \text{\AA} = 10^{-8} \text{ cm} = 10^{-10} \text{ m}$
Avogadro number	N	$6.023 \times 10^{23}/\text{mol}$
Boltzmann constant	k	$8.620 \times 10^{-5} \text{ eV/K} = 1.381 \times 10^{-23} \text{ J/K}$
Electronic charge	q	$1.602 \times 10^{-19} \text{ C}$
Electron rest mass	m_e	$9.109 \times 10^{-31} \text{ kg}$
Electron volt	eV	$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$
Gas constant	R	1.987 cal/mole-K
Permeability of free space	μ_o	$1.257 \times 10^{-6} \text{ H/m}$
Permittivity of free space	ϵ_o	$8.850 \times 10^{-12} \text{ F/m}$
Planck constant	h	$6.626 \times 10^{-34} \text{ J-s}$
Proton rest mass	m_p	$1.673 \times 10^{-27} \text{ kg}$
$h/2\pi$	\hbar	$1.054 \times 10^{-34} \text{ J-s}$
Thermal voltage at 300 K	V_T	0.02586 V
Velocity of light in vacuum	c	$2.998 \times 10^{10} \text{ cm/s}$
Wavelength of 1-eV quantum	λ	$1.24 \text{ }\mu\text{m}$

APPENDIX C

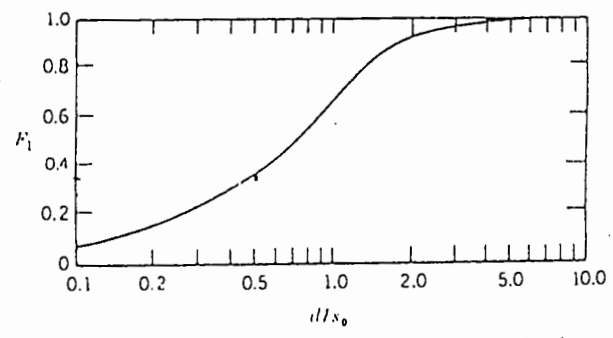


FIGURE 20.3 Correction factor F_1 for a thin wafer placed on a nonconducting surface as a function of d/s_0 . (From G. Knight Jr., Measurement of semiconductor parameters, in *Handbook of Semiconductor Electronics*, L. P. Hunter (ed.), p. 20.4. Copyright © 1962. Reprinted by permission of McGraw-Hill, Inc., New York.)

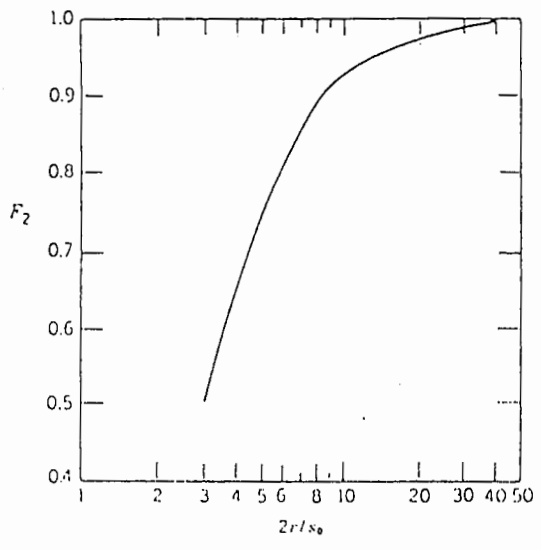


FIGURE 20.4 Correction factor F_2 for probes centered on a circular wafer of finite diameter $2r$ as a function of the ratio $2r/s_0$. (From F. M. Smits, Measurement of sheet resistivities with four-point probe, *Bell Syst. Tech. J.* vol. 37, part 1, May 1958; Table III, p. 716. Reprinted with permission. Copyright © 1958 AT&T.)