# UNIVERSITY OF SWAZILAND SUPPLEMENTARY EXAMINATIONS, JULY 2013 

FACULTY OF SCIENCE AND ENGINEERING DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

TITLE OF PAPER:

COURSE NUMBER:
EE221

TIME ALLOWED:
THREE HOURS

## INSTRUCTIONS:

1. There are five questions in this paper. Answer any FOUR questions.
2. Each question carries $\mathbf{2 5}$ marks.
3. Marks for different sections are shown on the right hand margin.
4. Clearly state the units of any values you calculate.
5. If you think not enough data has been given in any question you may assume any reasonable values.
6. A sheet containing useful formulae and other information is attached at the end.

## THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR

## QUESTION 1 (25 marks)

(a) The forward current in a diode is $32 \mu \mathrm{~A}$ when the diode forward voltage drop is 0.5 V , and 4.5 mA when the diode forward drop is 0.72 V . Using the approximate diode equation for a diode in forward bias, find
(i) The value of the parameter $n$ for the diode.
( 5 marks)
(i) The value of the parameter $I_{5}$.
(b) The forward voltage in a diode which has $n=1$ is increased by 0.06 V . By what factor does its forward current change?
(c) In Fig.Q1c, a source of 100 V r.m.s.supplies a sinusoidal a.c. voltage to a circuit made up of diodes and resistors. Assume that the diodes are ideal.
(i) Determine the behaviour of the diodes during each half-cycle.
(ii) Find the peak current in each of the resistors.
(iii) Sketch and clearly label the current waveforms in each resistor.


Fig. Q1c

## QUESTION 2 (25 marks)

(a) (I) Draw the circuit of a mains-operated full-wave diode bridge rectifier with capacitor smoothing.
(II) A full-wave bridge rectifier is supplied with a voltage $20 \sin 100 \pi t$ volts and feeds a load of $100 \Omega$ with $\mathrm{C}=2000 \mu \mathrm{~F}$. Assuming that the diode voltage drop is 0.7 V and may not be neglected, determine
(i) The load voltage.
(ii) The peak-to-peak ripple voltage.
(iii) The peak inverse voltage across each diode.
(iv) The peak current in the diodes.
(b) Figure Q. 2 b shows a simple application of a zener diode.
(i) Explain the operation of the circuit.
(ii) If $R_{\mathrm{L}}$ is removed from the circuit, find the power dissipated in the diode.
(iii) Find the range of $R_{\mathrm{L}}$ during which the zener diode is not conducting.
(iv) If a minimum current of 5 mA must be maintained in the zener diode for proper operation of the circuit, find the minimum value of $R_{\mathrm{L}}$ which may be used. (2 marks)


Fig.Q2b

## QUESTION 3 ( 25 marks)

(a) Consider the circuit shown in Fig.Q3a. Determine the quiescent values of base current, collector current and collector-emitter voltage when
(i) The current gain $\beta=50 \quad$ (6 marks)
(ii) The current gain $\beta=300$ (7 marks)
(ii) Comment on the two results above.


Fig. Q3a
(b) A transistor is biased as shown in Fig.Q3b. Determine the quiescent operating point of the transistor, assuming that $\beta=100$.


Fig.Q3b

## QUESTION 4 (25 marks)

(a) (i) List 3 important characteristics of an ideal opamp.
(ii) Show that the veltage gain of the opamp-based circuit in Fig.Q4a is given by

$$
\frac{v_{o}}{v_{i n}}=-\left(\frac{R_{4}}{R_{3}}\right)\left(\frac{R_{2} R_{3}}{R_{1} R_{2}+R_{2} R_{3}+R_{3} R_{1}}\right)
$$



Fig.Q4a
(b) Consider the opamp-based circuit shown in Fig.Q4b.
(i) Show that the output voltage and input voltages are related by

$$
\begin{equation*}
v_{o}=-\frac{1}{R C} \int_{0}\left(v_{1}+v_{2}\right) d t \tag{5marks}
\end{equation*}
$$

(ii) Hence find the output voltage when $R=100 \mathrm{k} \Omega, C=1 \mu \mathrm{~F}, v_{1}=3 \cos 10 t, v_{2}=5 \sin 20 t$


Fig.Q4b

## QUESTION 5 (25 marks)

(a) A transistor with $\mathrm{V}_{\mathrm{A}}=75 \mathrm{~V}$ is operated with a collector current of 2 mA and collector-emitter voltage of 10 V . The current gain is 150 .
(i) Find the parameters $g_{m}, r_{\pi}$, and $r_{0}$ at this operating point.
(ii) Draw the small signal ac equivalent circuit of the transistor.
(iii) If the transistor is supplied from a source of internal resistance $400 \Omega$ and the effective collector load is $2.7 \mathrm{k} \Omega$, find the voltage gain of the amplifier. Assume that the base bias resistors are very large compared with other resistors in the circuit.
(b) A circuit is to be designed which takes an input triangular wave of frequency 500 Hz with its amplitude changing between -5 V to +5 V and outputs a bipolar ( + and -) square-wave of same frequency but with amplitude oscillating between -10 V to +10 V . The phase relationship is that the square wave is positive whenever the triangular wave is decreasing in amplitude.
(i) Draw a sketch of the two waveforms and mark the amplitude and time axes. (3 marks)
(ii) Draw a suitable opamp-based circuit that can be used to effect the waveform change.
(iii) Derive a formula that can help you in your design.
(iv) Specify the components of your circuit, assuming all the components used are available in the E12 range.

## USEFUL INFORMATION AND FORMULAE

1. $\begin{array}{lllllllllllll}\text { E12 Range: } & 10 & 12 & 15 & 18 & 22 & 27 & 33 & 39 & 47 & 56 & 68 & 82\end{array}$
2. Diode: $\quad i_{D}=I_{S}\left(e^{\frac{v_{D}}{n V_{T}}}-1\right) \approx I_{S} e^{\frac{v_{D}}{n V_{T}}}$
3. BJT: $\quad i_{C}=\alpha I_{S}\left(e^{\frac{v_{B E}}{V_{T}}}-1\right)\left(1+\frac{V_{C E}}{V_{A}}\right)$
4. Half wave rectifier: $V_{r}=\frac{V_{m} T}{C R_{L}}, \quad \theta_{C}=\omega \Delta t=\sqrt{\frac{2 V_{r}}{V_{m}}}, \quad i_{\text {Dave }}=I_{L}\left(1+\pi \sqrt{\frac{2 V_{m}}{V_{r}}}\right)$

$$
i_{D \max }=I_{L}\left(1+2 \pi \sqrt{\frac{2 V_{m}}{V_{r}}}\right)
$$

5. Unless otherwise stated, assume that $V_{B E o n}=0.7 \mathrm{~V}, V_{C E s a t}=0.2 \mathrm{~V}$ and $V_{T}=25 \mathrm{mV}$.
6. Unless otherwise stated assume that opamps are ideal.
