UNIVERSITY OF SWAZILAND

FACULTY OF SCIENCE

DEPARTMENT OF ELECTRICAL & ELECTRONIC ENGINEERING

SUPPLEMENTARY EXAMINATION JULY 2013

DIGITAL SYSTEMS I

COURSE CODE – EE322

DURATION - 3 HOURS

INSTRUCTIONS TO CANDIDATES

i. There are FIVE questions in this paper. Answer any FOUR questions only.

ii. Each question carries equal marks.

iii. Show all your steps clearly in any calculations.

iv. State clearly any assumptions made.

v. Start each new question on a fresh page.

DO NOT OPEN THIS PAPER UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR.

Question 1

(a) Using the tabular method, minimize the following Boolean function:

$$F(A, B, C) = A'C + A'B + AB'C + BC \quad [12]$$

(b) Simplify the following using a k-map:

(i) $F = A'B'C' + B'CD' + A'BCD' + AB'C'$ [5]

(ii) $F(x, y, z) = \sum(0, 1, 2, 4, 5)$ [4]
$d(x, y, z) = \sum(3, 6, 7)$

(c) Using Boolean algebra simplify the following Boolean expression to a minimum number of literals:

$$F = w'z + xz + wx'z + x'y \quad [4]$$

Question 2

Analyse the combinational circuit shown in Figure Q2 and determine the following:

(a) Truth table. [12]
(b) Boolean function of the output F. [5]
(c) Timing Diagram showing how change in input relates to change in output with time. [8]

Show all working.

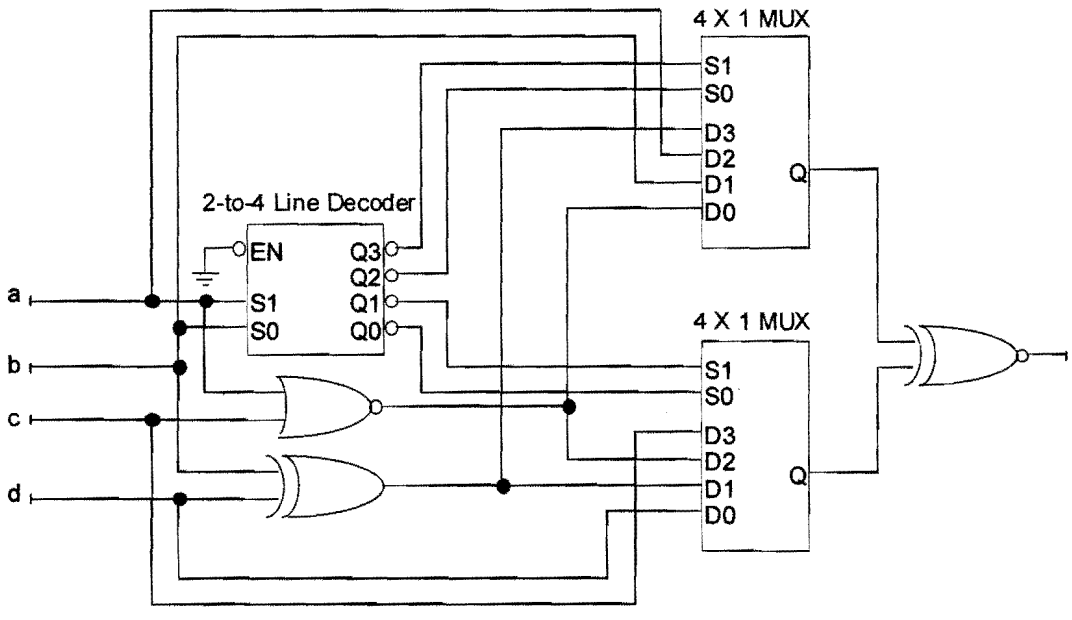

Figure Q2: Diagram for question 2

Question 3

(a) Derive the Boolean expressions for the output sum and output carry in a full adder circuit with inputs x_i, y_i, and c_i.

[6]

(b) Assuming that the *carry propagate* and *carry generate* are defined as

$$P_i = x_i + y_i$$
$$G_i = x_i y_i$$

respectively, show that the output carry and output sum of a full adder becomes

$$C_{i+1} = (C'_i G'_i + P'_i)' \quad [8]$$
$$S_i = (P_i G'_i) \oplus C_i \quad [7]$$

(c) Design a half-subtractor circuit with inputs x and y and outputs D and B. The circuit subtracts the bits x – y and places the difference in D and the borrow in B.

[4]

Question 4

(a) Figure Q4 is a waveform showing the behavior of a combinational circuit. A, B, and C are inputs, and X and Y are outputs. Implement the circuit and determine the function the circuit performs. [13]

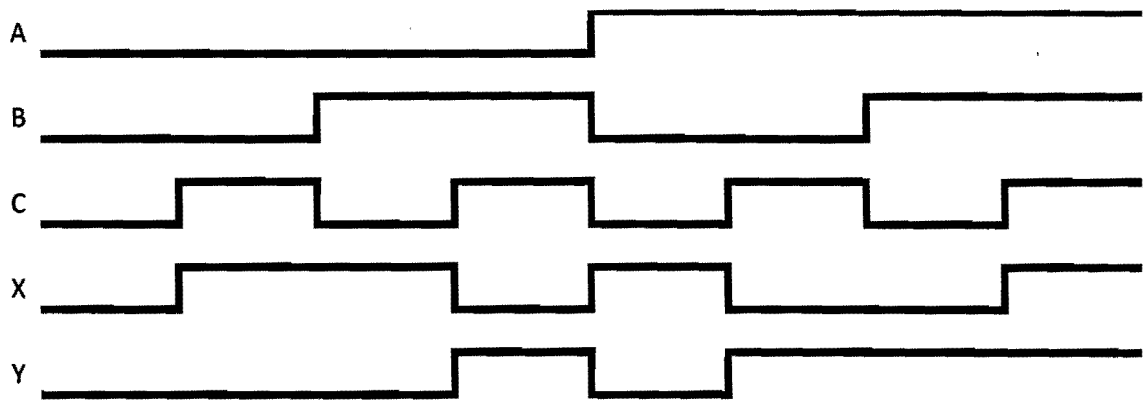

Figure Q4: Diagram for question 4 (a)

(b) Design a 4-bit Magnitude Comparator which compares two 4-bit binary numbers A, B and determines whether A<B, A>B, or A=B. [12]

Question 5

a) A combinational circuit is defined by the following three Boolean functions:

$$F_1(A, B, C) = \sum(2, 4, 7)$$
$$F_2(A, B, C) = \sum(0, 3)$$
$$F_3(A, B, C) = \sum(0, 2, 3, 4, 7)$$

Design the circuit with a decoder and a minimum number of external NAND gates. [7]

b)

i. Specify the truth table of an hexadecimal-to-binary priority encoder. In your truth table, provide an output V to indicate that at least one of the inputs is present. The input with the highest subscript number has the highest priority. [8]

ii. What will be the value of the four outputs if inputs D9 and D6 are at HIGH (logic 1) at the same time? [1]

c) Implement the following Boolean function with a 4 x 1 multiplexer and external gates. [5]

$$F(A, B, C, D) = \sum(0, 1, 3, 4, 8, 9, 15)$$

d) An 8 x 1 multiplexer has inputs A, B, and C connected to the selection inputs S_2, S_1, and S_0, respectively. The data inputs I_0 through I_7 are as follows: $I_1 = I_2 = I_7 = 0$; $I_3 = I_5 = 1$; $I_0 = I_4 = D$; and $I_6 = D'$. Determine the Boolean function that the multiplexer implements (express it is sum of products). [4]

END OF PAPER