# UNIVERSITY OF SWAZILAND SUPPLEMENTARY EXAMINATION, SECOND SEMESTER JULY 2016

## FACULTY OF SCIENCE AND ENGINEERING

# DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

TITLE OF PAPER:SOLID STATE ELECTRONICSCOURSE CODE:EE429

TIME ALLOWED: THREE HOURS

### **INSTRUCTIONS:**

- 1. There are FOUR questions in this paper. Answer all questions. Each question carries 25 marks.
- 2. If you think not enough data has been given in any question you may assume any reasonable values.
- 3. A list of useful Equations and constants is attached

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THIS PAPER CONTAINS NINE (8) PAGES INCLUDING THIS PAGE

### **QUESTION ONE (25 marks)**

- (a) Determine the number of atoms per unit cell in a face centered cubic Lattice. (3)
- (b) The volume density of atoms for a face centered cubic lattice is  $4 \times 10^{22}$  cm<sup>-3</sup>. Assume that the atoms are hard spheres with each atom touching its nearest neighbor. Determine the lattice constant and the radius of the atom. (5)
- (c) Given that the lattice constant of GaAs is 5.65, determine the number of Ga atoms and As atoms per cm<sup>3</sup>.
   (3)
- (d) According to classical physics, the average energy of an electron in an electron gas at thermal equilibrium is  $\frac{5kT}{2}$ . Determine, for T = 300 K,
  - (i) the average electron energy in eV(2)(ii) average electron momentum(3)(iii) the de Broglie wavelength.(4)
- (e) An electron and a photon have the same energy. At what value of energy (in eV) will the wavelength of the photon be 100 times that of the electron? (5)

(6)

#### **QUESTION TWO (25 marks)**

(a) Describe the lattice planes shown in the figure below:



- (b) The Fermi energy level for a particular material at T = 300 K is 4.25 eV. The electrons in this material follow the Fermi-Dirac distribution function.
  - (i) Find the probability of an energy level at 4.50 eV being occupied by an electron. (4)
  - (ii) What is the percentage change in Fermi energy level corresponding to a 100% increase in temperature, assume E<sub>F</sub> is constant?
  - (iii) Assume that the Fermi energy level is 0.28 eV above the valence band energy.
     Determine the probability of a state being empty of an electron at E<sub>v</sub>. What does the value obtained mean?
- (c) Show that the probability of an energy state being occupied  $\Delta E$  above the Fermi energy is the same as the probability of a state being empty  $\Delta E$  below the Femi level. (5)

#### **QUESTION THREE (25 marks)**

a) Consider a uniformly doped silicon pn junction with doping	concentrations
$N_a = 5 \times 10^{17} \text{ cm}^{-3}$ and $N_d = 10^{17} \text{ cm}^{-3}$ .	
(i) Calculate $V_{bi}$ at T = 300 K.	(2)
The junction has a cross-sectional area of $10^{-4}$ cm <sup>2</sup> and has an app	lied reverse-bias
voltage of $V_R = 5$ V. Calculate	
(ii) the depletion region width W.	(4)
(iii) E <sub>max</sub>	(2)
(iv) the total junction capacitance.	(2)

- (b) A Schottky diode is formed by depositing Au on n-type GaAs doped at  $N_d = 5 \times 10^{16} \text{ cm}^{-3}$ , T = 300K. Determine the forward-bias voltage required to obtain  $J_n = 5\text{A/cm}^2$ . Assume  $\emptyset_{Bn} = 0.867V$ . (6)
- (c) Consider an n-channel MOSFET with W =  $15\mu m$ , L =  $2\mu m$ , and  $C_{ox} = 6.9 \times 10^{-8} F/cm^2$ . When the transistor is biased in the saturation region, the drain current is  $I_{D(sat)} = 35\mu A$  at  $V_{GS} = 1.5$  V and  $I_{D(sat)} = 75\mu A$  at  $V_{GS} = 2.5$  V. Determine the electron mobility and the threshold voltage. Assume  $V_{GS} = 0.10$ V (5)
- (d) Consider a p-channel GaAs pn JFET at T 300 K. The parameters are  $N_d = 10^{18} cm^{-3}$ and  $a = 0.65 \mu m$ . Determine the channel doping concentration such that the internal pinch-off voltage is  $V_{PO}$ =2.75 V. (4)

(2)

### **QUESTION FOUR (25 marks)**

- (a) The experimentally measured junction capacitance of a one-sided silicon n+p junction biased at  $V_R = 3$  V and at T = 300 K is C= 0.105 pF. The built-in potential barrier is found to be  $V_{bi} = 0.765$  V. The cross-sectional area is A = 10<sup>-5</sup> cm<sup>2</sup>. Find the doping concentrations. (5)
- (b) Consider a silicon pn junction at T=300 K with a p-type doping concentration of  $N_a = 2 \times 10^{17} cm^{-3}$ .
  - (i) Determine the n-type doping concentration such that the maximum electric field is  $E_{max} = 2 \times 10^5$  V/cm at a reverse-biased voltage of  $V_R = 25$  V. (3)
  - (ii) What is the junction capacitance given that  $A = 3 \times 10^{-3} cm^2$ ? (3)
  - (iii)What is the difference between Avalanche breakdown and Zener breakdown in pn junctions?
- (c) An n<sup>+</sup>p silicon diode at T=300K has the following parameters:  $N_d = 10^{18} \text{ cm}^{-3}$ ,  $N_a = 10^{16} \text{ cm}^{-3}$ ,  $D_n = 25 \text{ cm}^2/\text{s}$ ,  $D_p = 10 \text{ cm}^2/\text{s}$ .  $\tau_{n0} = \tau_{p0} = 1\mu\text{s}$ , and  $A = 10^{-4} \text{ cm}^2$ Determine the diode current for a forward-bias voltage of 0.8 V (5)
- (d) Consider an n-type gallium arsenide semiconductor at T = 300 K doped at  $N_d = 5 \times 10^{16} cm^{-3}$ .
  - (i) Determine  $E_{Fn} E_F$  if the excess-carrier concentration is  $0.01N_d$  (3)
  - (ii) Determine  $E_{Fi} E_{Fp}$

## **USEFUL INFORMATION AND EQUATIONS**

$$J_{p}(x_{n}) = -eD_{p} \frac{d(\delta p_{n}(x))}{dx}\Big|_{x=x_{n}} \qquad J_{p}(x_{n}) = \frac{eD_{p}p_{0}}{L_{p}} \left[\exp\left(\frac{eV_{n}}{kT}\right) - 1\right] \qquad n_{0} = n_{i} \exp\left[\frac{E_{x} - E_{F_{i}}}{kT}\right]$$

$$J_{n}(-x_{p}) = eD_{n} \frac{d(\delta n_{p}(x))}{dx}\Big|_{x=-x_{p}} \qquad J_{n}(-x_{p}) = \frac{eD_{n}n_{p0}}{L_{n}} \left[\exp\left(\frac{eV_{n}}{kT}\right) - 1\right] \qquad p_{0} = n_{i} \exp\left[\frac{-(E_{r} - E_{r})}{kT}\right]$$

$$\delta n_{p}(x) = n_{p}(x) - n_{-0} = n_{p0} \left[\exp\left(\frac{eV_{n}}{kT}\right) - 1\right] \exp\left(\frac{x_{p} + x}{L_{n}}\right) \qquad E_{F_{i}} - E_{nidgep} = \frac{3}{4} kT \ln\left(\frac{m_{p}^{*}}{m_{n}^{*}}\right)$$

$$\sigma \approx e\mu_{n} n = e\mu_{n}(N_{n} - N_{n})$$

$$\delta p_{n}(x) = p_{n}(x) - p_{n0} = p_{nc} \left[\exp\left(\frac{eV_{n}}{kT}\right) - 1\right] \exp\left(\frac{x_{n} - x}{L_{p}}\right) \qquad \sigma \approx e\mu_{p}p = e\mu_{p}(N_{n} - N_{n})$$

$$L_{p}^{2} = D_{p}\tau_{p0} \qquad L_{n}^{2} = D_{n}\tau_{n0} \qquad J \propto \exp\left(\frac{-E_{t}}{kT}\right) \exp\left(\frac{eV_{n}}{kT}\right) \qquad J_{i} = en_{i}^{2}\left(\frac{1}{N_{n}}\sqrt{\frac{D_{n}}{T_{n}}} + \frac{1}{N_{d}}\sqrt{\frac{D_{n}}{T_{p0}}}\right)$$

$$V_{N} = \frac{kT}{e} \ln\left(\frac{N_{n}N_{d}}{n_{i}^{2}}\right) = V_{r} \ln\left(\frac{N_{n}N_{d}}{n_{i}^{2}}\right) \qquad E_{max} = -\left\{\frac{2e(V_{N} + V_{n})}{e}\left(\frac{N_{n}N_{d}}{N_{n} + N_{d}}\right)\right\}^{1/2} \qquad A^{*} = \frac{4\pi em_{n}^{*}k^{2}}{h^{3}}$$

$$W = \left\{\frac{2\epsilon_{n}(V_{bi} + V_{R})}{e}\left[\frac{N_{n}}{N_{n}}A_{n}d\right]\right\}^{1/2} \qquad C^{*} = \left\{\frac{e\epsilon_{n}N_{n}N_{d}}{2(V_{bi} + V_{k})(N_{n} + N_{d})}\right\}^{1/2} \qquad J_{ar} = A^{*}T^{2} \exp\left(\frac{-e\phi_{n}}{kT}\right)$$
Typical mobility values at  $T = 300$  K and low doping concentrations
$$I_{D} = \frac{W\mu_{n}C_{cx}}{L} \left(V_{cS} - V_{T}\right)V_{DS}$$

Typical mobility values at T = 300 K and low doping concentrations

	μ, (cm²/V-s)	μ, (cm²/V-5)
Silicon	1350	480
Gallium arsenide	8500	400
Germanium	3900	1900

Work	functions	of some	elements
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Element	Work function, $\phi_{\sigma}$
Ag, silver	4.26
Al, aluminum	4.28
Au, gold	5.1
Cr, chromium	4.5
Mo, molybdenum	4.6
Ni, nickel	5.15
Pd, palladium	5.12
Pt. platinum	5.65
Ti, titanium	4.33
W, tungsten	4.55

Commonly accepted values of  $n_i$  at T = 300 K.

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Silicon	$n_i = 1.5 \times 10^{10} \mathrm{cm}^{-3}$
Gallium arsenide	$n_i = 1.8 \times 10^6 \mathrm{cm}^{-3}$
Germanium	$n_i = 2.4 \times 10^{13} \mathrm{cm}^{-3}$

Electron affinity of some semiconductors

Element	Electron affinity, $\chi$
Ge, germanium	4.13
Si, silicon	4.01
GaAs, gallium arsenide	4.07
AlAs, aluminum arsenide	3.5

 $V_{p0} = \frac{ea^2 N_q}{2\epsilon_s}$ 

## PHYSICAL CONSTANTS

Physical constants

atoms per gram molecular weightBoltzmann's constant $k = 1.38 \times 10^{-23}$ J/K $= 8.62 \times 10^{-5}$ eV/KElectronic charge (magnitude) $e = 1.60 \times 10^{-19}$ CFree electron rest mass $m_0 = 9.11 \times 10^{-31}$ kg $\mu_0 = 4\pi \times 10^{-7}$ H/mPermeability of free space $\mu_0 = 4\pi \times 10^{-7}$ H/mPermittivity of free space $\epsilon_0 = 8.85 \times 10^{-14}$ F/cm $= 8.85 \times 10^{-12}$ F/mPlanck's constant $h = 6.625 \times 10^{-34}$ J-s $= 4.135 \times 10^{-15}$ eV-sProton rest mass $M = 1.67 \times 10^{-27}$ kg $c = 2.998 \times 10^{10}$ cm/sThermal voltage ( $T = 300$ K) $V_i = \frac{kT}{e} = 0.0259$ V $kT = 0.0259$ eV	Avogadro's number	$N_A = 6.02 \times 10^{+23}$
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Permittivity of free space $\epsilon_0 = 8.85 \times 10^{-14}$ F/cm $= 8.85 \times 10^{-12}$ F/mPlanck's constant $h = 6.625 \times 10^{-34}$ J-s $= 4.135 \times 10^{-15}$ eV-s $\frac{h}{2\pi} = \hbar = 1.054 \times 10^{-34}$ J-s $= 1.67 \times 10^{-27}$ kg Speed of light in vacuum $M = 1.67 \times 10^{-27}$ kg $c = 2.998 \times 10^{10}$ cm/sThermal voltage (T = 300 K) $V_t = \frac{kT}{e} = 0.0259$ V $kT = 0.0259$ eV	Permeability of free space	$\mu_0=4\pi imes 10^{-7}$ H/m
Planck's constant       = $8.85 \times 10^{-12}$ F/m         h = $6.625 \times 10^{-34}$ J-s         = $4.135 \times 10^{-15}$ eV-s $\frac{h}{2\pi} = \hbar = 1.054 \times 10^{-34}$ J-s         Proton rest mass         M = $1.67 \times 10^{-27}$ kg         Speed of light in vacuum         C = $2.998 \times 10^{10}$ cm/s         Thermal voltage (T = 300 K)         V <sub>t</sub> = $\frac{kT}{e} = 0.0259$ V         kT = 0.0259 eV	Permittivity of free space	$\epsilon_0 = 8.85  imes 10^{-14}$ F/cm
Planck's constant $h = 6.625 \times 10^{-34}  \text{J-s}$ $= 4.135 \times 10^{-15}  \text{eV-s}$ $\frac{h}{2\pi} = \hbar = 1.054 \times 10^{-34}  \text{J-s}$ Proton rest massProton rest mass $M = 1.67 \times 10^{-27}  \text{kg}$ $c = 2.998 \times 10^{10}  \text{cm/s}$ Speed of light in vacuum $c = 2.998 \times 10^{10}  \text{cm/s}$ Thermal voltage ( $T = 300  \text{K}$ ) $V_t = \frac{kT}{e} = 0.0259  \text{V}$ $kT = 0.0259  \text{eV}$		$= 8.85 \times 10^{-12}$ F/m
$= 4.135 \times 10^{-15} \text{ eV-s}$ $\frac{h}{2\pi} = \hbar = 1.054 \times 10^{-34} \text{ J-s}$ Proton rest mass $M = 1.67 \times 10^{-27} \text{ kg}$ Speed of light in vacuum $c = 2.998 \times 10^{10} \text{ cm/s}$ Thermal voltage (T = 300 K) $V_t = \frac{kT}{e} = 0.0259 \text{ V}$ $kT = 0.0259 \text{ eV}$	Planck's constant	$h = 6.625 \times 10^{-34}  \text{J}_{-8}$
$\frac{h}{2\pi} = \hbar = 1.054 \times 10^{-34} \text{ J-s}$ Proton rest mass Speed of light in vacuum Thermal voltage (T = 300 K) $K_{t} = \frac{kT}{e} = 0.0259 \text{ V}$ kT = 0.0259  eV		$= 4.135 \times 10^{-15} \mathrm{eV}$ -s
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Proton rest mass $M = 1.67 \times 10^{-27}$ kgSpeed of light in vacuum $c = 2.998 \times 10^{10}$ cm/sThermal voltage ( $T = 300$ K) $V_t = \frac{kT}{e} = 0.0259$ V $kT = 0.0259$ eV		$\frac{1}{2\pi}$ = $n = 1.054 \times 10^{-3}$
Speed of light in vacuum $c = 2.998 \times 10^{10}$ cm/sThermal voltage (T = 300 K) $V_t = \frac{kT}{e} = 0.0259$ V $kT = 0.0259$ eV	Proton rest mass	$M = 1.67  imes 10^{-27}  \mathrm{kg}$
Thermal voltage ( $T = 300 \text{ K}$ ) $V_t = \frac{kT}{e} = 0.0259 \text{ V}$ kT = 0.0259  eV	Speed of light in vacuum	$c = 2.998  imes 10^{10}  { m cm/s}$
kT = 0.0259  eV	Thermal voltage ( $T = 300 \text{ K}$ )	$V_t = \frac{kT}{e} = 0.0259 \text{ V}$
		kT = 0.0259  eV

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Property	Si	GaAs	Ge
Atoms (cm <sup>-3</sup> )	$5.0  imes 10^{22}$	$4.42 \times 10^{22}$	$4.42 \times 10^{22}$
Atomic weight	28.09	144.63	72.60
Crystal structure	Diamond	Zincblende	Diamond
Density (g/cm <sup>3</sup> )	2.33	5.32	5.33
Lattice constant (Å)	5.43	5.65	5.65
Melting point (°C)	1415	1238	937
Dielectric constant	11.7	13.1	16.0
Bandgap energy (eV)	1.12	1.42	0.66
Electron affinity, $\chi$ (V)	4.01	4.07	4.13
Effective density of states in conduction band, $N_c$ (cm <sup>-3</sup> )	$2.8 \times 10^{19}$	$4.7 \times 10^{17}$	$1.04 \times 10^{19}$
Effective density of states in valence band, $N_{\nu}$ (cm <sup>-3</sup> )	$1.04 \times 10^{19}$	$7.0 \times 10^{18}$	$6.0  imes 10^{18}$
Intrinsic carrier concentration (cm <sup>-3</sup> )	$1.5 \times 10^{10}$	$1.8  imes 10^{6}$	$2.4  imes 10^{13}$
Mobility (cm <sup>2</sup> /V-s)			
Electron, $\mu_n$	1350	8500	3900
Hole, $\mu_p$	480	400	1900
Effective mass $\left(\frac{m^*}{m_0}\right)$			
Electrons	$m_l^* = 0.98$	0.067	1.64
	$m_t^* = 0.19$		0.082
Holes	$m_{th}^* = 0.16$	0.082	0.044
	$m_{hh}^* = 0.49$	0.45	0.28
Density of states effective mass			
Electrons $\left(\frac{m_{dn}^*}{m_o}\right)$	1.08	0.067	0.55
Holes $\left(\frac{m_{dp}^*}{m_a}\right)$	0.56	0.48	0.37
Conductivity effective mass			
Electrons $\left(\frac{m_{cn}^*}{m_a}\right)$	0.26	0.067	0.12
Holes $\left(\frac{m_{cp}^*}{m_s}\right)$	0.37	0.34	0.21