# UNIVERSITY OF SWAZILAND <br> SUPPLEMENTARY EXAMINATION, SECOND SEMESTER JULY 2017 

## FACULTY OF SCIENCE AND ENGINEERING

## DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

TITLE OF PAPER: SOLID STATE ELECTRONICS COURSE CODE: EE429<br>TIME ALLOWED: THREE HOURS

## INSTRUCTIONS:

1. There are FOUR questions in this paper. Answer all questions. Each question carries 25 marks.
2. If you think not enough data has been given in any question you may assume any reasonable values.
3. A list of useful Equations and constants is attached

THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR

## QUESTION ONE (25 marks)

a) Determine the number of atoms per unit cell in a body centered cubic Lattice.
b) For each of the diagrams below, determine
i. The plane shown (shaded)
ii. The direction indicated by the arrow.

A.

B.

C.
c) Consider the plane (100) in a face centered cubic lattice. Determine
i. The number of atoms in the plane
ii. The surface density of the atoms if the lattice constant is $5 \AA$. NB: the surface density is the number of atoms per plane / surface area of the plane.
d) The probability that a state at $E_{C}+k T$ is occupied by an electron is equal to the probability that a state at $E_{v}-k T$ is empty. Determine the position of the Fermi energy level as a function of $E_{c}$ and $E_{v}$.
e) The de Broglie wavelength of an electron is $85 \AA$. Determine the electron energy (eV), momentum, and velocity.
f) Given that the lattice constant of GaAs is 5.65 , determine the number of Ga atoms and As atoms per $\mathrm{cm}^{3}$.

## QUESTION TWO (25 marks)

a) If the density of states function in the conduction band of a particular semiconductor is a constant equal to $g_{c}(E)=K$ where $K$ is a constant, derive the expression for the thermal-equilibrium concentration of electrons in the conduction band, assuming Fermi-Dirac statistics and assuming the Boltzmann approximation is valid.
b) Silicon at $\mathrm{T}=300 \mathrm{~K}$ is doped with acceptor atoms at a concentration of $7 \times 10^{15} \mathrm{~cm}^{-3}$
i. Determine $E_{F}-E_{V}$.
ii. Calculate the concentration of acceptor atoms that must be added to move the position of the Fermi level 1 kT closer to the valence-band edge
c) Consider a sample of silicon at $\mathrm{T}=300 \mathrm{~K}$. Assume that the electron concentration varies linearly with distance as shown in the figure below. The diffusion current density is found to be $J_{n}=0.19 \mathrm{~A} / \mathrm{cm}^{2}$. If the electron diffusion coefficient is $D_{n}=25 \mathrm{~cm}^{2} / \mathrm{s}$, determine the electron concentration at $\mathrm{x}=0$.

d) The electron concentration at $\mathrm{T}=300 \mathrm{~K}$ is given by

$$
n(x)=10^{16} \exp \left(\frac{-x}{18}\right) \mathrm{cm}^{-3}
$$

where $x$ is measured in Nm and is limited to $0 \leq x \leq 25$. The electron diffusion coefficient is $D_{n}=25 \mathrm{~cm}^{2} / \mathrm{s}$ and the electron mobility is $\mu_{\mathrm{n}}=960 \mathrm{~cm}^{2} / \mathrm{Vs}$. The total current density through the semiconductor is constant and equal to $J_{n}=$ $40 \mathrm{~A} / \mathrm{cm}^{2}$. The electron current density has both drift and diffusion current density components. Determine the electric field as a function of $x$ which must exist in the semiconductor.

## QUESTION THREE (25 marks)

(a) In Silicon, the hole concentration is given by $p(x)=10^{15} \exp \left(-x / L_{p}\right)$ for $x \geq 0$ and the electron concentration is given by $n(x)=5 \times 10^{14} \exp \left(x / L_{n}\right)$ for $x \leq 0$. The values of $L_{p}$ and $L_{n}$ are $5 \times 10^{-4} \mathrm{~cm}$ and $10^{-3} \mathrm{~cm}$ respectively. The hole and electron diffusion coefficient are $10 \mathrm{~cm}^{2} / \mathrm{s}$ and $25 \mathrm{~cm}^{2 / s}$ respectively. The total current density is defined as the sum of the hole diffusion current density at $x=0$ and the electron diffusion current density at $x=0$. Calculate the total current density.
(b) Consider the ideal long silicon pn junction shown in the figure below at $\mathrm{T}=300 \mathrm{~K}$. The n -region is doped with $10^{16}$ donor atoms per $\mathrm{cm}^{3}$ and the p -region is doped with $5 \times 10^{16}$ acceptor atoms per $\mathrm{cm}^{3}$. The minority carrier lifetimes are $\tau_{n 0}=0.05 \mu \mathrm{~s}$ and $\tau_{p 0}=0.01 \mu \mathrm{~s}$. The minority carrier diffusion coefficients are $D_{n}=23 \mathrm{~cm}^{2} / \mathrm{s}$ and $D_{p}=8 \mathrm{~cm}^{2} / \mathrm{s}$. The forward-bias voltage is $V_{a}=0.610 \mathrm{~V}$.


Calculate
(i) the excess hole concentration as a function of $x$ for $x \geq 0$
(ii) the hole diffusion current density at $x=3 \times 10^{-4} \mathrm{~cm}$
(c) Consider a uniformly doped silicon pn junction with doping concentrations $N_{a}=$ $5 \times 10^{17} \mathrm{~cm}^{-3}$ and $N_{d}=10^{17} \mathrm{~cm}^{-3}$.
(i) Calculate $V_{b i}$ at $\mathrm{T}=300 \mathrm{~K}$.

The junction has a cross-sectional area of $10^{-4} \mathrm{~cm}^{2}$ and has an applied reverse-bias voltage of $\mathrm{V}_{\mathrm{R}}=5 \mathrm{~V}$. Calculate
(ii) the depletion region width $W$.
(iii) $E_{\max }$
(iv) the total junction capacitance.
(d) A Schottky diode is formed by depositing Au on n-type GaAs d ped at $N_{d}=$ $5 \times 10^{16} \mathrm{~cm}^{-3}, \mathrm{~T}=300 \mathrm{~K}$. Determine the forward-bias voltage required to obtain $J_{n}=$ $5 \mathrm{~A} / \mathrm{cm}^{2}$. Assume $\emptyset_{B n}=0.867 \mathrm{~V}$.

## QUESTION FOUR ( 25 marks)

(a) A silicon pn junction in thermal equilibrium at $\mathrm{T}=300 \mathrm{~K}$ is doped such that $E_{F}-E_{F i}=0.365 \mathrm{eV}$ in the n region and $E_{F i}-E_{F}=0.33 \mathrm{eV}$ in the p region.
(i) Sketch the energy band diagram for the pn junction.
(ii) Find the impurity concentration in each region.
(iii) Determine $V_{b i}$.
(b) Consider a uniformly doped silicon pn junction at $\mathrm{T}=300 \mathrm{~K}$. At zero bias, $20 \%$ of the total space charge region is in the p region. The built in potential barrier is $V_{b i}=$ 0.71 V . Determine
(i) $N_{a}$
(ii) $N_{d}$
(iii) $X_{n}$
(iv) $X_{p}$
(v) $\left|E_{\max }\right|$

## USEFUL INFORMATION AND EOUATIONS

$$
\begin{aligned}
& L_{n}=q \mu_{n} n E+q D_{n} \frac{d n}{d x} \\
& J_{p}\left(x_{n}\right)=-\left.\varepsilon D_{p} \frac{d\left(\delta_{p}(v)\right.}{d x}\right|_{x-n} \quad J_{p}\left(x_{n}\right)=\frac{e D_{p} p_{r}}{L_{r}}\left[\exp \left(\frac{\epsilon}{d T}\right)-1\right] \quad n_{p}=n_{i} \exp \left[\frac{E_{r}-E_{R_{i}}}{k T}\right]
\end{aligned}
$$

$$
\begin{aligned}
& 8 n_{p}(x)=n(x)-n_{n}=n_{m}\left[\exp \left(\frac{c V_{e}}{K T}\right)-1\right] \exp \left(\frac{x_{s}-x}{L_{n}}\right) \\
& E_{f:}-E_{\text {rise }}=\frac{3}{4} k T \ln \left(\frac{m_{r}^{*}}{m_{n}^{*}}\right) \\
& \sigma=\tilde{C H}_{a} h=\varepsilon_{\mu_{n}}\left(N_{4}-N_{a}\right\} \\
& \delta p_{x}(x)=p_{\mathrm{T}}(x)-p_{\mathrm{n}}=p_{\mathrm{m}}\left[\exp \left(\frac{e V_{a}}{K T}\right)-1\right] \exp \left(\frac{x_{\sigma}-x}{L_{\Gamma}}\right) \\
& \sigma=e \mu_{s} \beta=c \mu_{i}\left(N_{w}-N s\right.
\end{aligned}
$$

$$
\begin{aligned}
& \text { Typical mothithy values at } T=300 \mathrm{k} \text { and low doping concentrations } \quad I_{0}=\frac{W \mu_{n} C_{0 s}}{L}\left(V_{O S}-V_{D}\right) V_{D S} \\
& \text { Conmonly atomptratue of in at } T=360 \mathrm{~K} \\
& \text { Gemaniun } \\
& 3=2.4 \times 10^{10} \mathrm{~cm}^{-3}
\end{aligned}
$$

## PHYSICAL CONSTANTS

Physical constants

| Avogadro's number | $N_{4}=6.02 \times 10^{-23}$ <br> atoms per gram molecular weight |
| :---: | :---: |
| Boltzmann's constant | $\begin{aligned} k & =1.38 \times 10^{-13} \mathrm{~J} / \mathrm{K} \\ & =8.62 \times 10^{-5} \mathrm{eV} / \mathrm{K} \end{aligned}$ |
| Electronic charge (magnitude) | $e=1.60 \times 10^{-19} \mathrm{C}$ |
| Free electron rest mass | $m_{6}=9.11 \times 10^{-31} \mathrm{~kg}$ |
| Permeability of free space | $\mu_{0}=4 \pi \times 10^{-7} \mathrm{H} / \mathrm{m}$ |
| Permitivity of free space | $\begin{aligned} \epsilon_{0} & =8.85 \times 10^{-14} \mathrm{~F} / \mathrm{cm} \\ & =8.85 \times 10^{-12} \mathrm{~F} / \mathrm{m} \end{aligned}$ |
| Planck's constant | $\begin{aligned} h & =6.625 \times 10^{-34} \mathrm{~J}-\mathrm{s} \\ & =4.135 \times 10^{-15} \mathrm{eV}-\mathrm{s} \end{aligned}$ |
|  | $\frac{h}{2 \pi}=\hbar=1.054 \times 10^{-34} \mathrm{~J}-\mathrm{s}$ |
| Proton rest mass | $M=1.67 \times 10^{-27} \mathrm{~kg}$ |
| Speed of lighe in vacuum | $c=2.998 \times 10^{10} \mathrm{~cm} / \mathrm{s}$ |
| Themal voltage ( $T=300 \mathrm{~K}$ ) | $V_{:}=\frac{k T}{e}=0.0259 \mathrm{~V}$ |
|  | $k T=0.0259 \mathrm{eV}$ |

Silicon, gallium arsenide, and germanium properties ( $T=300 \mathrm{~K}$ )

| Property | Si | GaAs | Ge |
| :---: | :---: | :---: | :---: |
| Atoms ( $\mathrm{cm}^{-3}$ ) | $5.0 \times 10^{22}$ | $4.42 \times 10^{22}$ | $4.42 \times 10^{2}$ |
| Atomic weight | 28.09 | 144.63 | 72.60 |
| Crystal structure | Diamond | Zincblende | Diamond |
|  | 2.33 | 5.32 | 5.33 |
| Lattice constant (A) | 5.43 | 5.65 | 5.65 |
| Melting point ( ${ }^{\circ} \mathrm{C}$ ) | 1415 | 1238 | 937 |
| Dielectric constant | 11.7 | 13.1 | 16.0 |
| Bandgap energy ( $\mathrm{V}^{\prime}$ ) | 1.12 | 1.42 | 0.66 |
| Electron affinity, $\chi$ (V) | 4.01 | 4.07 | 4.13 |
| Effective densily of states in conduction band, $N$. $\left(\mathrm{cm}^{-3}\right)$ | $2.8 \times 10^{19}$ | $4.7 \times 10^{17}$ | $1.04 \times 10^{99}$ |
| Effective density of states in valence band. $N_{\mathrm{v}}\left(\mathrm{cm}^{-3}\right)$ | $1.04 \times 10^{19}$ | $7.0 \times 10^{18}$ | $6.0 \times 10^{\text {is }}$ |
| Intrinsic carrier concentration $\left\langle\mathrm{cm}^{-3}\right.$ ) | $1.5 \times 10^{3}$ | $1.8 \times 10^{\circ}$ | $2.4 \times 10^{13}$ |
| Mobility ( $\mathrm{cm}^{2 /} / \mathrm{V}$-s) |  |  |  |
| Electron, $\mu_{n}$ | 1350 | 8500 | 3900 |
| Hole $\mu_{5}$ | 480 | 400 | 1900 |
| Effective mass $\left(\frac{m^{*}}{M_{g}}\right)$ |  |  |  |
| Electrons | $m_{j}^{*}=0.98$ | 0.067 | 1.64 |
|  | $m_{t}^{*}=0.19$ |  | 0.082 |
| Holes | $m_{m=0}^{*}=0.16$ | 0.082 | 0.044 |
|  | $m^{2}=0.49$ | 0.45 | 0.28 |
| Density of states effective mass |  |  |  |
| Electrons $\binom{m_{\infty}^{*}}{m^{*}}$ | 1.08 | 0.067 | 0.55 |
| Holes ( $m_{\text {mi }}{ }^{\text {m }}$ ) | 0.56 | 0.48 | 0.37 |
| Conductivity effective mass |  |  |  |
| Electrons $\left(\frac{m_{0}^{*}}{m_{0}}\right)$ | 0.26 | 0.067 | 0.12 |
| Holes ( $\frac{m_{3}^{*}}{m_{n}}$ ) | 0.37 | 0.34 | 0.21 |

