

UNIVERSITY OF ESWATINI
FACULTY OF SCIENCE & ENGINEERING
DEPARTMENT OF ELECTRICAL & ELECTRONIC ENGINEERING
DIGITAL SYSTEMS
COURSE CODE – EEE323
MAIN EXAMINATION
DECEMBER 2018
DURATION OF THE EXAMINATION - 3 HOURS

INSTRUCTIONS TO STUDENTS

1. There are **FIVE** questions in this paper. Answer any **FOUR** questions.
2. Each question carries 25 marks.
3. Show all your steps clearly in any calculations/work.
4. Start each new question on a fresh page.
5. Make sure that this exam contains 3 pages including this one.

DO NOT OPEN THIS PAPER UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR.

QUESTION ONE (25 marks)

- (a) (8 pts) Perform subtraction on the following unsigned binary numbers using 1's and 2's complement of the subtrahend.
- (i) $11010 - 1101$
 - (ii) $1000 - 110000$
- (b) (6 pts) Find the maxterm expansion for $F = xy + x'z$.
- (c) (5 pts) Simplify $f(x, y, z) = \prod(1,4,5,6)$ to a product of 2 sums.
- (d) (6 pts) Represent decimal 6137 in
- (i) BCD
 - (ii) Excess-3 code
 - (iii) 6311 code

QUESTION TWO (25 marks)

- a) (10 pts) For the function $f(A, B, C, D) = \sum(1,3,7,11,15)$, $d(A, B, C, D) = \sum(0,2,5)$,
- (i) find a minimum sum-of-products expression,
 - (ii) Find a minimum product-of-sums expression.
- b) (6 pts) Indicate how a NOR gate can be used to implement:
- (i) An Inverter:
 - (ii) An OR Gate:
 - (iii) An AND Gate:
- c) (9 pts) Implement the following Boolean function F , together with the don't-care conditions d , using no more than two NOR gates:

$$F(A, B, C, D) = \sum(2, 4, 6, 10, 12)$$
$$d(A, B, C, D) = \sum(0, 8, 9, 13)$$

Assume that both the normal and complement inputs are available.

QUESTION THREE (25 marks)

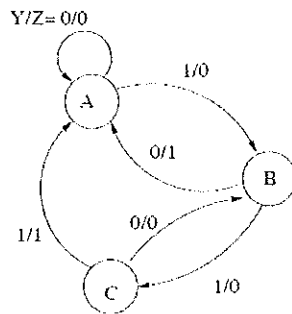
- (a) (7 pts) Implement the following Boolean function with a multiplexer:
- $$F(A, B, C, D) = \sum(0, 1, 3, 4, 7, 12, 13, 14)$$
- (b) (8 pts) Draw a NAND logic diagram that implements the complement of the following function:

$$F(A, B, C, D) = \sum(0, 1, 2, 3, 6, 8, 10, 11, 14)$$

- (c) (5 pts) A *PN* flip-flop has four operations: clear to 0, no change, complement, and set to 1, when inputs *P* and *N* are 00, 01, 10, and 11, respectively. Tabulate the characteristic table and derive the characteristic equation.
- (d) (5 pts) Write the characteristic equations and the excitation tables for D, T and JK flip-flops.

QUESTION FOUR (25 marks)

- (a) (7 pts) Design a half-subtractor circuit with inputs *x* and *y* and outputs *D* and *B*. The circuit subtracts the bits $x - y$ and places the difference in *D* and the borrow in *B*.
- (b) (10 pts) Design a full-subtractor circuit with three inputs *x*, *y*, *z* and two outputs *D* and *B*. The circuit subtracts $x - y - z$, where *z* is the input borrow, *B* is the output borrow, and *D* is the difference.
- (c) (8 pts) Convert the state diagram of figure below to ASM chart.



QUESTION FIVE (25 marks)

- (a) (5 pts) Explain the difference between a **Moore** machine and a **Mealy** machine. Draw a block diagram indicating the structure of a general state machine. Indicate on the diagram where one can find the **present state** and **next state**.
- (b) 10 pts.) Design a counter with *T* flip-flops that goes through the following binary repeated sequence: 0, 1, 3, 7, 6, 4.
- (c) (10 pts) A sequential circuit has two *JK* flip-flops *A* and *B* and one input *x*. The circuit is described by the following flip-flop input equations:

$$J_A = x, \quad K_A = B$$

$$J_B = x, \quad K_B = A'$$
 - (i) Derive the state equations A^+ and B^+ by substituting the input equations for the *J* and *K* variables.
 - (ii) Draw the state diagram of the circuit. You must tabulate state table first.