

**UNIVERSITY OF SWAZILAND**  
**FACULTY OF SCIENCE**  
**DEPARTMENT OF PHYSICS**  
**SUPPLEMENTARY EXAMINATION 2006**

**TITLE OF PAPER:** MODERN PHYSICS & WAVE OPTICS  
**COURSE NUMBER:** P231  
**TIME ALLOWED:** THREE HOURS  
**INSTRUCTIONS:** ANSWER ANY FOUR OUT OF FIVE QUESTIONS  
EACH QUESTION CARRIES 25 MARKS  
MARKS FOR EACH SECTION ARE IN THE RIGHT  
HAND MARGIN

THIS PAPER HAS SEVEN PAGES INCLUDING THE COVER PAGE

THE LAST PAGE CONTAINS FORMULAE AND CONSTANTS THAT MAY BE  
USEFUL IN SOME PROBLEMS

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CHIEF INVIGILATOR

## QUESTION 1

- (a) A star moving away from the earth at  $0.280c$  emits radiation that we measure to be most intense at the wavelength of 500 nm. Determine the surface temperature of this star. First find the real frequency of the emitted radiation. **(6 marks)**
- (b) Discuss the photo-electric effect. Include relevant equations. Also state whether the photoelectric effect favours the wave nature or particle nature of light. **(10 marks)**
- (c) In Compton scattering, does the photon behave like a particle or wave? Explain how you draw your conclusion. **(3 marks)**
- (d) X-rays of wavelength of  $\lambda = 0.22$  nm are scattered by a block of material and the scattered waves are observed at  $50^\circ$  to the incident beam.
- (i) Calculate the wavelength of the scattered X-rays. **(3 marks)**
  - (ii) What is the kinetic energy of the scattered electrons if they were initially at rest? **(3 marks)**

## QUESTION 2

(a) The classical model of blackbody radiation given by the Rayleigh-Jones law has two major flaws. Identify them and explain how Planck's law deals with them. **(4 marks)**

(b) Consider a single electron orbiting a stationary nucleus with charge  $+Ze$ , where  $e$  is the charge of single proton and  $Z$  is the atomic number.

(i) What is the total energy of the system using a classical model? Clearly show with the aid of a diagram how you obtain your result. **(3 marks)**

(ii) Show that the  $n^{\text{th}}$  radius of orbit of the electron is given by

$$r_n = n^2 \frac{a_0}{Z},$$

Where  $a_0 = \frac{\hbar^2}{m_e k_e e^2}$  is the Bohr radius. **(8 marks)**

(b) Use the Rydberg equation to calculate the wavelength of the radiation emitted by a hydrogen atom from  $n = 290$  to  $n = 289$  levels. **(3 marks)**

(c) Use classical mechanics to calculate the wavelength of the radiation at the  $n = 290$  orbit, where its radius of orbit is  $r = 4.01 \mu\text{m}$  and its velocity is  $U = 8.01 \times 10^3$  m/s. **(3 marks)**

(d) How do the two results from (b) and (c) compare and what does that prove? **(4 marks)**

### QUESTION 3

(a) A radioactive sample contains 3.50  $\mu\text{g}$  of pure carbon 11 ( $^{11}_6\text{C}$ ), which has a half-life of 20.4 min.

(i) What is the number of nuclei in the sample? **(3 marks)**

(ii) Find the activity of the sample in becquerels initially. **(3 marks)**

(iii) Find the activity after exactly eight hours. **(2 marks)**

(iii) What is the number of remaining nuclei after eight hours. **(2 marks)**

(b) Radium 226 decays spontaneously to produce radon 222 and an alpha particle,  $^{226}\text{Ra} \rightarrow ^{222}\text{Rn} + ^4\text{He}$ . Calculate the Q value for this reaction in MeV. Use full calculator accuracy and round at the end to 3 significant figures. What kind of a reaction is this in terms of energy? **(6 marks)**

(c) When two protons approach each other very closely they experience both the Coulomb force and the nuclear force. State which force is attractive and which is repulsive. Also sketch the potential energy diagrams for each force. **(6 marks)**

#### QUESTION 4

(a) What do you understand by the terms interference and diffraction? You can use diagrams if helpful. **(4 marks)**

(b) In a double-slit experiment, the viewing screen is  $L = 1.2$  m away. The slits are separated by a distance  $d$  of 0.02 mm. The second-order bright fringe ( $m = 2$ ) is 5 cm from the axis.

(i) What is the wavelength of the light? **(4 marks)**

(ii) What is the distance between adjacent bright fringes? **(4 marks)**

(c) A single slit of width  $d$  is placed in front of a lens of focal length  $f$  and is illuminated normally with light of wavelength  $\lambda$ . The first minima on either side of the central maximum of the diffraction pattern observed in the focal plane of the lens each is a distance  $b$  from the centre of the central maximum. What is the value of  $d$  in terms of  $f$ ,  $\lambda$  and  $b$ ? **(7 marks)**

(d) An oil film is 400 nm thick with a refractive index of 1.6 floats on water of refractive index 1.33 and is illuminated by a continuous spectrum of light from the sun. Some colours appear to be very strong compared to others when viewing the film. Determine which visible wavelengths are suppressed by the film. Above the film is air of refractive index 1. **(6 marks)**

### QUESTION 5

(a) A microscope eyepiece has an aperture diameter of 0.8 cm. A neon laser at 633 nm is used to view the object

- (i) What is the limiting angle of resolution  $\theta_{\min}$ . **(2 marks)**
- (ii) If oil of refractive index 1.6 is used to fill the space between the objective lens and the object, what is the limiting angle of resolution? **(3 marks)**
- (iii) If violet light at 400 nm is used to view the object what is the limiting angle of resolution. **(2 marks)**
- (iv) From your results in (i), (ii) and (iii) comment on the effect on  $\theta_{\min}$  when using a higher refractive index medium and when using a shorter wavelength. **(2 marks)**

(b) Determine the minimum distance between two point sources that the human eye can distinguish at the near point (25 cm), assuming a pupil diameter of 2 mm, and a wavelength of 589 nm. **(5 marks)**

(c) Discuss the principle of laser operation with the aid of diagrams. **(8 marks)**

(d) Briefly discuss why sunrise and sunset tend to be red. **(3 marks)**

## SOME INFORMATION THAT MAY BE USEFUL IN SOME PROBLEMS

$$\sigma = 5.6696 \times 10^{-8} \text{ W}/(\text{m}^2\text{K}^2)^3$$

$$\text{Boltzmann's constant, } k_B = 1.3801 \times 10^{-23} \text{ J/K}$$

$$\text{Bohr magneton, } \mu_B = 9.27 \times 10^{-24} \text{ J/T}$$

$$\text{Speed of light in vacuum, } c = 2.99792458 \times 10^8 \text{ m/s}$$

$$\text{Planck's constant, } h = 6.626075 \times 10^{-34} \text{ Js}$$

$$\hbar = 1.054572 \times 10^{-34}$$

$$hc = 1.986447 \times 10^{-25}$$

$$2\pi\hbar c^2 = 3.741859 \times 10^{-15}$$

$$\text{mass of an electron, } m_e = 9.1093897 \times 10^{-31} \text{ kg}$$

$$\text{mass of a proton, } m_p = 1.672623 \times 10^{-27} \text{ kg}$$

$$\text{mass of a neutron, } m_n = 1.6749286 \times 10^{-27} \text{ kg}$$

$$\text{Coulomb constant, } k_e = 8.987551787 \times 10^9 \text{ Nm}^2/\text{C}^2$$

$$\text{electron charge, } e = 1.60217733 \times 10^{-19} \text{ C}$$

$$1 \text{ atomic mass unit} = 1 \text{ amu} = 1 u = 1.6605402 \times 10^{-27} \text{ kg} = 931.494 \text{ MeV}$$

$$1 \text{ eV} = 1.60217733 \times 10^{-19} \text{ J}$$

$$T_{1/2}(^{14}\text{C}) = 5730 \text{ years}$$

$$\frac{N(^{14}\text{C})}{N(^{12}\text{C})} = 1.3 \times 10^{-12}$$

$$\text{Helium } (^4\text{He}) \text{ nuclear mass} = 4.002602 \text{ u}$$

$$\text{Radon } (^{222}\text{Rn}) \text{ nuclear mass} = 222.017571 \text{ u}$$

$$\text{Radium } (^{226}\text{Ra}) \text{ nuclear mass} = 226.025402 \text{ u}$$

$$\lambda_{\max} = \frac{hc}{4.965kT}$$

$$\theta_{\min} = 1.22\lambda D$$

$$I = \frac{2\pi\hbar c^2}{\lambda^5 \left( e^{\frac{hc}{\lambda kT}} - 1 \right)}$$

$$\int \cos^2 u \, du = \frac{u}{2} + \frac{1}{4} \sin 2u$$