

UNIVERSITY OF SWAZILAND

FACULTY OF SCIENCE

DEPARTMENT OF PHYSICS

MAIN EXAMINATION 2006/2007

TITLE OF THE PAPER: NUCLEAR PHYSICS

COURSE NUMBER : P442

TIME ALLOWED : THREE HOURS

INSTRUCTIONS:

- ANSWER ANY **FOUR** OUT OF **FIVE** QUESTIONS.
- EACH QUESTION CARRIES **25** MARKS.
- MARKS FOR DIFFERENT SECTIONS ARE SHOWN IN THE RIGHT-HAND MARGIN.
- USE THE INFORMATION GIVEN IN THE ATTACHED **APPENDIX** WHEN NECESSARY.

THIS PAPER HAS **SIX** PAGES, INCLUDING THIS PAGE.

DO NOT OPEN THE PAPER UNTIL THE INVIGILATOR HAS GIVEN PERMISSION.

Q.1.

(A) (i) Define mass defect , nuclear binding energy and separation energy. [6]

(ii) Compute mass defect, nuclear binding energy and neutron separation energy for ${}^{20}_9F$. [6]

Given: Atomic mass of ${}^{20}_9F = 19.999981$ (u) .

${}^{19}_9F = 18.99840$ (u).

(B) (i) Define radius of the nuclei. [2]

(ii) If we assume the charges to be discrete electrostatic energy for a nucleus of radius R and charge Ze is given by $\frac{3Z(Z-1)e^2}{20\pi\epsilon_0 R}$.

(a) Show that for a mirror nuclei, the Coulomb energy difference is given by [2]

$$|\Delta E| = \frac{6Ze^2}{20\pi\epsilon_0 R} \text{ where } Z \text{ refers to the nuclei of lower charge.}$$

(b) Use this formula to estimate R in the case of ${}^{16}_7N$ (atomic mass=16.0061(u))

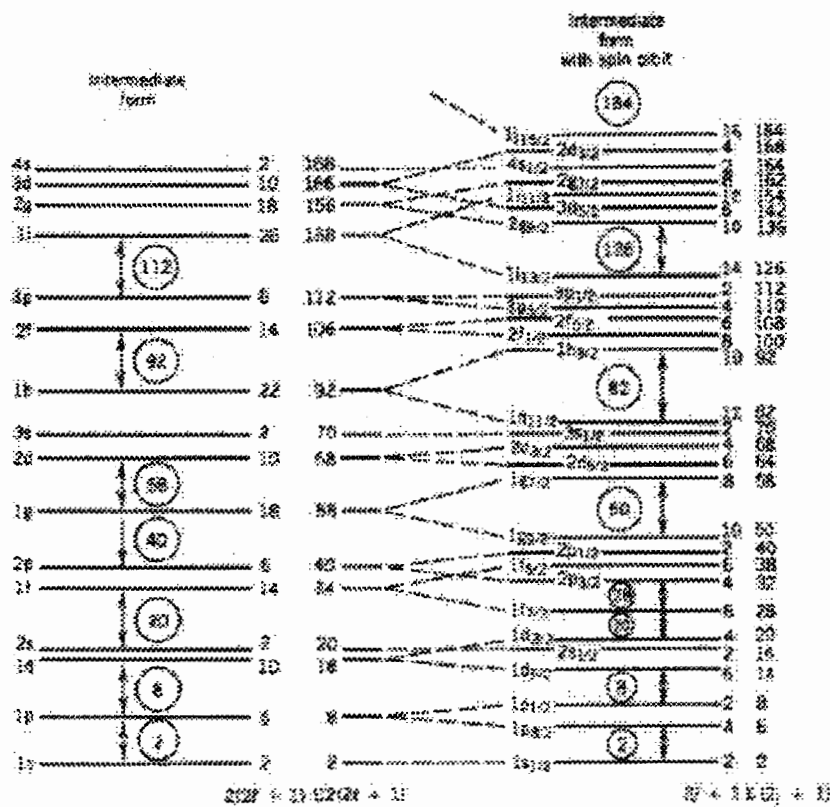
and ${}^{16}_8O$ (atomic mass=15.994915(u)). [3]

(C) Describe the processes:

(i) Nuclear Fission and Nuclear Fusion. [3]

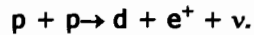
(ii) Photoelectric effect and Auger process. [3]

Q.2. (A) Use the given shell model level scheme to determine the angular momentum and parity for the ground states of ${}^{17}_8O$ and ${}^{69}_{31}Ga$ without spin and with spin. [10]
What do you understand by the term " Magic Numbers " ?



Note: Refer to a better reproduction of the figure provided at the examination hall .

(B) Defining the Q value as $(m_i - m_f) c^2$, compute the range of neutrino energies (minimum and maximum) in the solar fusion reaction: [5]



Assume the initial protons to have negligible kinetic energies.

Here m_i = initial masses and m_f = final masses.

symbols: p=proton. d = deuteron. e^+ =positron, and ν = neutrino.

Given: Assume the neutrino mass to be zero.

Nuclear mass of deuteron = 1875.611 MeV.

(C)

(i) Explain why two types of selection rules (the Fermi and GT) exist in β -decay. [2]

(ii) Among the possible interactions :

S(scalar),V(vector),T(Tensor),A(axial vector) and P(pseudo-scalar);

name the interactions which are the major contributors in Fermi type and GT-type β - transitions. [2]

(iii) Describe the significant processes through which the γ -rays in the energy range greater than 5 MeV primarily interact with matter. [6]

Q.3. (A) Semi-empirical mass formula is given by

$$m(Z, A) = Zm_p + (A - Z)m_n - a_v A + a_s A^{2/3} + a_c Z^2 A^{-1/3} + a_a \frac{(A - 2Z)^2}{A} \pm \delta \left[\begin{array}{l} \text{odd - odd} \\ \text{even - even} \end{array} \right]$$

where $m(Z, A)$ corresponds to nuclear mass.

(i) Explain the origin of the various terms. [6]

(ii) Assume following values of the parameters in the Semi-empirical mass formula:

$$a_v = 14.1 \text{ MeV}, \quad a_s = 13.0 \text{ MeV}, \quad a_c = 0.595 \text{ MeV} \text{ and}$$

$$a_a = 19.0 \text{ MeV}$$

Neglect the pairing energy contribution.

Use the semi-empirical mass formula to calculate nuclear binding energy and

neutron separation energy for ${}^{20}_9\text{F}$. [8]

(B) The α -decay of ${}^{253}_{99}\text{Es}$ ($I = 7/2, \pi = +$) leads to a sequence of

negative-parity states in ${}^{249}_{97}\text{Bk}$ with spin

$$3/2, 5/2, 7/2, 9/2, 11/2, 13/2.$$

Assume that ground state of ${}^{249}_{97}\text{Bk}$ has spin $3/2^-$ and all other states are excited states according to the order given in the spin assignments.

The excited states decay by γ - transitions.

(a) For each state find the permitted values of ℓ_α . [6]

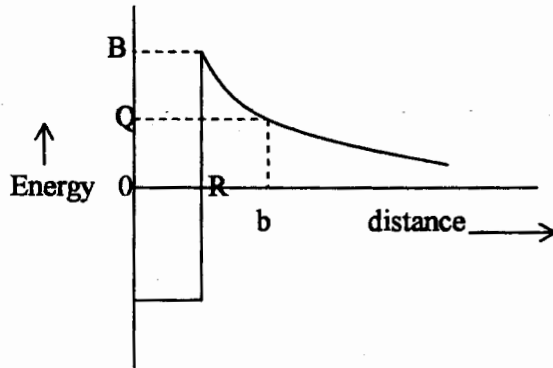
(b) Draw an energy level diagram and their dominant multi-pole assignments. [5]

Note: Most probable transitions are expected to be up to E2 and M2.

Q. 4. (A) ${}^{137}_{55}\text{Cs}$ with its ground state $7/2^+$ decays by beta-decay to $11/2^-$ and $3/2^+$ states of ${}^{137}_{56}\text{Ba}$. What types of transitions are expected in each case? [4]

(B) The alpha-decay Q-value of $^{238}_{92}\text{U}$ is 4.268 MeV.

- (i) Calculate the height B of the Coulomb barrier between the alpha-particle and the daughter nucleus, assuming that the nuclear potential has a sharp edge at a radius of $1.4A^{1/3}$ fm. [4]
- (ii) Calculate the distance b beyond which the alpha-particle kinetic energy is positive. [5]



(C) $^{22}_{11}\text{Na}$ atom has mass of 20487.686 MeV and it decays, with half life of 2.6 years, from its 3^+ ground state by positron emission to ground state of Ne and by electron capture to the 2^+ first excited state of $^{22}_{10}\text{Ne}$ of atomic mass 20484.844 MeV,

- (a) Draw the energy level diagram. [2]
- (b) Write down expressions for Q-values for the two types of decay, [2]
- (c) Calculate the Q-values for the two types of decay in MeV. [4]
- (d) What types of transitions are expected in each case? [4]

Q.5. (A) (i) A nuclear excited state decays by an E2 transition to the $3/2^+$ ground state. List the possible spin-parity assignments of the excited state. [3]

(ii) List all the possible multi-polarities for the following γ -transitions, indicating in each case, which is likely to be the most intense. [6]

(a) $3^- \rightarrow 2^+$, (b) $5/2^+ \rightarrow 9/2^+$.

(iii) Explain why transition from 0^+ to 0^+ will not allow any γ -radiation. [4]

(B) An even-Z, even-N nucleus has the following sequence of levels above its 0^+ ground state:

$2^+(89\text{keV}), 4^+(288\text{keV}), 6^+(585\text{keV}), 0^+(1050\text{keV}), 2^+(1129\text{keV})$

Draw an energy level diagram and show all reasonably probable γ transitions and their dominant multi-pole assignments. [10]

(C) Supply the missing component(s) in the following processes: [2]

(i) $^{40}_{19}\text{K} \rightarrow \nu +$

(ii) $^{40}_{19}\text{K} \rightarrow \bar{\nu} +$

END OF EXAMINATION

Appendix

Selection Rules:

(A) β -decay:

Type of Transition		ΔI	Parity Change
Allowed	Fermi	0	No
	GT	± 1 or 0 (except $0 \rightarrow 0$)	No
1 st Forbidden	Fermi	$\pm 1, 0$ (except $0 \rightarrow 0$)	Yes
	GT	$\pm 2, \pm 1$, or 0 (except $0 \rightarrow 0$; $1/2 \rightarrow 1/2$; $0 \rightarrow 1$)	Yes
2 nd Forbidden	Fermi	± 2	No
	GT	± 3	No

(B) γ - decay:

	E1	E2	E3	E4
$\Delta\pi$	Yes	No	Yes	No
$ \Delta J \leq$	1	2	3	4
	M1	M2	M3	M4
$\Delta\pi$	No	Yes	No	Yes
$ \Delta J \leq$	1	2	3	4

(C) Useful Information

PHYSICAL CONSTANTS ¹ AND DERIVED QUANTITIES

Speed of light $c = 2.99792458 \times 10^8 \text{ m s}^{-1} \sim 3.00 \times 10^{23} \text{ fm s}^{-1}$

Avogadro's number $N_A = 6.02214199(47) \times 10^{26}$ molecules per kg-mole

Planck's constant $h = 6.62606876(52) \times 10^{-34} \text{ J s}$

$\hbar = 1.054571596(82) \times 10^{-34} \text{ J s} = 0.65821 \times 10^{-21} \text{ MeV s}$

$\hbar^2 = 41.802 \text{ u MeV fm}^2$

$\hbar c = 197.327 \text{ MeV fm}$

Elementary charge $e = 1.602176462(63) \times 10^{-19} \text{ C}$

$e^2/4\pi\epsilon_0 = 1.4400 \text{ MeV fm}$

Fine structure constant $\alpha = \frac{e^2}{4\pi\epsilon_0\hbar c} = 1/137.036$

Boltzmann constant $k = 1.3806503(24) \times 10^{-23} \text{ JK}^{-1} = 0.8617 \times 10^{-4} \text{ eV K}^{-1}$

MASSES AND ENERGIES

Atomic mass unit m_u or $u = 1.66053873(13) \times 10^{-27} \text{ kg}$

$m_u c^2 = 931.494 \text{ MeV}$

Electron $m_e = 9.10938188(72) \times 10^{-31} \text{ kg}$

$m_e/m_u = 5.486 \times 10^{-4} = 1/1823$

$m_e c^2 = 0.510998902(21) \text{ MeV}$

Proton	m_p	$= 1.67262158(13) \times 10^{-27} \text{ kg}$
	m_p / m_u	$= 1.00727647$
	$m_p c^2$	$= 938.272 \text{ MeV}$
Hydrogen atom	m_H	$= 1.673533 \times 10^{-27} \text{ kg}$
	m_H / m_u	$= 1.007825$
	$m_H c^2$	$= 938.783 \text{ MeV}$
Neutron	m_n	$= 1.67492716(13) \times 10^{-27} \text{ kg}$
	m_n / m_u	$= 1.00866491578(55)$
	$m_n c^2$	$= 939.565 \text{ MeV}$
Alpha particle	m_α	$= 6.644656 \times 10^{-27} \text{ kg}$
	m_α / m_u	$= 4.001506175$
	$m_\alpha c^2$	$= 3727.379 \text{ MeV}$

CONVERSION FACTORS

Fermi	$1 \text{ fm} = 10^{-15} \text{ m}$
	$1 \text{ eV} = 1.6022 \times 10^{-19} \text{ J}$
Million electron volts	$1 \text{ MeV} = 1.602176 \times 10^{-13} \text{ J}$
	$1 \text{ MeV}/c^2 = 1.783 \times 10^{-30} \text{ kg}$
Cross section (barn)	$1 \text{ b} = 10^{-28} \text{ m}^2$
Year	$1 \text{ y} = 3.1536 \times 10^7 \text{ s}$

USEFUL FORMULAE

$$t_{\frac{1}{2}} = \frac{\ln 2}{\lambda} = \tau \ln 2 \quad \text{where } t_{\frac{1}{2}} = \text{half life, } \lambda = \text{decay constant and } \tau = \text{mean life.}$$

Energy width of a state of lifetime τ :

$$\Gamma = 6.58212 \times 10^{-22} / \tau(\text{s}) \text{ MeV}$$

Non-relativistic speed of mass m with energy E :

$$v = 1.389 \times 10^7 [(E(\text{MeV}) / m(u))]^{1/2} \text{ ms}^{-1}$$

Non-relativistic wave number of mass m with energy E :

$$k = 2\pi/\lambda = 0.21874 [m(u) \times E(\text{MeV})]^{1/2} \text{ fm}^{-1}$$

Wave number for a photon of energy E :

$$k = 2\pi/\lambda = E / \hbar c = E(\text{MeV}) / 197.327 \text{ fm}^{-1}$$

¹ Source: 1998 CODATA Recommended Values. Uncertainties are given in parentheses.