

UNIVERSITY OF SWAZILAND

FACULTY OF SCIENCE

DEPARTMENT OF PHYSICS

MAIN EXAMINATION : 2009/2010
TITLE OF PAPER : THERMODYNAMICS
COURSE NUMBER : P242
TIME ALLOWED : THREE HOURS
INSTRUCTIONS : ANSWER ANY FOUR OUT OF FIVE QUESTIONS

EACH QUESTION CARRIES 25 MARKS

MARKS FOR DIFFERENT SECTIONS ARE SHOWN IN THE RIGHT-HAND MARGIN.

THIS PAPER HAS 7 PAGES, INCLUDING THIS PAGE.

DO NOT OPEN THE PAPER UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR.

INFORMATION

Universal gas constant, R	$= 8.31 \text{ J mol}^{-1}\text{K}^{-1}$
Specific heat of water, c_w	$= 4186 \text{ J kg}^{-1}\text{K}^{-1}$
Density of water, ρ	$= 10^3 \text{ kg.m}^{-3}$
Latent heat of fusion for ice, L_f	$= 3.33 \times 10^5 \text{ Jkg}^{-1}$
Specific heat of iron, c_i	$= 448 \text{ J kg}^{-1}\text{K}^{-1}$
Avogadro's number, N_A	$= 6.02 \times 10^{23} \text{ molecules.mol}^{-1}$
Boltzmann constant, k_B	$= 1.38 \times 10^{-23} \text{ JK}^{-1}$
Stefan-Boltzmann constant, σ	$= 5.67 \times 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$
1 atmosphere	$= 1.013 \times 10^5 \text{ Nm}^{-2}$
Thermal conductivity of gold, k_{gold}	$= 314 \text{ Wm}^{-1}\text{K}^{-1}$
Thermal conductivity of silver, k_{silver}	$= 427 \text{ Wm}^{-1}\text{K}^{-1}$

QUESTION 1

- (a) Show, mathematically, that for a given mass of an ideal gas and for an adiabatic process,

$$p = kV^{-\gamma}$$

where k and γ are constants. The other symbols have the usual meaning. (11 marks)

- (b) Two moles of an ideal gas ($\gamma = 1.40$) expands slowly and adiabatically from a pressure of 5.00 atm and a volume of 12.0 liters to a final volume of 30.0 liters.

(i) What is the final pressure of the gas? (3 marks)

(ii) What are the initial and final temperatures? (4 marks)

- (c) During the compression stroke of a certain gasoline engine, the pressure increases from 1.00 atm to 20.0 atm. Assuming that the process is adiabatic and reversible and the gas is ideal with $\gamma = 1.40$,

(i) By what factor does the volume change and (3 marks)

(ii) By what factor does the temperature change? (3 marks)

(iii) What is the compression ratio? (1 mark)

QUESTION 2

- (a) Consider the van der Waals equation below:

$$\left(p + \frac{a}{v^2}\right)(v - b) = RT$$

- (i) Expand this equation in virial form and show that

$$pv + \frac{a}{v} = \frac{RT}{\left(1 - \frac{b}{v}\right)} \quad (4 \text{ marks})$$

- (ii) Determine the first three virial constants. (7 marks)

- (b) The constant b that appears in van der Waals' equation of state for oxygen is measured to be $31.8 \text{ cm}^3/\text{mol}$. Assuming a spherical shape, estimate the diameter of the oxygen molecule. (6 marks)

- (c) The molecular speed distribution law for a sample of gas containing N molecules is

$$N(v) = 4\pi N \left(\frac{m}{2\pi k_B T}\right)^{\frac{3}{2}} v^2 \exp\left(-\frac{mv^2}{2k_B T}\right)$$

Show that the average speed of a gas molecule is given by

$$\bar{v} = 1.59 \sqrt{\frac{k_B T}{m}}$$

Note:

$$\int_0^{\infty} v^3 \exp(-\lambda v^2) dv = \frac{1}{2\lambda^2}, \text{ where the symbols have the usual meaning.} \quad (8 \text{ marks})$$

QUESTION 3

- (a) State two factors that affect the efficiency of automobile engines? (2 marks)
- (b) In practical heat engines such as the automobile engine, which of the following do we have more control of: (i) the temperature of the hot reservoir or (ii) the temperature of the cold reservoir? Explain. (4 marks)
- (c) An ideal heat pump absorbs heat Q_C from a cold reservoir and rejects heat Q_H to a hot reservoir. With the aid of Fig. 1, derive the expression below, which represents the amount of work required to run the pump: (13 marks)
- $$|W| = \frac{T_H - T_C}{T_C} |Q_C|$$
- (d) One of the most efficient engines ever built has an efficiency of 42% and operates between 430°C and 1870°C .
- (i) What is its maximum theoretical efficiency? (3 marks)
- (ii) How much power does the engine deliver if it absorbs $1.4 \times 10^5 \text{ J}$ of the thermal energy each second? (3 marks)

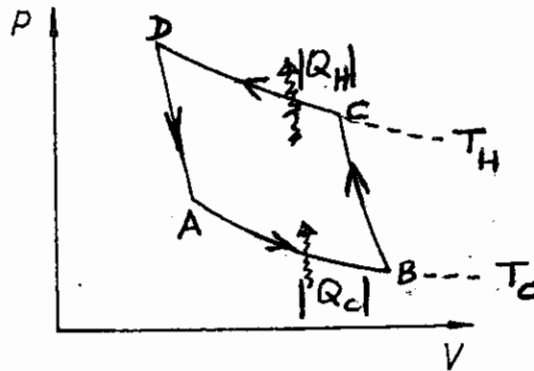


Fig. 1

QUESTION 4

- (a) Fig. 2 shows a schematic diagram of a solar water heating panel system. Explain how the system works. Comment on the properties of the materials used to make the panel, with the aid of a detailed diagram (of the panel). Label the diagram. (12 marks)
- (b) The surface of the Sun has a temperature of about 5800 K. Taking the radius of the Sun to be 6.96×10^8 m, calculate the total energy radiated by the Sun each day. (Assume $e = 1$). (4 marks)
- (c) A bar of gold is in thermal contact with a bar of silver of the same length and area. One end of the compound bar (double slab) is maintained at 80.0°C while the opposite end is at 30.0°C .

Find the temperature at the junction of the two metals when the heat flow reaches steady state. (9 marks)

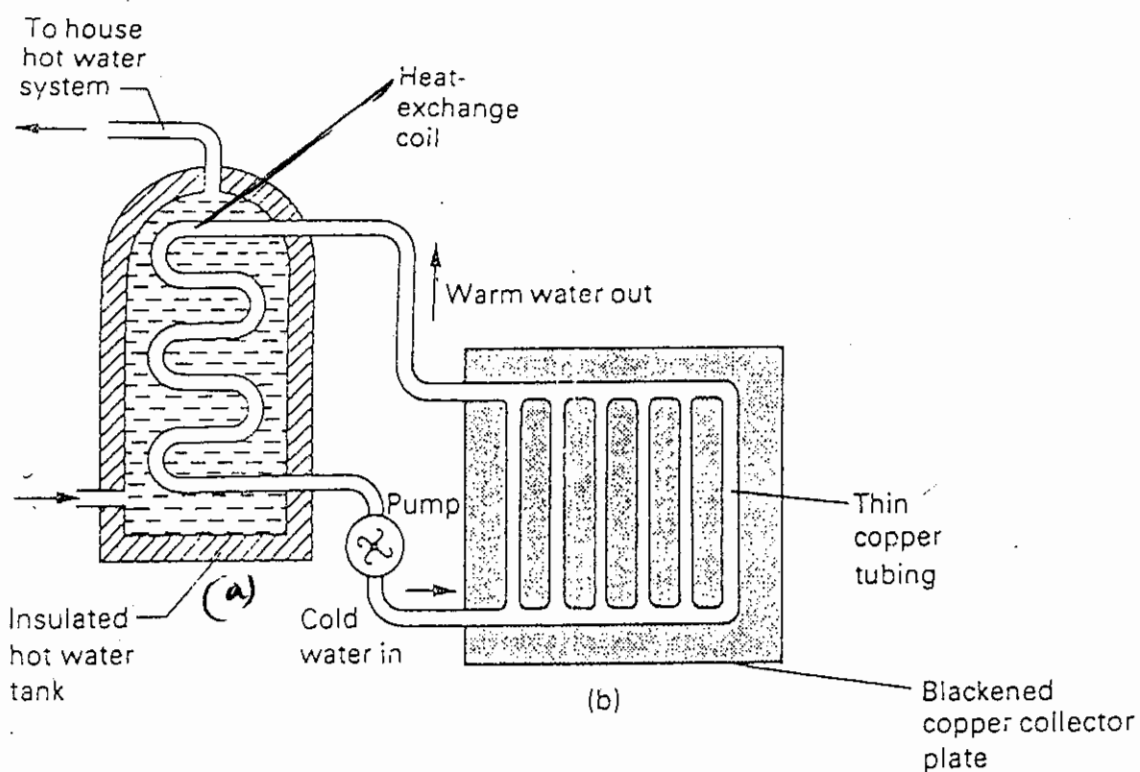


Fig. 2

QUESTION 5

- (a) State the Clausius theorem in thermodynamics. (2 marks)
- (b) Discuss two common examples of natural processes that involve an increase in entropy. Be sure to account for all parts of each system under consideration. (4 marks)
- (c) A thermodynamic process occurs in which the entropy of a system changes by -8.0 J/K . According to the second law of thermodynamics, what can you conclude about the entropy change of the environment? (2 marks)
- (d) A 1.5 kg iron horseshoe initially at 600°C is dropped into a bucket containing 20 kg of water at 25°C .
- (i) What is the final temperature? (Neglect the heat capacity of the container) (4 marks)
- (ii) Find the change in entropy of the water, iron and universe (7 marks)
- (e) Using an ideal Carnot refrigerator, how much work is required to change 0.50 kg of tap water at 10°C into ice at -20°C ? Assume that the freezer compartment is held at -20°C and the refrigerator exhausts heat into a room at 20°C . (6 marks)