## UNIVERSITY OF SWAZILAND

FACULTY OF SCIENCE AND ENGINEERING DEPARTMENT OF PHYSICS

MAIN EXAMINATION 2015/16

| TITLE OF PAPER: | DIGITAL ELECTRONICS |
| :--- | :--- |
| COURSE NUMBER: | P411 |
| TIME ALLOWED: | 3 HOURS |
| INSTRUCTIONS: | ANSWER ANY FOUR OUT OF FIVE QUESTIONS. |
|  | EACH QUESTION CARRIES 25 MARKS. |
|  | MARKS FOR DIFFERENT SECTIONS ARE SHOWN |
|  | ENCLOSED IN SQUARE BRACKETS. |

THIS PAPER HAS SEVEN (7) PAGES INCLUDING THIS PAGE.
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## QUESTION 1

a) Convert the hexadecimal number 2B6D.5AB $\mathrm{AB}_{16}$ to its equivalent decimal number.
b) Find the equivalent octal number for the BCD coded number $101011100101_{B C D}$. [3]
c) Subtract ( 1110.011$)_{2}$ from $(11011.11)_{2}$ using basic rules of binary subtraction.
d) i) Find the decimal equivalent of the following binary number expressed in the 2 's complement format: $00001110_{2}$
ii) Two possible binary representations of $(-1)_{10}$ are $(10000001)_{2}$ and (11111111) $)_{2}$.

One of them belongs to the sign-bit magnitude format and the other to the 2 's complement format. Identify, which is which.
e) Consider the two signals simultaneously entering the XOR gate in Figure 1. Make a table listing the binary outputs corresponding to the input points labelled $a, b, \ldots l$

## lkjihgiedoba



Figure 1

## QUESTION 2

a) Draw logic implementation of an inverter using (i) two-input NAND, (ii) two-input NOR, (iii) two-input EX-OR and (iv) two-input EX-NOR.
b) Explain what a 'wired-AND' is, using an example.
c) State the De Morgan's Theorem.
d) Simplify the following expressions using Boolean algebra:

$$
\begin{align*}
& \text { i) } F=(X+\bar{Y}+\bar{X} \cdot Y) \cdot \bar{Z}  \tag{3}\\
& \text { ii) } F=\bar{X} \cdot Y \cdot(X+\bar{Y}+\bar{X} \cdot Y)(X+\bar{Y}) \tag{3}
\end{align*}
$$

e) Convert the following logical expression into canonical POS or maxterm form: $F=(A+B)(A+C)(B+C)$

## QUESTION 3

a) Map the function having four variables in a K-map and give the simplified Boolean expression. The function is $\mathrm{F}(\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D})=\Sigma \mathrm{m}(2,6,10,14)$.
b) Using the Karnaugh Map, simplify the Boolean function given by

$$
\begin{equation*}
F(A, B, C)=(A+B+C)(\overline{\mathrm{A}}+\mathrm{B}+\overline{\mathrm{C}})(\mathrm{A}+\overline{\mathrm{B}}+\mathrm{C}) \tag{6}
\end{equation*}
$$

for the don't care condition expressed as $(\bar{A}+\bar{B})(\bar{A}+B+C)$.
c) For the half-adder circuit of Figure 2(a), the inputs applied at A and B are as shown in Figure 2(b). Plot the corresponding SUM and CARRY outputs on the same scale. [4]

(a)

(b)

Figure 2
d) Write down Boolean expressions representing the SUM and CARRY outputs in terms of three input binary variables to be added. Design a suitable combinational circuit to hardware-implement the design using NAND gates only.

## QUESTION 4

a) How do you characterize or define a combinational circuit? How does it differ from a sequential circuit? Give two examples each of combinational and sequential logic devices.
b) Design and draw up the truth table for a four-line to two-line priority encoder with active HIGH inputs and outputs, with priority assigned to the higher-order data input line.
c) Figure 3 illustrates a clocked RS flip-flop pulse-train with the set (S) and reset (R) inputs drawn above and below the pulse-train, respectively. For each of the eight clock pulses ( $a$ to $h$ ), list the binary output $Q$ of the flip-flop.


Figure 3
c) For a logic circuit of a four-NAND gate JK flip flop as in Figure 4. Copy and complete Tablel with the various signals at the inputs and outputs of the clocked JK flip flop.


Figure 4

| Inputs |  | Outputs before the <br> clock pulse |  | Outputs after the <br> clock pulse |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $J$ | $K$ | $Q$ | $\bar{Q}$ | $Q$ | $\bar{Q}$ |
| 0 | 0 | 0 | 1 |  |  |
| 0 | 0 | 1 | 0 |  |  |
| 0 | 1 | 0 | 1 |  |  |
| 0 | 1 | 1 | 0 |  |  |
| 1 | 0 | 0 | 1 |  |  |
| 1 | 0 | 1 | 0 |  |  |
| 1 | 1 | 0 | 1 |  |  |
| 1 | 1 | 1 | 0 |  |  |

Table 1

## QUESTION 5

a) Determine the number of flip-flops required to construct a MOD-10:
(i) Ring counter;
(ii) Johnson counter.

Also write the count sequences in the two cases.
b) Give two uses of shift registers.
c) Determine the resolution of a 12 -bit $\mathrm{A} / \mathrm{D}$ converter having a full-scale analogue input voltage of 5 V .
d) Describe the functions of the following elements of a microprocessor unit:
(i) Data register (DR);
(ii) Address register (AR); [2]
(iii) Arithmetic logic unit (ALU); [2]
(iv) Stack Pointer (SP).

