

**UNIVERSITY OF ESWATINI**  
**FACULTY OF SOCIAL SCIENCES**  
**DEPARTMENT OF ECONOMICS**  
**MAIN EXAMINATION 2018/2019**

**TITLE OF PAPER : INTRODUCTION TO ECONOMETRICS II**  
**COURSE CODE : ECO 308**  
**TIME ALLOWED : TWO (2) HOURS**

**INSTRUCTIONS :**

- 1. ANSWER QUESTION ONE (1) AND ANY OTHER TWO (2) IN THIS PAPER.**
- 2. ONLY SCIENTIFIC NON-PROGRAMMABLE CALCULATORS ARE ALLOWED.**
- 3. ROUND UP YOUR FINAL ANSWERS TO THREE (3) DECIMAL PLACES.**
- 4. IF IT IS NOT SPECIFIED, USE  $\alpha = 0.05$  FOR STATISTICAL TESTS.**
- 5. THE REQUIRED PROBABILITY TABLES ARE ATTACHED AT THE BACK OF QUESTION PAPER.**

**THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR**

**QUESTION 1 (Compulsory)****[40 MARKS]**

- a) Briefly outline the consequences of heteroscedasticity [6 Marks]
- b) Outline the steps of detecting heteroscedasticity when using the Park Test. [8 Marks]
- c) Consider a situation where the researcher has information that the following model has heteroscedastic error variances :  $y_i = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + u_i$   
If the variance of the errors is known to be  $Var(u_i|x_i) = \sigma^2 x_2^2$ , show how this model can be transformed to make the error variances homoscedastic. [10 Marks]
- d) Briefly discuss two (2) ways in which you can remedy the problem of multicollinearity in a model. [5 Marks]
- e) The Variance Inflating Factor (*VIF*) is utilised to detect the presence of multicollinearity, how is the *VIF* computed, and what is the logic of using it in detecting multicollinearity. [6 Marks]
- f) Outline and discuss the weaknesses of the Linear Probability Model (*LPM*). [5 Marks]

**ANSWER ANY TWO QUESTIONS FROM THE FOLLOWING QUESTIONS****QUESTION 2****[30 MARKS]**

- a) Explain how the Linear Probability Model (*LPM*) differs from a Probit model? [7 Marks]
- b) The following is a Logit model that was estimated to determine car ownership as a function of the logarithm of income. Car ownership was a binary variable where  $Y = 1$  if a household owned a car, and zero otherwise.

$$\hat{L}_i = -2.77231 + 0.347582 \ln Income$$

$$(0.82756) \quad (0.0858)$$

$$n = 2,820$$

- i) Interpret the estimated logit model. [8 Marks]
- ii) From the estimated logit model, how would you obtain the expression for the probability of car ownership? [5 Marks]

- iii) What is the probability that a household with an income of 20,000 will own a car? [5 Marks]
- iv) What is the rate of change of probability at the income level 20,000? [5 Marks]

**QUESTION 3****[30 MARKS]**

- a) Distinguish between fixed effects and random effects panel data models. [6 Marks]
- b) Give three (3) reasons where you would choose one model over the other between fixed effects model and random effects model. [6 Marks]
- c) Caution should be exercised when using the fixed effects least squares dummy variable model. Discuss three (3) of these problems. [6 Marks]
- d) Suppose you have model for the three airline companies in a country stated as:

$$C_{it} = \beta_{0i} + \beta_1 Q_{it} + \beta_2 PF_{it} + \beta_3 LF_{it} + u_{it}$$

$$i = 1,2,3 \quad t = 1,2, \dots, 20$$

Where  $C$  is Total Cost in \$1,000,  $Q$  is output in revenue passenger miles, and  $PF$  is the fuel price.

- i) Setup a fixed effects least-squares dummy variable model, and explain the coefficients that explain the fixed effects. [8 Marks]
- ii) What difficulty is likely to be encountered if the model would be allowed to capture time effects? [4 Marks]

**QUESTION 4****[30 MARKS]**

Multiple Linear regression models may suffer from functional form misspecification, if they don't properly account for the relationship between the dependent and independent variables.

If, say the true wage model is:

$$\ln Wage = \beta_0 + \beta_1 educ + \beta_2 exper + \beta_3 exper^2 + u_i$$

$$\ln Wage = \beta_0 + \beta_1 educ + \beta_2 exper + \beta_3 exper^2 + u_i$$

However for some reason, the researcher estimates the following model:

$$\ln Wage = \beta_0 + \beta_1 educ + \beta_2 exper + u_i$$

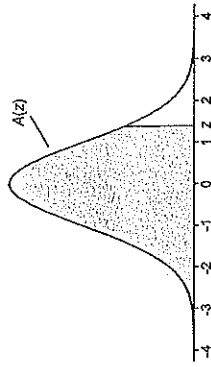
- a) What problems will the researcher encounter if they try to measure returns to education using the misspecified model? [10 marks]
- b) What is the problem of estimating the returns to experience using the misspecified model? [10 Marks]
- c) Outline the Ramsey RESET Test for Model Misspecification. [10 Marks]

TABLE A.1

Cumulative Standardized Normal Distribution

$A(z)$  is the integral of the standardized normal distribution from  $-\infty$  to  $z$  (in other words, the area under the curve to the left of  $z$ ). It gives the probability of a normal random variable not being more than  $z$  standard deviations above its mean. Values of  $z$  of particular importance:

$z$	$A(z)$
1.645	0.9500
1.960	0.9750
2.326	0.9900
2.576	0.9950
3.090	0.9990
3.291	0.9995



0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6444	0.6481	0.6519
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7421	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8483	0.8505	0.8526	0.8547	0.8567	0.8587	0.8606
1.1	0.8625	0.8643	0.8661	0.8678	0.8694	0.8710	0.8726	0.8741	0.8756	0.8770
1.2	0.8786	0.8801	0.8816	0.8831	0.8846	0.8860	0.8874	0.8888	0.8902	0.8915
1.3	0.8928	0.8941	0.8954	0.8967	0.8979	0.8991	0.8999	0.9011	0.9022	0.9031
1.4	0.9042	0.9052	0.9061	0.9070	0.9078	0.9086	0.9093	0.9099	0.9105	0.9111
1.5	0.9118	0.9124	0.9129	0.9134	0.9138	0.9142	0.9146	0.9149	0.9152	0.9155
1.6	0.9158	0.9161	0.9164	0.9167	0.9169	0.9171	0.9173	0.9175	0.9176	0.9177
1.7	0.9178	0.9179	0.9180	0.9181	0.9182	0.9183	0.9184	0.9185	0.9186	0.9187
1.8	0.9187	0.9188	0.9188	0.9189	0.9189	0.9190	0.9190	0.9191	0.9191	0.9192
1.9	0.9192	0.9192	0.9193	0.9193	0.9193	0.9194	0.9194	0.9194	0.9194	0.9195
2.0	0.9195	0.9195	0.9195	0.9196	0.9196	0.9196	0.9196	0.9197	0.9197	0.9197
2.1	0.9197	0.9197	0.9197	0.9198	0.9198	0.9198	0.9198	0.9198	0.9199	0.9199
2.2	0.9199	0.9199	0.9199	0.9199	0.9200	0.9200	0.9200	0.9200	0.9200	0.9200
2.3	0.9200	0.9200	0.9200	0.9200	0.9201	0.9201	0.9201	0.9201	0.9201	0.9201
2.4	0.9201	0.9201	0.9201	0.9201	0.9202	0.9202	0.9202	0.9202	0.9202	0.9202
2.5	0.9202	0.9202	0.9202	0.9202	0.9203	0.9203	0.9203	0.9203	0.9203	0.9203
2.6	0.9203	0.9203	0.9203	0.9203	0.9204	0.9204	0.9204	0.9204	0.9204	0.9204
2.7	0.9204	0.9204	0.9204	0.9204	0.9205	0.9205	0.9205	0.9205	0.9205	0.9205
2.8	0.9205	0.9205	0.9205	0.9205	0.9206	0.9206	0.9206	0.9206	0.9206	0.9206
2.9	0.9206	0.9206	0.9206	0.9206	0.9207	0.9207	0.9207	0.9207	0.9207	0.9207
3.0	0.9207	0.9207	0.9207	0.9207	0.9208	0.9208	0.9208	0.9208	0.9208	0.9208
3.1	0.9208	0.9208	0.9208	0.9208	0.9209	0.9209	0.9209	0.9209	0.9209	0.9209
3.2	0.9209	0.9209	0.9209	0.9209	0.9210	0.9210	0.9210	0.9210	0.9210	0.9210
3.3	0.9210	0.9210	0.9210	0.9210	0.9211	0.9211	0.9211	0.9211	0.9211	0.9211
3.4	0.9211	0.9211	0.9211	0.9211	0.9212	0.9212	0.9212	0.9212	0.9212	0.9212
3.5	0.9212	0.9212	0.9212	0.9212	0.9213	0.9213	0.9213	0.9213	0.9213	0.9213
3.6	0.9213	0.9213	0.9213	0.9213	0.9214	0.9214	0.9214	0.9214	0.9214	0.9214

TABLE A.2

t Distribution: Critical Values of t

Degrees of freedom	Two-tailed test:					One-tailed test:				
	10%	5%	2.5%	1%	0.5%	10%	5%	2.5%	1%	0.5%
1	6.314	12.706	31.821	63.657	318.309	1.645	1.960	2.878	4.773	6.366
2	2.920	4.303	6.965	9.925	22.327	1.645	1.960	2.878	4.773	6.366
3	2.353	3.182	5.841	8.161	16.224	1.645	1.960	2.878	4.773	6.366
4	2.132	2.776	5.408	7.173	14.267	1.645	1.960	2.878	4.773	6.366
5	2.015	2.571	5.051	6.608	12.924	1.645	1.960	2.878	4.773	6.366
6	1.943	2.447	4.759	6.215	12.151	1.645	1.960	2.878	4.773	6.366
7	1.894	2.365	4.599	5.965	11.716	1.645	1.960	2.878	4.773	6.366
8	1.860	2.306	4.484	5.808	11.476	1.645	1.960	2.878	4.773	6.366
9	1.833	2.262	4.414	5.715	11.325	1.645	1.960	2.878	4.773	6.366
10	1.812	2.228	4.360	5.646	11.257	1.645	1.960	2.878	4.773	6.366
11	1.796	2.201	4.318	5.593	11.204	1.645	1.960	2.878	4.773	6.366
12	1.782	2.179	4.281	5.552	11.161	1.645	1.960	2.878	4.773	6.366
13	1.771	2.160	4.255	5.521	11.127	1.645	1.960	2.878	4.773	6.366
14	1.761	2.145	4.234	5.497	11.098	1.645	1.960	2.878	4.773	6.366
15	1.753	2.131	4.216	5.477	11.073	1.645	1.960	2.878	4.773	6.366
16	1.746	2.120	4.200	5.460	11.052	1.645	1.960	2.878	4.773	6.366
17	1.740	2.110	4.186	5.445	11.034	1.645	1.960	2.878	4.773	6.366
18	1.734	2.101	4.173	5.432	11.019	1.645	1.960	2.878	4.773	6.366
19	1.729	2.093	4.161	5.420	11.006	1.645	1.960	2.878	4.773	6.366
20	1.725	2.086	4.150	5.409	11.000	1.645	1.960	2.878	4.773	6.366
21	1.721	2.080	4.140	5.400	11.000	1.645	1.960	2.878	4.773	6.366
22	1.717	2.074	4.131	5.392	11.000	1.645	1.960	2.878	4.773	6.366
23	1.714	2.069	4.123	5.385	11.000	1.645	1.960	2.878	4.773	6.366
24	1.711	2.064	4.116	5.379	11.000	1.645	1.960	2.878	4.773	6.366
25	1.708	2.060	4.110	5.374	11.000	1.645	1.960	2.878	4.773	6.366
26	1.706	2.056	4.104	5.369	11.000	1.645	1.960	2.878	4.773	6.366
27	1.703	2.052	4.100	5.365	11.000	1.645	1.960	2.878	4.773	6.366
28	1.701	2.048	4.096	5.361	11.000	1.645	1.960	2.878	4.773	6.366
29	1.699	2.045	4.092	5.358	11.000	1.645	1.960	2.878	4.773	6.366
30	1.697	2.042	4.089	5.355	11.000	1.645	1.960	2.878	4.773	6.366
32	1.694	2.037	4.085	5.352	11.000	1.645	1.960	2.878	4.773	6.366
34	1.691	2.032	4.081	5.349	11.000	1.645	1.960	2.878	4.773	6.366
36	1.688	2.028	4.077	5.346	11.000	1.645	1.960	2.878	4.773	6.366
38	1.686	2.024	4.073	5.343	11.000	1.645	1.960	2.878	4.773	6.366
40	1.684	2.021	4.070	5.340	11.000	1.645	1.960	2.878	4.773	6.366
42	1.682	2.018	4.067	5.337	11.000	1.645	1.960	2.878	4.773	6.366
44	1.680	2.015	4.064	5.334	11.000	1.645	1.960	2.878	4.773	6.366
46	1.679	2.013	4.061	5.331	11.000	1.645	1.960	2.878	4.773	6.366
48	1.677	2.011	4.058	5.328	11.000	1.645	1.960	2.878	4.773	6.366
50	1.676	2.009	4.056	5.326	11.000	1.645	1.960	2.878	4.773	6.366
60	1.671	2.000	4.049	5.319	11.000	1.645	1.960	2.878	4.773	6.366
70	1.667	1.994	4.043	5.313	11.000	1.645	1.960	2.878	4.773	6.366
80	1.664	1.990	4.039	5.309	11.000	1.645	1.960	2.878	4.773	6.366
90	1.662	1.987	4.036	5.306	11.000	1.645	1.960	2.878	4.773	6.366
100	1.660	1.984	4.034	5.304	11.000	1.645	1.960	2.878	4.773	6.366
120	1.658	1.980	4.031	5.301	11.000	1.645	1.960	2.878	4.773	6.366
150	1.655	1.976	4.028	5.298	11.000	1.645	1.960	2.878	4.773	6.366
200	1.653	1.972	4.025	5.295	11.000	1.645	1.960	2.878	4.773	6.366
300	1.650	1.968	4.022	5.292	11.000	1.645	1.960	2.878	4.773	6.366
400	1.649	1.966	4.020	5.290	11.000	1.645	1.960	2.878	4.773	6.366
500	1.648	1.965	4.019	5.289	11.000	1.645	1.960	2.878	4.773	6.366
600	1.647	1.964	4.018	5.288	11.000	1.645	1.960	2.878	4.773	6.366
$\infty$	1.645	1.960	4.015	5.286	11.000	1.645	1.960	2.878	4.773	6.366

TABLE A.3

F Distribution: Critical Values of F (5% significance level)

$v_1$	1	2	3	4	5	6	7	8	9	10	12	14	16	18	20
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54	241.88	243.91	245.36	246.46	247.32	248.01
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	19.40	19.41	19.42	19.43	19.44	19.45
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.71	8.69	8.67	8.66
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.87	5.84	5.82	5.80
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.64	4.60	4.58	4.56
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.96	3.92	3.90	3.87
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.53	3.49	3.47	3.44
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.24	3.20	3.17	3.15
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.03	2.99	2.96	2.94
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.86	2.83	2.80	2.77
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.74	2.70	2.67	2.65
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.64	2.60	2.57	2.54
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.55	2.51	2.48	2.46
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.48	2.44	2.41	2.39
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.42	2.38	2.35	2.33
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.37	2.33	2.30	2.28
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.33	2.29	2.26	2.23
18	4.41	3.55	3.16	2.92	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.29	2.25	2.22	2.19
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.26	2.21	2.18	2.16
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.22	2.18	2.15	2.12
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.20	2.16	2.12	2.10
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.17	2.13	2.10	2.07
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.15	2.11	2.08	2.05
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.13	2.09	2.05	2.03
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.11	2.07	2.04	2.01
26	4.22	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.15	2.09	2.05	2.02	1.99
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.08	2.04	2.00	1.97
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.06	2.02	1.99	1.96
29	4.18	3.33	2.95	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.05	2.01	1.97	1.94
30	4.17	3.32	2.92	2.69	2.55	2.42	2.33	2.27	2.21	2.16	2.09	2.04	1.99	1.96	1.93
35	4.12	3.27	2.87	2.64	2.49	2.37	2.29	2.22	2.16	2.11	2.04	1.99	1.94	1.91	1.88
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.95	1.90	1.87	1.84
50	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.07	2.03	1.95	1.89	1.85	1.81	1.78
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.86	1.82	1.78	1.75
70	3.98	3.13	2.74	2.50	2.35	2.23	2.14	2.07	2.02	1.97	1.89	1.84	1.79	1.75	1.72
80	3.96	3.11	2.72	2.49	2.33	2.21	2.13	2.06	2.00	1.95	1.88	1.82	1.77	1.73	1.70
90	3.95	3.10	2.71	2.47	2.32	2.20	2.11	2.04	1.99	1.94	1.86	1.80	1.76	1.72	1.69
100	3.94	3.09	2.70	2.46	2.31	2.19	2.10	2.03	1.97	1.92	1.85	1.79	1.75	1.71	1.68
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96	1.91	1.83	1.78	1.73	1.69	1.66
150	3.90	3.06	2.66	2.43	2.27	2.16	2.07	2.00	1.94	1.89	1.82	1.76	1.71	1.67	1.64
200	3.89	3.04	2.65	2.42	2.26	2.14	2.05	1.98	1.92	1.87	1.80	1.74	1.69	1.66	1.62
250	3.88	3.03	2.64	2.41	2.25	2.13	2.04	1.97	1.91	1.86	1.79	1.73	1.68	1.65	1.61
300	3.87	3.03	2.63	2.40	2.24	2.13	2.04	1.97	1.91	1.86	1.78	1.72	1.68	1.64	1.61
400	3.86	3.02	2.63	2.39	2.23	2.12	2.03	1.96	1.90	1.85	1.78	1.72	1.67	1.63	1.60
500	3.86	3.01	2.62	2.39	2.23	2.12	2.03	1.96	1.90	1.85	1.77	1.71	1.66	1.62	1.59
600	3.86	3.01	2.62	2.39	2.23	2.11	2.02	1.95	1.89	1.84	1.77	1.71	1.66	1.62	1.59
750	3.85	3.01	2.62	2.38	2.22	2.11	2.02	1.95	1.89	1.84	1.77	1.70	1.66	1.62	1.58
1000	3.85	3.00	2.61	2.38	2.22	2.11	2.02	1.95	1.89	1.84	1.76	1.70	1.65	1.61	1.58

TABLE A.4

$\chi^2$  (Chi-Squared) Distribution: Critical Values of  $\chi^2$

Degrees of Freedom	Significance level		
	5%	1%	0.1%
1	3.841	6.635	10.828
2	5.991	9.210	13.816
3	7.815	11.345	16.266
4	9.488	13.277	18.467
5	11.070	15.086	20.515
6	12.592	16.812	22.458
7	14.067	18.475	24.322
8	15.507	20.090	26.124
9	16.919	21.666	27.877
10	18.307	23.209	29.588