

**UNIVERSITY OF SWAZILAND**

**FINAL EXAMINATION 2011/12**

**BASS I**

**TITLE OF PAPER** : ELEMENTARY QUANTITATIVE METHODS I

**COURSE NUMBER** : MS011

**TIME ALLOWED** : THREE (3) HOURS

**INSTRUCTIONS** : 1. THIS PAPER CONSISTS OF  
SEVEN QUESTIONS.  
2. ANSWER ANY FIVE QUESTIONS

**SPECIAL REQUIREMENTS** : NONE

THIS EXAMINATION PAPER SHOULD NOT BE OPENED UNTIL  
PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR.

(b) If  $kx^3 + 9x^2 - 3x - 7$  is divided by  $x + 1$ , the remainder is  $-4$ . Find the value of  $k$ . [M3A2]

(c) Use long division to evaluate  $(6x^3 - 5x^2 + x - 4) \div (2x^2 - x + 3)$ . [M6A4]

### QUESTION 2

(a) Solve the following equations for  $x$

(i)  $\log_2 x + \log_2(x + 2) = 3$  [M3A3]

(ii)  $\log(x^2 + 1) - \log(x - 2) = 1$  [M3A3]

(b) Evaluate

(i)  $\log_3 243$  [M2A2]

(ii)  $\log_{10} \frac{1}{10000}$  [M2A2]

### QUESTION 3

(a) Prove the following trig identities

(i)  $\sin \theta + \cos \theta \cot \theta = \theta$  [M3A2]

(ii)  $\frac{(\sec \theta - 1)(\sec \theta + 1)}{\tan \theta} = \tan \theta$  [M3A2]

(b) (i) If  $\tan \theta = \frac{3}{4}$  and  $\theta$  is in  $\theta III$ , find  $\sin \theta$  and  $\cos \theta$  [M3A2]

(ii) If  $\sin \theta = \frac{12}{13}$  and  $\theta$  is in  $\theta II$ , find the other 5 ratios. [M3A2]

QUESTION 4

a) Find all roots of  $p(x) = x^3 - 9x^2 + 26x - 24 = 0$  [m6A4]

b) Solve the following trig equations

(i)  $\cos 2\theta = \frac{1}{2}$  [M6A4]

(ii)  $2\cos^2 \theta + \cos \theta - 1 = 0$  [M3A2]

QUESTION 5

a) Find the amount at the end of nine years on an original principal of E4 500 at 8% if interest is

(i) simple interest [M3A2]

(ii) compounded annually [M3A2]

b) Find an equation for each of the following straight lines. Write your answer in 3 different form

(i) through (2, 3) and (4, 8) [M3A2]

(ii) through (3, -3) and perpendicular to  $2x + 3y = 6$  [M2A2]

QUESTION 6

a) Use synthetic division to find the quotient and the remainder when  $p(x) = 2x^4 + 5x^3 - 2x^2 + 4x + 6$  is divided by  $D(x) = x + 3$ . [M6A4]

b) The area of a rectangle is 6 square metres. If the length is 1 metre longer than the width find the dimensions of the rectangle. [M6A4]

QUESTION 7

a) Given that  $f(x) = \frac{3}{x-2}$

(i) Find  $f(8)$

(ii) Find  $f^{-1}(x)$

(iii) Find  $f^{-1}\left(\frac{1}{2}\right)$  [10]

b) Given that  $\sin \theta = \frac{3}{5}$  and  $\theta$  is in  $\theta II$ .

Find

(i)  $\sin 2\theta$

(ii)  $\tan 2\theta$  [10]