

UNIVERSITY OF SWAZILAND

SUPPLEMENTARY EXAMINATION 2011/12

BASS I

TITLE OF PAPER : ELEMENTARY QUANTITATIVE METHODS I

COURSE NUMBER : MS011

TIME ALLOWED : THREE (3) HOURS

INSTRUCTIONS : 1. THIS PAPER CONSISTS OF
SEVEN QUESTIONS.
2. ANSWER ANY FIVE QUESTIONS

SPECIAL REQUIREMENTS : NONE

THIS EXAMINATION PAPER SHOULD NOT BE OPENED UNTIL
PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR.

QUESTION 1

- (a) Solve, giving solutions between 0° and 360° , the equation

$$\sin^2 \theta + 2 \cos \theta = 2$$

[10]

- (b) Find the exact value of $\cos 15^\circ$

[10]

- (c) Solve for x

(i) $2^x = 64$

$$2^x = 64$$

(ii) $3^x = \frac{1}{81}$

$$3^x = \frac{1}{81}$$

[10]

QUESTION 2

- (a) Use the remainder theorem to find the remainder when $p(x) = 5x^3 - 14x + 3$ is divided by $D(x) = x - 2$

[6]

- (b) Use the factor theorem to determine whether $D(x) = x - 5$ is a factor of $p(x) = x^3 + 2x^2 - 25x - 5$.

[8]

- (c) Solve $\tan 3\theta = 1$

[6]

QUESTION 3

- (a) Given that $f(x) = \frac{2x + 3}{x - 1}$ find

(i) $f(3)$

(ii) $f^{-1}(x)$

(iii) $f^{-1}(2)$

[12]

- (b) Solve $2 \log_5 x = \log_5(2x + 3)$

[8]

QUESTION 4

- a) Find the simple interest on E4000 at 20% for 9 years. [5]
- b) Find the amount at the end of 12 years on a principal of E8 000 at 8% compounded quarterly. [5]
- c) Solve for x
- (i) $4^x = 1024$.
- (ii) $3^x = 7$. [10]

QUESTION 5

- a) Determine whether $p(x) = x^3 - x^2 + 2$ is divisible by $D(x) = x + 1$. [6]
- b) Find all rational roots of $p(x) = x^4 - 5x^2 + 4$. [8]
- c) Use synthetic division to evaluate $(x^8 - 1) \div (x + 1)$. [6]

QUESTION 6

a) Prove the following identity

$$\frac{\sin \theta}{1 - \cot \theta} + \frac{\cos \theta}{1 - \tan \theta} = \sin \theta + \cos \theta$$

[10]

b) Find an equation of a straight line in

(i) through $(5, -5)$ parallel to $4x + y - 1 = 0$

(ii) through $(4, 3)$ perpendicular to $3x + 2y - 2 = 0$

[10]

QUESTION 7

a) Find the quotient and remainder when $p(x) = 3x^4 - 4x^3 + 2x + 1$ is divided by $D(x) = x^2 + 2x$

[10]

b) Two rectangular rooms each have an area of $240m^2$. If the length of one of the rooms is x metres and the other room is $4m$ longer, write down the width of each room in terms of x . If the width of the rooms differ by $3m$ form an equation in x and show that this reduce to $x^2 + 4x - 320 = 0$. Solve this equation.

[10]