

**UNIVERSITY OF SWAZILAND**

**SUPPLEMENTARY EXAMINATION PAPER 2005**

**TITLE OF PAPER :       INDIRECT TECHNIQUES OF DEMOGRAPHIC ESTIMATION**

**COURSE CODE    :       DEM 303**

**TIME ALLOWED  :       THREE (3) HOURS**

**INSTRUCTIONS  :       ANSWER ALL QUESTIONS FROM SECTION A AND ANY THREE (3) QUESTIONS FROM SECTION B.**

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**SECTION A: ANSWER ALL QUESTIONS (40 MARKS)**

**QUESTION 1 (4+12+4 marks)**

- a. Discuss the importance of indirect estimation in demography. Elaborate your answer with an example.
- b. Describe briefly the characteristics of each region (family) of the Coale and Demeny regional model life tables.
- c. Describe how you would select a model life table from the Coale and Demeny regional model life tables to use in specific demographic estimation.

**QUESTION 2 (6+10+4 marks)**

- a. What are the uses of Brass logit system?
- b. Brass' logit lifetable system mathematically relates two different life tables using the equation:  

$$\text{Logit}(l_x) = \alpha + \beta (l_x^*)$$
  - (i) Define the functions  $l_x$ ,  $l_x^*$ , and the parameters  $\alpha$  and  $\beta$ .
  - (ii) Give the formula for computing logit ( $l_x$ ).
  - (iii) Briefly outline two of the methods used to compute the parameters  $\alpha$  and  $\beta$ .
- c. What are the advantages of the logit system?

## SECTION B: ANSWER ANY THREE (3) QUESTIONS

(60 MARKS)

## QUESTION 3 (4+4+12 marks)

- What are the assumptions of the Widowhood method?
- What data are required to make use of the widowhood method?
- Outline the computational procedure for estimating the conditional female conditional survivorship probabilities using the widowhood method.

## QUESTION 4 (4+4+6+6 marks)

- Find the value of  ${}_4q_1$  corresponding to the level 13.8 in the female South Model life table.
- Find the value of  ${}_3d_2$  corresponding to the level 14.7 in the female North model life table.
- What is the probability of surviving to age 4 in a population whose probability of surviving to age 5 is 0.785? Assume that the North model is applicable.
- Using the West model, compute the percentage change in the under five female mortality when the level changes from 9 to 10.

## QUESTION 5 (10+10 marks)

Describe any two of the following indirect demographic estimation methods. Make sure to include data requirements and computational procedures of each method.

- Sisterhood method;
- Orphanhood Method; and
- Brass P/F Ratio Method.

## QUESTION 6 (6+4+6+4 marks)

- What are the characteristics of a stable population?
- What is the difference between strong ergodicity and weak ergodicity?
- Outline three uses of stable populations.
- What is the difference between relational models and parametric models?

TABLE XIV. Values of  $l_x$  by single years of age from 1 to 5 for regional model life tables ( $l_0 = 100,000$ ) at mortality levels 1-24

LEVEL	MODEL					WEST					MODEL					NORTH											
	$l_1$	$l_2$	$l_3$	$l_4$	$l_5$	$l_1$	$l_2$	$l_3$	$l_4$	$l_5$	$l_1$	$l_2$	$l_3$	$l_4$	$l_5$	$l_1$	$l_2$	$l_3$	$l_4$	$l_5$	$l_1$	$l_2$	$l_3$	$l_4$	$l_5$		
1	63445	54958	51154	48696	46836	58050	50262	46851	44617	42957	62858	54755	49828	46166	43381	68005	59681	54557	50689	47753	62858	54755	49828	46166	43381	40000	37000
2	66601	58514	54891	52549	50776	61614	54105	50817	48663	47062	66052	58313	53606	50109	47449	70776	62905	58061	54403	51626	66052	58313	53606	50109	47449	44000	41000
3	69444	61785	58353	56135	54456	64826	57643	54497	52437	50906	68919	61570	57101	53780	51254	73263	65852	61290	57847	55232	68919	61570	57101	53780	51254	47000	44000
4	72027	64811	61578	59488	57907	67743	60918	57929	55972	54517	71515	64572	60350	57212	54826	75516	68564	64285	61055	58602	71515	64572	60350	57212	54826	50000	47000
5	74389	67625	64593	62634	61152	70411	63965	61142	59293	57919	73883	67354	63382	60432	58187	77570	71074	67074	64055	61763	73883	67354	63382	60432	58187	53000	50000
6	76562	70251	67423	65596	64213	72865	66812	64160	62424	61133	76057	69943	66224	63461	61359	79456	73407	69683	66871	64373	76057	69943	66224	63461	61359	56000	53000
7	78571	72713	70088	68391	67107	75135	68812	67004	65382	64177	78119	71922	68252	65319	63360	81196	75585	72130	69521	67043	78119	71922	68252	65319	63360	58000	55000
8	80438	75028	72604	71037	69852	77243	71243	69691	68185	67066	80408	74394	70777	67819	65866	84308	78625	76008	73434	71101	80408	74394	70777	67819	65866	60000	57000
9	82178	77211	74986	73547	72459	79209	74360	72237	70846	69813	82807	76601	74654	73378	72430	87022	81349	78665	76335	74019	82807	76601	74654	73378	72430	65000	62000
10	83807	79276	77246	75933	74940	81049	76601	74654	73378	72430	84616	78206	76275	75191	74288	89008	83092	80374	78206	76275	84616	78206	76275	75191	74288	68000	65000
11	85336	81233	79394	78206	77307	82775	78726	76953	75791	74928	86446	80374	78440	77144	76316	90884	84887	82442	80374	78440	86446	80374	78440	77144	76316	70000	67000
12	86775	83092	81441	80374	79567	84401	80745	79144	78096	77316	88004	81749	80084	78954	78208	91769	85954	83405	81749	80084	88004	81749	80084	78954	78208	72000	69000
13	88121	84865	83405	82462	81749	85983	82816	81428	80520	79844	89476	83405	81806	80520	79844	93949	87954	85413	83405	81806	89476	83405	81806	80520	79844	74000	71000
14	89396	86646	85413	84616	84013	87487	84756	83560	82777	82194	90476	84756	83092	82194	81547	94965	89089	86646	84756	83092	90476	84756	83092	82194	81547	76000	73000
15	90606	88290	87242	86559	86037	88804	86446	85414	84738	84235	91672	86446	84887	84235	83682	96884	91169	88290	86446	84887	91672	86446	84887	84235	83682	78000	75000
16	91769	89864	88987	88407	87954	90084	88086	87208	86632	86203	92517	88086	86446	85877	85499	97118	91769	89864	88987	88407	92517	88086	86446	85877	85499	80000	77000
17	92884	91352	90635	90153	89772	91322	89716	89076	88477	88098	93499	91266	90662	90244	89921	98361	92884	91352	90635	90153	93499	91266	90662	90244	89921	84000	81000
18	93949	92759	92192	91806	91496	92517	91266	90662	90244	89921	94965	93666	92266	91933	91672	99555	93949	92759	92192	91806	94965	93666	92266	91933	91672	86000	83000
19	94965	94089	93664	93372	93134	94767	93666	93372	93134	92933	96884	94767	94129	93547	93353	99995	94965	94089	93664	93372	96884	94767	94129	93547	93353	88000	85000
20	95931	95347	95059	94859	94693	95476	94693	94476	94329	94277	97718	95476	95236	95070	94937	99995	95931	95347	95059	94859	97718	95476	95236	95070	94937	90000	87000
21	96884	96531	96355	96231	96127	95866	96231	96127	96060	96011	97718	96531	96355	96231	96127	99995	96884	96531	96355	96231	97718	96531	96355	96231	96127	94000	91000
22	97718	97507	97400	97324	97260	96901	97324	97260	97200	97199	97718	97507	97400	97324	97260	99995	97718	97507	97400	97324	97718	97507	97400	97324	97260	96000	93000
23	98470	98361	98305	98264	98230	97838	98264	98230	98200	98199	98470	98361	98305	98264	98230	99995	98470	98361	98305	98264	98470	98361	98305	98264	98230	97000	94000
24	99095	99048	99024	99007	98992	98652	99007	98992	98982	98982	99095	99048	99024	99007	98982	99995	99095	99048	99024	99007	99095	99048	99024	99007	98982	98000	95000
25	99555	99540	99533	99527	99527	99289	99527	99527	99527	99527	99555	99540	99533	99527	99527	99995	99555	99540	99533	99527	99555	99540	99533	99527	99527	99000	96000

TABLE XIV (Continued). Values of  $l_x$  by single years of age from 1 to 5 for regional model life tables ( $l_0 = 100,000$ ) at mortality levels 1 to 24

LEVEL	E A S T				M O D E L				S O U T H					
	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	
1	57180	49795	46656	44596	43167	49453	42922	40206	38482	37222	48164	53927	66423	43368
2	60636	53494	50458	48466	47084	53511	47063	44382	42680	41436	51612	57056	68857	47083
3	63788	56935	54022	52111	50784	57211	50920	48305	46644	45431	54829	59951	71056	50567
4	66680	60150	57375	55554	54290	60606	54530	52003	50399	49227	57842	62645	73058	53846
5	69350	63168	60240	58815	57619	63741	57920	55500	53963	52840	60675	65163	74894	56941
6	71827	66009	63536	61913	60786	66649	61115	58814	57353	56286	63347	67526	76586	59870
7	74135	68692	66378	64860	63806	69358	64135	61963	60584	59577	65874	69750	78154	62849
8	76292	71232	69081	67670	66690	71891	66997	64962	63670	62725	67971	71850	80975	65291
9	78317	73643	71657	70353	69448	74268	69715	67822	66620	65742	70546	73838	82229	67870
10	80221	75936	74115	72920	72090	76504	72302	70555	69445	68635	72471	75422	83337	70092
11	82003	78166	76535	75464	74722	78599	74819	73247	72249	71520	74819	77504	85474	72446
12	83663	80270	78828	77881	77225	80519	77144	75741	74850	74199	77357	79929	87667	74702
13	85260	82285	81020	80191	79615	82373	79387	78145	77357	76781	79387	81547	89132	76867
14	86794	84213	83117	82397	81897	84161	81547	80461	79770	79266	80461	82092	90325	78502
15	88267	86059	85120	84504	84077	85882	83626	82688	82092	81657	82688	84829	88288	80935
16	89677	87823	87035	86518	86159	87536	85624	84829	84324	83956	84829	86470	88288	82282
17	91028	89531	88885	88455	88151	89123	87494	86867	86470	86166	86867	88539	88288	84018
18	92318	91160	90650	90305	90055	90643	89406	88879	88539	88288	88879	90529	90325	85574
19	93548	92706	92328	92069	91877	92095	91200	90797	90529	90325	90797	92429	90325	86935
20	94721	94176	93927	93753	93622	93480	92897	92620	92429	92282	92620	94127	92282	88065
21	95904	95546	95380	95262	95171	94852	94462	94266	94127	94018	94266	95648	94127	89906
22	96939	96718	96614	96539	96481	96111	95868	95741	95648	95574	95741	97110	95648	91718
23	97739	97681	97681	97638	97605	97245	97110	97035	96980	96935	97035	98116	96980	93190
24	98640	98583	98555	98535	98518	98219	98154	98116	98088	98065	98116	98936	98088	95799
25	99245	99223	99212	99204	99198	98989	98963	98948	98936	98926	98948	98936	98936	96906

  

LEVEL	M O D E L				S O U T H			
	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$	$l_x$
1	69279	55503	49161	45812	43909	66423	53927	48164
2	71532	58606	52655	49512	47727	68857	57056	51612
3	73567	61479	55913	52974	51304	71056	59951	54829
4	75420	64152	58964	56225	54668	73058	62645	57842
5	77119	66651	61832	59287	57894	74894	65163	60675
6	78685	68997	64537	62181	60843	76586	67526	63347
7	80136	71206	67094	64923	63689	78154	69750	65874
8	81487	73291	69518	67525	66394	79613	71850	68270
9	82748	75265	71820	70001	68968	80975	73838	70546
10	83916	77145	74028	72382	71447	82229	75650	72616
11	84937	78890	76106	74636	73801	83337	77434	74711
12	85933	80569	78099	76795	76054	84419	79153	76724
13	86903	82184	80011	78863	78211	85474	80809	78657
14	87848	83738	81845	80846	80278	86501	82405	80515
15	88764	85232	83606	82748	82260	87498	83941	82300
16	89651	86670	85297	84573	84161	88463	85419	84015
17	90509	88068	86936	86334	85986	89397	86841	85663
18	91342	89424	88523	88038	87751	90303	88235	87270
19	92266	90774	90064	89676	89440	91361	89859	89132
20	93180	92044	91496	91193	91004	92369	91237	90668
21	94089	93256	92849	92620	92475	93372	92551	92123
22	94988	94405	94116	93952	93846	94367	93799	93491
23	95868	95484	95292	95181	95108	95343	94765	94555
24	96716	96483	96365	96296	96249	96287	96064	95934
25	97514	97386	97321	97282	97255	97178	97057	96984