

UNIVERSITY OF SWAZILAND

MAIN EXAMINATION 2010

TITLE OF PAPER: INDIRECT TECHNIQUES FOR DEMOGRAPHIC ESTIMATION

COURSE NUMBER: DEM 303

TIME ALLOWED: 3 HOURS

INSTRUCTIONS: ANSWER QUESTION 1 AND 2 AND ANY TWO QUESTIONS FROM SECTION B. ALL QUESTIONS ARE WORTH 25 MARKS EACH.

REQUIREMENTS: CALCULATOR

THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR

SECTION A: COMPULSORY (Answer all questions)

Question 1

- a) Describe the importance of indirect estimation in Demography. Elaborate your answer with examples.(4)
- b) Describe how you would select a model life table from the Coale and Demeny regional model life tables to use in specific demographic estimation. (4)
- c) Find the value of ${}_4q_1$ corresponding to level 13.8 in the female South model life table.(4)
- d) Find the value of ${}_3d_2$ corresponding to level 14.7 in the female North model life table.(4)
- e) What is the probability of surviving to age 4 in a population whose probability of surviving to age 5 is 0.785? Assume the male East model is applicable. (5)
- f) Give any two weaknesses/limitations of the Brass Growth Balance method for estimating the completeness of death registration.(4)

Question 2

- a) What are the assumptions of the Brass method for estimating childhood mortality using information from women on the proportion of children dead? (6)
- b) You are given the data below on average parity per woman and proportion of children dead classified by age group of women. Using Trussel's variant of the Brass method, calculate $q(2)$ and $q(3)$. (8)

Age group	i	Average parity	Proportion dead
15-19	1	0.170	0.0560
20-24	2	1.100	0.0817
25-29	3	2.360	0.0760

You may find the following information useful:

i	a(i)	b(i)	c(i)
1	1.0819	-3.0005	0.8689
2	1.2846	-0.6181	-0.3024
3	1.2223	0.0851	-0.4704

- c) Describe the problems associated with the reverse survival technique.(6)
- d) Give an interpretation of the parameters for the Coale-McNeil model for nuptiality. (5)

SECTION B (answer any 2 questions)

Question 3

- a) You are given the following life table values for a certain country. Estimate the values of α and β you would use to fit the Brass logit model to the data. (16)

Age	l_x
15	0.592
20	0.559
25	0.548
30	0.528
35	0.511
40	0.492
45	0.460
50	0.435

- b) What do the data suggest about the age pattern of mortality for this country?(3)
c) Use the values of the parameters obtained to estimate the values for l_{10} and l_{55} . (6)

Question 4

- a) What is the difference between relational models and parametric models?(5)
b) What is the difference between life table models and stable population models? (6)
c) What are the characteristics of a stable population? (6)
d) Describe the Sisterhood method for maternal mortality. Make sure to include the data requirements and computational procedures. (8)

Question 5

- a) What are the disadvantages of the widowhood method for estimating adult survivorship? (6)
b) Using the data on the proportion of ever married respondents classified by age given below, calculate the male probability of survival from age 20 to age 35 and from age 20 to 40. (10)

Age	$NW_f(n)$	$NW_f(n-5)$
30	0.8668	0.7408
35	0.9246	0.8668
40	0.9458	0.9246

You may find the following information useful:

n	a(n)	b(n)	c(n)	d(n)
30	-0.0284	-0.00465	0.00157	1.0822
35	-0.0159	-0.00638	0.00253	1.0831
40	-0.0041	-0.00784	0.00395	1.0596

Assume that $SMAM_m = 25.3$ years and $SMAM_f = 23.2$ years.

- c) What are the assumptions for the orphanhood method for estimating adult mortality? (6)
- d) One of the methods for estimating fertility is by using the increment of cohort parities between two surveys/censuses. Under what conditions is it appropriate to use this method? (3)

Question 6

- a) Give an interpretation of the parameters for the Brass Relational Gompertz model for fertility. (6)
- b) You are given the following age-specific marital fertility rates attained by a certain Christian religious group living in the USA for a certain period.

Age group	ASMFR
15-19	0.300
20-24	0.550
25-29	0.502
30-34	0.447
35-39	0.406
40-44	0.222
45-49	0.061

Use the Coale-Trussel model to estimate the parameters m and M you would use to fit the marital fertility schedule, using the least squares method. (15)

You may find the following information useful: $Y(i) = \ln [\Phi(i)/h(i)]$

- c) Give an interpretation of the parameters obtained above.(4)

TABLE XIV. Values of l_x by single years of age from 1 to 5 for regional model life tables ($l_0 = 100,000$) at mortality levels 1-24

LEVEL	Females		Males		WEST		MODEL		NORTH		MODEL		NORTH	
	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x	l_x
1	63445	54958	51154	48696	58050	50262	46836	50689	62858	54755	47753	50689	62858	54755
2	66601	58514	54891	52549	61614	54105	50776	54403	66052	58313	51626	54403	66052	58313
3	69444	61785	58353	56135	64826	57643	54456	57847	68919	61570	55232	57847	68919	61570
4	72027	64811	61578	59488	67743	60918	57907	61055	71515	64572	58602	61055	71515	64572
5	74389	67625	64593	62634	70411	63965	61152	63883	73883	67354	61763	63883	73883	67354
6	76562	70251	67423	65596	72865	66812	64213	66871	76057	69943	67543	66871	76057	69943
7	78571	72713	70088	68391	75135	69481	67107	69591	78062	72362	70197	69591	78062	72362
8	80438	75028	72604	71037	77243	71992	69852	71723	80624	74631	72197	71723	80624	74631
9	82178	77211	74986	73547	79209	74360	72459	74900	83264	78177	75101	74900	83264	78177
10	83807	79276	77246	75933	81042	76601	74900	77307	84777	80679	77373	77307	84777	80679
11	85336	81233	79394	78206	82775	78726	77307	79567	86196	82479	79535	79567	86196	82479
12	86775	83092	81441	80374	84401	80745	79567	82440	87529	84247	81724	82440	87529	84247
13	88121	84865	83405	82462	85983	82816	81749	84654	88709	85835	83396	84654	88709	85835
14	89396	86646	85413	84616	87487	84756	83560	86559	89758	87367	85751	86559	89758	87367
15	90606	88290	87242	86559	88804	86446	85414	88087	90652	88548	87134	88087	90652	88548
16	91769	89864	88987	88407	90084	88086	87208	89527	91517	89588	88230	89527	91517	89588
17	92884	91352	90635	90153	91322	89716	89772	91806	92511	90662	90244	91806	92511	90662
18	93949	92759	92192	93372	92517	91266	91496	93134	93666	92266	91933	93134	93666	92266
19	94965	94089	94089	93664	94767	94129	94693	94859	94767	94129	94547	94859	94767	94129
20	95931	95347	95059	94859	95866	95460	95127	96231	95866	95460	95236	96231	95866	95460
21	96884	96531	96355	96231	96901	96648	96501	97324	96901	96648	96501	97324	96901	96648
22	97718	97507	97400	97324	97838	97699	97616	98264	97838	97699	97616	98264	97838	97699
23	98470	98305	98305	98264	98552	98588	98548	99007	98552	98588	98548	99007	98552	98588
24	99095	99048	99024	99007	99289	99266	99522	99527	99289	99266	99522	99527	99289	99266
25	99555	99540	99533	99527										
1	68005	59681	54557	50689	62858	54755	47753	50689	62858	54755	47753	50689	62858	54755
2	70776	62905	58061	54403	66052	58313	51626	54403	66052	58313	51626	54403	66052	58313
3	73263	65852	61290	57847	68919	61570	55232	57847	68919	61570	55232	57847	68919	61570
4	75516	68564	64285	61055	71515	64572	58602	61055	71515	64572	58602	61055	71515	64572
5	77570	71074	67074	64055	73883	67354	61763	64055	73883	67354	61763	64055	73883	67354
6	79456	73407	69683	66871	76057	69943	67543	66871	76057	69943	67543	66871	76057	69943
7	81196	75585	72130	69523	78062	72362	70197	69523	78062	72362	70197	69523	78062	72362
8	82808	77625	74434	72025	79920	74631	72197	72025	79920	74631	72197	72025	79920	74631
9	84508	79542	76608	74394	81620	76764	74019	74394	81620	76764	74019	74394	81620	76764
10	85709	81349	78665	76639	83264	78777	75101	76639	83264	78777	75101	76639	83264	78777
11	87022	83056	80615	78772	84777	80679	77373	78772	84777	80679	77373	78772	84777	80679
12	88253	84670	82464	80799	86196	82479	79535	80799	86196	82479	79535	80799	86196	82479
13	89398	86244	84302	82337	87529	84247	81724	82337	87529	84247	81724	82337	87529	84247
14	90441	87729	86046	84770	88709	85835	83396	84770	88709	85835	83396	84770	88709	85835
15	91453	89164	87717	86609	89758	87367	85751	86609	89758	87367	85751	86609	89758	87367
16	92431	90521	89291	88340	90975	88909	87595	88340	90975	88909	87595	88340	90975	88909
17	93372	91802	90773	89971	92054	90376	89335	89971	92054	90376	89335	89971	92054	90376
18	94274	93012	91508	90978	93094	91759	90927	90978	93094	91759	90927	90978	93094	91759
19	95136	94153	93487	92959	94091	93061	92531	92959	94091	93061	92531	92959	94091	93061
20	95956	95230	94729	94330	95043	94286	94003	94330	95043	94286	94003	94330	95043	94286
21	96736	96246	95904	95628	95950	95437	95401	95628	95950	95437	95401	95628	95950	95437
22	97487	97221	97032	96879	96826	96534	96534	96879	96826	96534	96534	96879	96826	96534
23	98122	97974	97867	97780	97580	97408	97408	97780	97580	97408	97408	97780	97580	97408
24	98723	98648	98593	98548	98321	98230	98230	98548	98321	98230	98230	98548	98321	98230
25	99219	99187	99163	99144	98944	98904	98912	99144	98944	98904	98912	99144	98944	98904

TABLE XIV (Continued). Values of l_x by single years of age from 1 to 5 for regional model life tables ($l_0 = 100,000$) at mortality levels 1 to 24

LEVEL	M O D E L			E A S T			M O D E L			S O U T H		
	l_1	l_2	l_3	l_1	l_2	l_3	l_1	l_2	l_3	l_1	l_2	l_3
1	57180	49795	46656	44596	43167	49453	42922	40206	38482	43368	45074	48164
2	60636	53494	50458	48466	47084	53511	47063	44382	42680	47083	48694	51612
3	63788	56935	54022	52111	50784	57211	50920	48305	46644	50567	52083	54829
4	66680	60150	57375	55554	54290	60606	54530	52003	50399	53846	55267	57842
5	69350	63168	60340	58815	57619	63741	57920	55500	53963	56941	58269	60675
6	71827	66009	63536	61913	60786	66649	61115	58814	57353	61107	63347	65870
7	74135	68692	66378	64860	63806	69358	64135	61963	60584	64962	67351	70529
8	76292	71232	69081	67670	66697	71891	66997	64962	63620	68742	71670	74977
9	78317	73643	71857	70353	69448	74268	69715	67555	66445	71520	74445	77850
10	80221	75936	74115	72920	72090	76504	72302	70555	69445	74199	77022	80498
11	82003	78166	76535	75464	74722	78999	74819	73247	72249	77450	80357	83926
12	83663	80270	78828	77881	77225	80519	77144	75741	74850	79781	82735	86470
13	85260	82285	81020	80191	79615	82373	79387	78145	77357	81661	84611	88488
14	86794	84213	83117	82397	81897	84161	81547	80461	79770	83626	86770	90325
15	88267	86059	85120	84304	84077	85882	83626	82688	82092	86324	89429	93282
16	89677	87823	87035	86518	86159	87536	85624	84829	84324	88470	91627	95574
17	91028	89531	88865	88455	88151	89123	87544	86887	86470	90529	92822	96980
18	92318	91160	90650	90305	90055	90643	89406	88879	88539	92429	94729	98935
19	93548	92706	92328	92069	91877	92095	91200	90797	90529	94229	96448	100000
20	94721	94176	93927	93753	93622	93880	92897	92620	92429	96111	97935	100000
21	95904	95546	95262	95171	95171	94852	94462	94256	94127	97448	99088	100000
22	96939	96718	96614	96481	96481	96111	95868	95741	95648	98116	100000	100000
23	97861	97739	97638	97605	97605	97245	97110	97035	96980	98811	100000	100000
24	98640	98583	98555	98535	98518	98219	98154	98116	98088	98935	100000	100000
25	99245	99223	99212	99204	99198	98989	98963	98948	98936	98935	100000	100000

TABLE 3. STANDARD PATTERN OF NATURAL FERTILITY AND OF DEVIATIONS FROM NATURAL FERTILITY, BY AGE GROUP, FOR THE COALE AND TRUSSELL FERTILITY MODEL.

Age group (1)	Index i (2)	Natural fertility $h(i)$ (3)	Deviation pattern from natural fertility $w(i)$ (4)
15-19	1	0.411	0.000
20-24	2	0.460	0.000
25-29	3	0.431	-0.279
30-34	4	0.395	-0.667
35-39	5	0.322	-1.042
40-44	6	0.167	-1.414
45-49	7	0.024	-1.671

ANNEX II

General and African Standard Life Table l_x 's and Logits

General standard			African standard		
x	l_x	$Y_x(x)$	x	l_x	$Y_x(x)$
0	1.0000		0	1.0000	
1	0.8499	-0.8670	1	0.8802	-0.9972
2	0.8070	-0.7153	2	0.8335	-0.8053
3	0.7876	-0.6553	3	0.8101	-0.7253
4	0.7762	-0.6218	4	0.7964	-0.6820
5	0.7691	-0.6016	5	0.7863	-0.6514
10	0.7502	-0.5498	10	0.7502	-0.5498
15	0.7362	-0.5131	15	0.7362	-0.5131
20	0.7130	-0.4551	20	0.7130	-0.4551
25	0.6826	-0.3829	25	0.6326	-0.3829
30	0.6525	-0.3150	30	0.6525	-0.3150
35	0.6223	-0.2496	35	0.6223	-0.2496
40	0.5898	-0.1817	40	0.5898	-0.1817
45	0.5535	-0.1073	45	0.5535	-0.1073
50	0.5106	-0.0212	50	0.5106	-0.0212
55	0.4585	0.0832	55	0.4585	0.0832
60	0.3965	0.2100	60	0.3965	0.2100
65	0.3210	0.3746	65	0.3210	0.3746
70	0.2380	0.5818	70	0.2380	0.5818
75	0.1516	0.8611	75	0.1516	0.8611
80	0.0768	1.2433	80	0.0768	1.2433
85	0.0276	1.7810	85	0.0276	1.7810
90	0.0059	2.5634	90	0.0059	2.5634
95	0.0006	3.7090	95	0.0006	3.7090
100	0.0000		100	0.0000	

Source: Carrier and Hobcraft (1973) (These are the smoothed and extended versions of the original standard)