

**UNIVERSITY OF SWAZILAND**

**FINAL EXAMINATION PAPER 2011**

**TITLE OF PAPER : NONPARAMETRIC ANALYSIS**

**COURSE CODE : ST409**

**TIME ALLOWED : TWO (2) HOURS**

**REQUIREMENTS : CALCULATOR AND STATISTICAL TABLES**

**INSTRUCTIONS : ANSWER ANY THREE QUESTIONS**

### Question 1

[20 marks, 10+10]

- (a) In an attempt to assess the effectiveness of a political candidate's campaign oratory, a group of 60 subjects were asked the question prior to and after a prepared speech by the candidate, "If the election were held right now, would you vote for Candidate X against the incumbent?" The results are as follows:

Before	After	
	-	+
+	2	25
-	20	13

Are the responses before and after the speech associated? Use  $\alpha = 0.05$ .

- (b) The following data are the annual incomes (in thousands of emalangeni) for a random sample of  $n = 10$  adults from a certain area

12.8, 13.6, 14.7, 16.2, 17.9, 18.6, 19.2, 19.8, 20.3, 24.4

Use the *sign* test to test that the median income doesn't exceed SZL20000 in this particular area. Use the exact null distribution of your test statistic to determine the critical value. Report your conclusions.

### Question 2

[20 marks, 10+10]

- (a) In a survey conducted in 1992, senior high school students were asked if they had ever used marijuana. Of the females sampled, 445 said yes and 675 said no; of the males sampled, 515 said yes and 641 said no. Are male high school students more likely to use marijuana?
- (b) It is desired to design a given automobile to allow enough headroom to accommodate comfortably all but the tallest 5% of the people who drive. Former studies indicate that the 95<sup>th</sup> percentile was 70.3 inches. In order to see if the former studies are still valid, a random sample of size 100 is selected. It is found that the 12 tallest persons in the sample have the following heights.

72.6, 70.0, 71.3, 70.5, 70.8, 76.0, 70.1, 72.5, 71.1, 70.6, 71.9, 72.8

Is it reasonable to use 70.3 as the 95<sup>th</sup> percentile.

### Question 3

[20 marks, 8+12]

- (a) Find the exact distribution of the Wilcoxon Signed Rank statistic for  $n = 4$ .
- (b) The following data give the stroke index for 7 patients before and after treatment. We wish to test the hypothesis that the treatment has no effect.

Before	109	57	53	57	68	72	51
After	56	44	55	40	62	46	48

Use an appropriate test to see if the treatment has no effect. Use a 5% significance level. State the hypothesis, define the critical region(s) and conclusion. Also derive a 95% confidence interval for the median difference. Show all calculations.

### Question 4

[20 marks, 10+10]

- (a) The following data, arising from independent runs of a particular experiment, are a sample of  $n = 10$  proportions:

0.012, 0.020, 0.076, 0.090, 0.179, 0.187, 0.190, 0.328, 0.622, 0.764.

Use an appropriate test to assess at the 10% significance level whether these data can be regarded as being sampled from a distribution having *cdf*

$$F_X(x) = 1 - (1 - x)^3, \quad 0 < x < 1.$$

- (b) In a diet test, each of four diet programs is applied to a sample of people. At the end of three weeks, the amount of pounds people lost are shown below.

Diet Program			
1	2	3	4
12	19	16	28
6	10	20	17
18	13	26	22
23	20	19	16
25	20		

Test to determine if there is enough evidence at the 5% significance level to infer that at least two population locations differ.

### Question 5

[20 marks, 10+10]

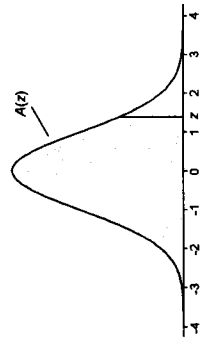
- (a) An experimenter was involved in a study to determine if there is an association between stress and mental health. The Hopkins Symptom Checklist was used to determine the level of symptoms experiences and a scale was developed to measure stress levels. For data obtained, refer to the following table. Use **Kendall's tau** to perform the appropriate test at the 1% level of significance.

Participant	Stress (X)	Symptoms (Y)
1	33	100
2	30	92
3	11	83
4	18	69
5	5	98
6	16	105
7	3	65
8	21	84
9	21	70
10	35	120

- (b) On 20 successive trips between Manzini and Mbabane a bus carried 24, 19, 32, 28, 21, 23, 26, 17, 20, 28, 30, 24, 13, 35, 26, 21, 19, 29, 27, and 23 passengers. Test whether it is reasonable to treat these data as if they constitute a random sample at  $\alpha = 0.01$ .

TABLE A-1  
Cumulative Standardized Normal Distribution

$A(z)$  is the integral of the standardized normal distribution from  $-\infty$  to  $z$  (in other words, the area under the curve to the left of  $z$ ). It gives the probability of a normal random variable not being more than  $z$  standard deviations above its mean. Values of  $z$  of particular importance:

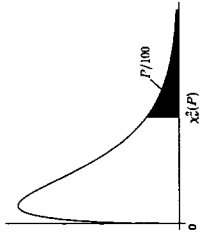


$z$	$A(z)$	Lower limit of right 5% tail
1.645	0.9500	Lower limit of right 2.5% tail
1.960	0.9750	Lower limit of right 1% tail
2.326	0.9900	Lower limit of right 0.5% tail
2.576	0.9950	Lower limit of right 0.1% tail
3.090	0.9990	Lower limit of right 0.05% tail
3.291	0.9995	

$z$	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9958	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9978	0.9979	0.9980	0.9981	0.9982	0.9983
2.9	0.9984	0.9985	0.9986	0.9987	0.9988	0.9989	0.9990	0.9991	0.9992	0.9993
3.0	0.9994	0.9995	0.9996	0.9997	0.9998	0.9999	0.9999	0.9999	0.9999	0.9999
3.1	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.2	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.3	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.4	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.5	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.6	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998

Percentage Points of the  $\chi^2$ -Distribution

This table gives the percentage points  $\chi^2(P)$  for various values of  $P$  and degrees of freedom  $\nu$ , as indicated by the figure to the right.



If  $X$  is a variable distributed as  $\chi^2$  with  $\nu$  degrees of freedom,  $P/100$  is the probability that  $X \geq \chi^2(P)$ . For  $\nu > 100$ ,  $\sqrt{2X}$  is approximately normally distributed with mean  $\sqrt{2\nu - 1}$  and unit variance.

$\nu$	Percentage points $P$											
	1	2	3	4	5	10	5	2.5	1	0.5	0.1	0.05
1	2.706	3.841	5.024	6.635	7.879	10.828	12.116	15.202	17.730	19.987	22.105	24.103
2	4.605	5.991	7.378	9.210	10.597	13.816	16.266	18.467	20.515	22.458	24.103	26.018
3	6.251	7.815	9.348	11.345	12.838	16.266	18.467	20.515	22.458	24.103	26.018	27.868
4	7.779	9.488	11.143	13.277	14.860	18.467	20.515	22.458	24.103	26.018	27.868	29.666
5	9.236	11.070	12.833	15.086	16.750	20.515	22.458	24.103	26.018	27.868	29.666	31.420
6	10.645	12.592	14.449	16.812	18.548	22.458	24.103	26.018	27.868	29.666	31.420	33.137
7	12.017	14.067	16.013	18.475	20.278	24.322	26.018	27.868	29.666	31.420	33.137	34.821
8	13.362	15.507	17.535	20.090	21.955	26.124	27.868	29.666	31.420	33.137	34.821	36.478
9	14.684	16.919	19.023	21.666	23.589	27.877	29.666	31.420	33.137	34.821	36.478	38.109
10	15.987	18.307	20.483	23.209	25.188	29.588	31.420	33.137	34.821	36.478	38.109	39.719
11	17.275	19.675	21.920	24.725	26.757	31.264	33.137	34.821	36.478	38.109	39.719	41.308
12	18.549	21.026	23.337	26.217	28.300	32.909	34.821	36.478	38.109	39.719	41.308	42.879
13	19.812	22.362	24.736	27.688	29.819	34.528	36.478	38.109	39.719	41.308	42.879	44.434
14	21.064	23.685	26.119	29.141	31.319	36.123	38.109	39.719	41.308	42.879	44.434	45.973
15	22.307	24.996	27.488	30.578	32.801	37.697	39.719	41.308	42.879	44.434	45.973	47.498
16	23.542	26.296	28.845	32.000	34.267	39.252	41.308	42.879	44.434	45.973	47.498	49.000
17	24.769	27.587	30.191	33.409	35.718	40.790	42.879	44.434	45.973	47.498	49.000	50.490
18	25.989	28.869	31.526	34.805	37.156	42.312	44.434	45.973	47.498	49.000	50.490	51.969
19	27.204	30.144	32.852	36.191	38.582	43.820	45.973	47.498	49.000	50.490	51.969	53.438
20	28.412	31.410	34.170	37.566	39.987	45.315	47.498	49.000	50.490	51.969	53.438	54.897
25	34.382	37.652	40.646	44.314	46.928	52.620	54.897	56.703	58.337	59.703	60.981	62.158
30	40.256	43.773	46.979	50.892	53.672	59.703	62.158	64.766	67.331	69.126	70.631	71.920
40	51.805	55.758	59.342	63.691	66.766	73.402	76.095	78.756	81.331	83.658	85.801	87.786
50	63.167	67.505	71.420	76.154	79.490	86.561	89.561	92.338	94.976	97.329	99.432	101.280
80	96.578	101.879	106.629	112.329	116.321	124.839	128.261	131.445	134.284	136.864	139.209	141.313

## Percentage Points of the Wilcoxon Signed Rank Distribution

This table gives the lower percentage points of  $W^+$ , the sum of the ranks of the positive observations in a ranking in order of increasing absolute magnitude of a random sample of size  $n$  from a continuous distribution which is symmetric about zero. The function tabulated  $x(P)$  is the largest  $x$  such that  $P(W^+ < x) \leq P/100$ .

$n$	$P$											
	$n$	5	2.5	1	0.5	0.1	$n$	5	2.5	1	0.5	0.1
8	8	6	4	2	1	0	43	337	311	282	262	223
9	9	6	4	2	0	0	44	354	328	297	277	236
10	11	9	6	4	1	1	45	372	344	313	292	250
11	14	11	8	6	2	2	46	390	362	329	308	264
12	18	14	10	8	3	3	47	408	379	346	323	278
13	22	18	13	10	5	5	48	427	397	363	340	293
14	26	22	16	13	7	7	49	447	416	380	356	308
15	31	26	20	16	9	9	50	467	435	398	374	324
16	36	30	24	20	12	12	51	487	454	417	391	340
17	42	35	28	24	15	15	52	508	474	435	409	356
18	48	41	33	28	19	19	53	530	495	455	428	373
19	54	47	38	33	22	22	54	551	515	474	446	390
20	61	53	44	38	27	27	55	574	537	494	466	408
21	68	59	50	43	31	31	56	596	558	515	485	426
22	76	66	56	49	36	36	57	619	580	536	505	444
23	84	74	63	55	41	41	58	643	603	557	526	463
24	92	82	70	62	46	46	59	667	626	579	547	483
25	101	90	77	69	52	52	60	691	649	601	568	502
26	111	99	85	76	59	59	61	716	673	624	590	522
27	120	108	93	84	65	65	62	742	698	647	612	543
28	131	117	102	92	72	72	63	768	722	670	635	564
29	141	127	111	101	80	80	64	794	748	694	658	585
30	152	138	121	110	87	87	65	821	773	719	682	607
31	164	148	131	119	95	95	66	848	799	743	706	629
32	176	160	141	129	104	104	67	876	826	769	730	652
33	188	171	152	139	113	113	68	904	853	794	755	675
34	201	183	163	149	122	122	69	932	880	820	780	698
35	214	196	174	160	132	132	70	961	908	847	806	722
36	228	209	186	172	142	142	71	991	937	874	832	746
37	242	222	199	183	152	152	72	1021	965	902	859	771
38	257	236	212	195	163	163	73	1051	995	929	885	796
39	272	250	225	208	174	174	74	1082	1024	958	913	822
40	287	265	239	221	186	186	75	1113	1054	987	941	848
41	303	280	253	234	198	198	76	1145	1085	1016	969	874
42	320	295	267	248	210	210	77	1177	1116	1045	998	901
43	337	311	282	262	223	223	78	1210	1148	1076	1027	928

## Upper Critical Values for the Kruskal-Wallis Test

Group Sizes	Nominal size $\alpha$				
	0.10	0.05	0.025	0.01	
2 2	4.571 (.06667)	---	---	---	---
3 2 1	4.285 (.10000)	---	---	---	---
3 2 2	4.500 (.06667)	4.714 (.04762)	---	---	---
3 3 1	4.571 (.10000)	5.143 (.04286)	---	---	---
3 3 2	4.556 (.10000)	5.361 (.03214)	---	---	---
3 3 3	4.622 (.10000)	5.500 (.05000)	5.556 (.02500)	---	---
4 2 1	4.500 (.07619)	---	---	---	---
4 2 2	4.658 (.10000)	5.333 (.03333)	5.500 (.02500)	---	---
4 3 1	4.095 (.09286)	5.238 (.05000)	5.833 (.02143)	---	---
4 3 2	4.311 (.08841)	5.444 (.04603)	6.000 (.02381)	---	---
4 3 3	4.709 (.08238)	5.791 (.04371)	6.185 (.02476)	---	---
4 4 1	4.187 (.08238)	4.397 (.04762)	6.167 (.02423)	---	---
4 4 2	4.455 (.09076)	5.455 (.04444)	6.271 (.02413)	---	---
4 4 3	4.544 (.09076)	5.658 (.04444)	6.301 (.02413)	---	---
4 4 4	4.654 (.08824)	5.922 (.04666)	6.615 (.02484)	---	---
5 2 1	4.200 (.08824)	5.000 (.04762)	---	---	---
5 2 2	4.373 (.08985)	5.160 (.04430)	6.000 (.01852)	---	---
5 3 1	4.018 (.08524)	4.960 (.04762)	6.044 (.01984)	---	---
5 3 2	4.651 (.09127)	5.251 (.04921)	6.004 (.02460)	---	---
5 3 3	4.533 (.08637)	5.648 (.04892)	6.315 (.02121)	---	---
5 4 1	3.987 (.09841)	4.985 (.04444)	6.858 (.02381)	---	---
5 4 2	4.541 (.09841)	5.273 (.04877)	6.068 (.02482)	---	---
5 4 3	4.549 (.09892)	5.656 (.04863)	6.410 (.02495)	---	---
5 4 4	4.668 (.09817)	5.657 (.04863)	6.673 (.02459)	---	---
5 5 1	4.109 (.08596)	5.127 (.04618)	6.000 (.02165)	---	---
5 5 2	4.923 (.09704)	5.338 (.04726)	6.346 (.02469)	---	---
5 5 3	4.545 (.09935)	5.705 (.04612)	6.549 (.02436)	---	---
5 5 4	4.523 (.09935)	5.666 (.04631)	6.760 (.02490)	---	---
5 5 5	4.560 (.09952)	5.780 (.04678)	6.740 (.02475)	---	---
6 5 3	---	---	---	---	---
6 5 4	---	---	---	---	---
6 5 5	---	---	---	---	---
7 5 3	---	---	---	---	---
7 5 4	---	---	---	---	---
7 5 5	---	---	---	---	---
8 5 3	---	---	---	---	---
8 5 4	---	---	---	---	---
8 5 5	---	---	---	---	---
9 5 3	---	---	---	---	---
9 5 4	---	---	---	---	---
9 5 5	---	---	---	---	---
10 5 3	---	---	---	---	---
10 5 4	---	---	---	---	---
10 5 5	---	---	---	---	---
11 5 3	---	---	---	---	---
11 5 4	---	---	---	---	---
11 5 5	---	---	---	---	---
12 5 3	---	---	---	---	---
12 5 4	---	---	---	---	---
12 5 5	---	---	---	---	---
13 5 3	---	---	---	---	---
13 5 4	---	---	---	---	---
13 5 5	---	---	---	---	---
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22 5 4	---	---	---	---	---
22 5 5	---	---	---	---	---
23 5 3	---	---	---	---	---
23 5 4	---	---	---	---	---
23 5 5	---	---	---	---	---
24 5 3	---	---	---	---	---
24 5 4	---	---	---	---	---
24 5 5	---	---	---	---	---
25 5 3	---	---	---	---	---
25 5 4	---	---	---	---	---
25 5 5	---	---	---	---	---
26 5 3	---	---	---	---	---
26 5 4	---	---	---	---	---
26 5 5	---	---	---	---	---
27 5 3	---	---	---	---	---
27 5 4	---	---	---	---	---
27 5 5	---	---	---	---	---
28 5 3	---	---	---	---	---
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28 5 5	---	---	---	---	---
29 5 3	---	---	---	---	---
29 5 4	---	---	---	---	---
29 5 5	---	---	---	---	---
30 5 3	---	---	---	---	---
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31 5 3	---	---	---	---	---
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32 5 3	---	---	---	---	---
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32 5 5	---	---	---	---	---
33 5 3	---	---	---	---	---
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34 5 3	---	---	---	---	---
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37 5 3	---	---	---	---	---
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38 5 3	---	---	---	---	---
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39 5 3	---	---	---	---	---
39 5 4	---	---	---	---	---
39 5 5	---	---	---	---	---
40 5 3	---	---	---	---	---
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40 5 5	---	---	---	---	---
41 5 3	---	---	---	---	---
41 5 4	---	---	---	---	---
41 5 5	---	---	---	---	---
42 5 3	---	---	---	---	---
42 5 4	---	---	---	---	---
42 5 5	---	---	---	---	---
43 5 3	---	---	---	---	---
43 5 4	---	---	---	---	---
43 5 5	---	---	---	---	---

**Kolmogorov-Smirnov One-Sided Test**

n	0.1	0.05	0.025	0.01	0.005
1	0.9000	0.9500	0.9750	0.9900	0.9950
2	0.6838	0.7764	0.8419	0.9000	0.9293
3	0.5648	0.6360	0.7076	0.7846	0.8290
4	0.4927	0.5652	0.6239	0.6889	0.7342
5	0.4470	0.5094	0.5633	0.6272	0.6685
6	0.4104	0.4680	0.5193	0.5774	0.6166
7	0.3815	0.4361	0.4834	0.5384	0.5758
8	0.3583	0.4096	0.4543	0.5065	0.5418
9	0.3391	0.3875	0.4300	0.4796	0.5133
10	0.3226	0.3687	0.4092	0.4566	0.4889
11	0.3083	0.3524	0.3912	0.4367	0.4677
12	0.2958	0.3382	0.3754	0.4192	0.4490
13	0.2847	0.3255	0.3614	0.4036	0.4325
14	0.2748	0.3142	0.3489	0.3897	0.4176
15	0.2659	0.3040	0.3376	0.3771	0.4042
16	0.2578	0.2947	0.3273	0.3657	0.3920
17	0.2504	0.2863	0.3180	0.3553	0.3809
18	0.2436	0.2785	0.3094	0.3457	0.3706
19	0.2373	0.2714	0.3014	0.3369	0.3612
20	0.2316	0.2647	0.2941	0.3287	0.3524
21	0.2262	0.2586	0.2872	0.3210	0.3443
22	0.2212	0.2528	0.2809	0.3139	0.3367
23	0.2165	0.2475	0.2749	0.3073	0.3295
24	0.2120	0.2424	0.2693	0.3010	0.3229
25	0.2079	0.2377	0.2640	0.2952	0.3166
26	0.2040	0.2332	0.2591	0.2896	0.3106
27	0.2003	0.2290	0.2544	0.2844	0.3050
28	0.1968	0.2250	0.2499	0.2794	0.2997
29	0.1935	0.2212	0.2457	0.2747	0.2947
30	0.1903	0.2176	0.2417	0.2702	0.2899
31	0.1873	0.2141	0.2379	0.2660	0.2853
32	0.1844	0.2108	0.2342	0.2619	0.2809
33	0.1817	0.2077	0.2308	0.2580	0.2768
34	0.1791	0.2047	0.2274	0.2543	0.2728
35	0.1766	0.2018	0.2242	0.2507	0.2690
36	0.1742	0.1991	0.2212	0.2473	0.2653
37	0.1719	0.1965	0.2183	0.2440	0.2618
38	0.1697	0.1939	0.2154	0.2409	0.2584
39	0.1675	0.1915	0.2127	0.2379	0.2552
40	0.1655	0.1891	0.2101	0.2349	0.2521
>40	$1.07/\sqrt{n}$	$1.22/\sqrt{n}$	$1.36/\sqrt{n}$	$1.52/\sqrt{n}$	$1.63/\sqrt{n}$

**Upper Critical Values of Spearman's Rank Correlation Coefficient  $R_s$**

Note: In the table below, the critical values give significance levels as close as possible to but not exceeding the nominal  $\alpha$ .

n	Nominal $\alpha$				
	0.10	0.05	0.025	0.01	0.005
4	0.700	0.700	0.700	0.700	0.700
5	0.697	0.699	0.699	0.699	0.699
6	0.697	0.714	0.708	0.693	0.699
7	0.694	0.714	0.708	0.693	0.699
8	0.694	0.714	0.708	0.693	0.699
9	0.694	0.714	0.708	0.693	0.699
10	0.694	0.714	0.708	0.693	0.699
11	0.694	0.714	0.708	0.693	0.699
12	0.694	0.714	0.708	0.693	0.699
13	0.694	0.714	0.708	0.693	0.699
14	0.694	0.714	0.708	0.693	0.699
15	0.694	0.714	0.708	0.693	0.699
16	0.694	0.714	0.708	0.693	0.699
17	0.694	0.714	0.708	0.693	0.699
18	0.694	0.714	0.708	0.693	0.699
19	0.694	0.714	0.708	0.693	0.699
20	0.694	0.714	0.708	0.693	0.699
21	0.694	0.714	0.708	0.693	0.699
22	0.694	0.714	0.708	0.693	0.699
23	0.694	0.714	0.708	0.693	0.699
24	0.694	0.714	0.708	0.693	0.699
25	0.694	0.714	0.708	0.693	0.699
26	0.694	0.714	0.708	0.693	0.699
27	0.694	0.714	0.708	0.693	0.699
28	0.694	0.714	0.708	0.693	0.699
29	0.694	0.714	0.708	0.693	0.699

(Continued)