UNIVERSITY OF SWAZILAND

FINAL EXAMINATION PAPER 2012

TITLE OF PAPER:QUANTITATIVE METHODS IN DEMOGRAPHYCOURSE CODE:DEM206TIME ALLOWED:TWO (2) HOURSREQUIREMENTS:CALCULATOR AND STATISTICAL TABLESINSTRUCTIONS:ANSWER ANY THREE QUESTIONS

1

Question 1

[20 marks, 10+5+5]

(a) Many people believe that criminals who plead tend to get lighter sentences than those who are convicted in trials. The accompanying table summarises randomly selected sample data for Manzini defendants in burglary cases. All the subjects had prior prison sentences. At the 0.05 significance level, test the claim that the sentence (sent to prison or not sent to prison) is independent of plea. If you were an attorney defending a guilty defendant, would these results suggest that you should encourage a guilty plea?

	Guilty Plea	Not Guilty Plea
Sent to prison	392	58
Not sent to prison	564	14

- (b) A husband and wife are each 70 years old. The probability that the husband will die sometimes this year is 0.10, and the probability that the wife will die this year is 0.05. The probability that the husband will die this year given that his wife has died is 0.40.
 - (i) What is the probability that at least one of them will die this year?
 - (ii) What is the probability that the wife will die, given that the husband has died?

Question 2

[20 marks, 8+4+8]

The following table shows a random sample of 12 couples who stated the number of children they planned to have at the time of their marriage and the number of actual children they have.

Couple	1	2	3	4	5	6	7	8	9	10	11	12
Planned Number of Children	3	3	0	2	2	3	0	3	2	1	3	2
Actual Number of Children	4	3	0	4	4	3	0	4	3	1	3	1

- (a) Find the linear least-squares regression line of y on x.
- (b) Estimate the number of children that a couple who had planned to have 5 children actually had?
- (c) Is the *relationship* between the planned number of children and the actual number of children meaningful (or significant)? Use $\alpha = 0.05$.

Question 3

[20 marks, 8+6+6]

(a) The following table gives a summary of the birth weights (in kilograms) recorded for a sample of male babies born to mothers taking a special vitamin supplement.

\bar{x}	3.675
s_x	0.6573177821
n	32

Test the claim that the mean birth weight for all male babies born of mothers given vitamins is equal to 3.39kg, which is the mean for the population of all males

2

- (b) Swazi Airlink works only with advance reservations and experiences a 7% rate of no shows. How many reservations could be accepted with a capacity of 50 if there is at least a 0.95 probability that all reservations who show will be accommodated?
- (c) Several women are not hired at the Telecoms Company, they do some research and find that among the many people who applied, 30% were women. However, the 20 people who were hired consist of only 2 women and 18 men. Find the probability of randomly selecting 20 people from a large pool of applicants (30% of whom are women) and getting 2 or fewer women. Based on the results, does it appear that the company is discriminating based on gender?

Question 4

[20 marks, 10+10]

(a) In a first phase of a health study in a city, a random sample of size 2000 is to be obtained. The city is comprised (broadly) of five different ethnic subpopulations that make up 40%, 30%, 10%, 10% and 10% of the city population respectively.

A commercial company is employed to obtain the random sample, with the instruction that the sample should reflect the ethnic composition of the city. The sample they return is summarized in the following table.

	Ethnic Subpopulation							
	1	2	3	4	5			
Number in Sample	822	638	210	157	173			

Using a Chi-squared test for this one-way layout, comment on whether the company have fulfilled their remit to produce a sample that reflects the ethnic composition of the city.

(b) The listed values are waiting times (in minutes) of customers at a Manzini Bank, where customers enter a single line that feed two teller windows. Assuming the waiting times are normally distributed, construct a 95% confidence interval for the population mean μ .

 $6.5 \quad 6.6 \quad 6.7 \quad 6.8 \quad 7.1 \quad 7.3 \quad 7.4 \quad 7.7 \quad 7.7 \quad 7.7$

Question 5

[20 marks, 10+6+4]

(a) In an experimental study of nutrition, laboratory animals were allocated at random to one of four different diets, **A**, **B**, **C** and **D**. The response measurement was the weight gain (in grammes) of each animal over one week.

The data recorded are tabulated below; entries in the rows of the table are the weight gains for animals allocated to each diet.

Diet							
Α	0.54	1.98	0.65	0.52	1.92	1.48	0.97
В	1.24	1.82	1.39	1.25	1.29		
С	2.05	2.18	1.94	2.50	1.98	2.17	1.83
D	1.88	6.23	3.51	3.77	1.25	0.72	

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Using the data, an ANOVA analysis is to be carried out. Write out the ANOVA table in full. State clearly the null and alternative hypothesis, the test statistic, the null distribution, and the conclusion.

- (b) Estimate the probability of getting at least 65 girls in 100 births if the sex ratio is 105 girls to a 100 boys.
- (c) Explain the difference between a *parameter* and *statistic*, and the difference between *sampling error* and *non-sampling error* in full.

4

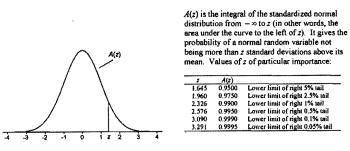
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STATISTICAL TABLES

1

TABLE A.1

Cumulative Standardized Normal Distribution



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0,07	0,08	0.09
0.0	0.5000	0.5040	0,5080	0.5120	0.5160	0.5199	0.5239	0.5279	0,5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0,5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0,5987	0,6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0,6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0,6628	0.6664	0.6700	0.6736	0.6772	0,6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0,7088	0,7123	0,7157	0.7190	0.7224
0,6	0,7257	0,7291	0,7324	0.7357	0,7389	0.7422	0,7454	0,7486	0.7517	0.7549
0.7	0,7580	0.7611	0.7642	0.7673	0,7704	0.7734	0.7764	0.7794	0,7823	0.7852
0.8	0,7881	0.7910	0,7939	0.7967	0,7995	0.8023	0.8051	0.8078	0.8106	0,8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0,8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0,8686	0.8708	0.8729	0.8749	0.8770	0,8790	0.8810	0.8830
1.2	0,8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0,9032	0.9049	0,9066	0.9082	0,9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0,9222	0.9236	0.9251	0.9265	0,9279	0.9292	0,9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0,9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0,9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0,9599	0.9608	0.9616	0.9625	0.9633
1.8	0,9641	0.9649	0.9656	0,9664	0.9671	0,9678	0.9686	0,9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0,9783	0,9788	0.9793	0.9798	0.9803	0.9808	0,9812	0.9817
2.1	0.9821	0.9826	0.9830	0,9834	0,9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0,9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0,9890
2.3	0,9893	0.9896	0.9898	0.9901	0.9904	0,9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0,9946	0,9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0,9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0,9970	0.9971	0,9972	0,9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0,9979	0,9979	0.9980	0.9981
2.9	0.9981	0,9982	0.9982	0,9983	0.9984	0.9984	0,9985	0,9985	0.9986	0,9986
3.0	0,9987	0,9987	0.9987	0,9988	0.9988	0.9989	0.9989	0,9989	0,9990	0,9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0,9993
3.2	0.9993	0.9993	0.9994	0.9994	0,9994	0.9994	0.9994	0.9995	0.9995	0,9995
3.3	0.9995	0.9995	0.9995	0.9996	0,9996	0,9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0,9997	0.9997	0.9997	0,9997	0.9997	0,9998
3.5	0.9998	0.9998	0.9998	0,9998	0.9998	0,9998	0,9998	0.9998	0,9998	0.9998
3,6	0,9998	0.9998	0.9999							

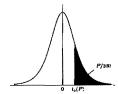
Percentage Points of the t-Distribution

This table gives the percentage points $t_{\nu}(P)$ for various values of P and degrees of freedom ν , as indicated by the figure to the right.

The lower percentage points are given by symmetry as $-t_{\nu}(P)$, and the probability that $|t| \ge t_{\nu}(P)$ is 2P/100.

The limiting distribution of t as $\nu \to \infty$ is the normal distribution with zero mean

and unit variance.



Percentage points P

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15 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 1.337 1.746 2.120 2.583 2.921 3.686 4.015 18 1.330 1.734 2.101 2.552 2.878 3.610 3.922 21 1.323 1.721 2.080 2.518 2.831 3.527 3.819 25 1.316 1.708 2.060 2.485 2.787 3.450 3.725 30 1.303 1.684 2.021 2.457 2.750 3.385 3.646 40 1.303 1.684 2.021 2.423 2.704 3.007 3.551 50 1.299 1.667 2.092 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390		13	1.350	1.771	2.160				
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16 1.330 1.734 2.101 2.552 2.878 3.610 3.922 21 1.323 1.721 2.080 2.518 2.831 3.527 3.819 25 1.316 1.708 2.060 2.485 2.787 3.450 3.725 30 1.310 1.697 2.042 2.457 2.750 3.385 3.646 40 1.303 1.684 2.021 2.423 2.704 3.307 3.551 50 1.299 1.667 2.092 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390		15	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16 1.330 1.734 2.101 2.552 2.878 3.610 3.922 21 1.323 1.721 2.080 2.518 2.831 3.527 3.819 25 1.316 1.708 2.060 2.485 2.787 3.450 3.725 30 1.310 1.697 2.042 2.457 2.750 3.385 3.646 40 1.303 1.684 2.021 2.423 2.704 3.307 3.551 50 1.299 1.667 2.092 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
21 1.323 1.721 2.080 2.518 2.831 3.527 3.819 25 1.316 1.708 2.060 2.485 2.787 3.450 3.725 30 1.697 2.042 2.457 2.750 3.385 3.646 40 1.303 1.684 2.021 2.423 2.704 3.307 3.551 50 1.299 1.676 2.009 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
25 1.316 1.708 2.060 2.485 2.787 3.450 3.725 30 1.310 1.697 2.042 2.457 2.750 3.385 3.646 40 1.303 1.684 2.021 2.423 2.704 3.307 3.551 50 1.299 1.676 2.009 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
30 1.30 1.697 2.042 2.457 2.750 3.385 3.046 40 1.303 1.684 2.021 2.423 2.704 3.307 3.551 50 1.299 1.676 2.009 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
40 1.303 1.684 2.021 2.423 2.704 3.307 3.551 50 1.299 1.676 2.009 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
50 1.299 1.676 2.009 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390		30	1.310	1.697	2.042	2.457	2.750	3.385	3.646
50 1.299 1.676 2.009 2.403 2.678 3.261 3.496 70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
70 1.294 1.667 1.994 2.381 2.648 3.211 3.435 100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
100 1.290 1.660 1.984 2.364 2.626 3.174 3.390									
∞ 1.282 1.645 1.960 2.326 2.576 3.090 3.291					-				
		00	1.282	1.645	1.960	2.326	2.576	3.090	3.291

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Percentage Points of the χ^2 -Distribution

Percentage points P

6.635

9.210

11.345

13.277

15.086

20.090

26.217

27.688

29.141

30.578

23.542 26.296 28.845 32.000 34.267 39.252 41.308

33.409

34.805

63.691

16.812 18.548

18.475 20.278

21.666 23.589

23.209 25.188

0.5

7.879

10.597

12.838

14.860

16.750

21.955

28.300

29.819

31.319

32.801

35.718

37.156

39.997

66.766

36.191 38.582

0.1

10.828

13.816

16.266

18.467

20.515

26.124

29.588

31.264

32.909

34.528

36.123

37.697

40.790

42.312

45.315 47.498

86.661 89.561

43.820

52.620

59.703

73.402

22.458 24.103

24.322 26.018

27.877 29.666

0.05

12.116

15.202

17.730

19.997

22.105

27.868

31.420 33.137

34.821

36.478

38.109

39.719

42.879

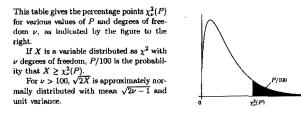
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45.973

54.947

62.162

76.095



2.5

5.024

7.378

9.348

11.143

12.833

17.275 19.675 21.920 24.725 26.757

27.488

31.526

34.382 37.652 40.646 44.314 46.928

40.256 43.773 46.979 50.892 53.672

63.167 67.505 71.420 76.154 79.490

5

3.841

5.991

7.815

9.488

11.070

18.549 21.026 23.337

19.812 22.362 24.736

24.996

28.869

27.204 30.144 32.852

17 24.769 27.587 30.191

12.592 14.449

14.067 16.013

15.507 17.535

16.919 19.023

18.307 20.483

23.685 26.119

28.412 31.410 34.170 37.566

55.758 59.342

10

2.706

4.605

6.251

7.779

9.236

12.017

13.362

15.987

21.064

22.307

25.989

51.805

ν

1

2

3

4

5

6 10.645

7

8

9 14.684

10

11

12

13

14

15

16

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19

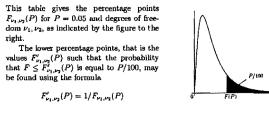
20

25

30

40

50



					ν_1				
ν2	1	2	3	4	5	6	12	24	~
2	18.513	19.000	19.164	19.247	19.296	19.330	19.413	19.454	19.496
3	10.128	9.552	9.277	9.117	9.013	8.941	8.745	8.639	8.526
4	7.709	6.944	6.591	6.388	6.256	6.163	5.912	5.774	5.628
5	6.608	5.786	5.409	5.192	5.050	4.950	4.678	4.527	4.365
6	5.987	5.143	4.757	4.534	4.387	4.284	4.000	3.841	3.669
7	5.591	4.737	4.347	4.120	3.972	3.866	3.575	3.410	3.230
8	5.318	4.459	4.066	3.838	3.687	3.581	3.284	3.115	2.928
9	5.117	4.256	3.863	3.633	3.482	3.374	3.073	2.900	2.707
10	4.965	4.103	3.708	3.478	3.326	3.217	2.913	2.737	2.538
11	4.844	3.982	3.587	3.357	3.204	3.095	2.788	2.609	2.404
12	4.747	3.885	3.490	3.259	3.106	2.996	2.687	2.505	2.296
13	4.667	3.806	3.411	3.179	3.025	2.915	2.604	2.420	2.206
14	4.600	3.739	3.344	3.112	2.958	2.848	2.534	2.349	2.131
15	4.543	3.682	3.287	3.056	2.901	2.790	2.475	2.288	2.066
16	4.494	3.634	3.239	3.007	2.852	2.741	2.425	2.235	2.010
17	4.451	3.592	3.197	2.965	2.810	2.699	2.381	2.190	1.960
18	4.414	3.555	3.160	2.928	2.773	2.661	2.342	2.150	1.917
19	4.381	3.522	3.127	2.895	2.740	2.628	2.308	2.114	1.878
20	4.351	3.493	3.098	2.866	2.711	2.599	2.278	2.082	1.843
25	4.242	3.385	2.991	2.759	2.603	2,490	2.165	1.964	1.711
30	4.171	3.316	2.922	2.690	2.534	2.421	2.092	1.887	1.622
40	4.085	3.232	2.839	2.606	2.449	2.336	2.003	1.793	1.509
50	4.034	3.183	2.790	2.557	2.400	2.286	1.952	1.737	1.438
100	3.936	3.087	2.696	2.463	2.305	2.191	1.850	1.627	1.283
~	3.841	2.996	2.605	2.372	2.214	2.099	1.752	1.517	1.002

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δ

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80 96.578 101.879 106.629 112.329 116.321 124.839 128.261