

UNIVERSITY OF SWAZILAND

DEPARTMENT OF STATISTICS AND DEMOGRAPHY

SUPPLEMENTARY EXAMINATION, 2011/12

COURSE TITLE: DESIGN AND ANALYSIS OF EXPERIMENTS

COURSE CODE: ST 404

TIME ALLOWED: TWO (2) HOURS

INSTRUCTION: ANSWER ANY THREE QUESTIONS

SPECIAL REQUIREMENTS: STATISTICAL TABLES

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INVIGILATOR**

Question 1

a) Explain how the principles of design of experiments are applied in case of Randomised Block Design. **(5 marks)**

b) The Hidden Valley Construction Company is interested in knowing whether landscaping increases the sales price of property by an amount that exceeds the cost of the landscaping. The company is developing five different subdivisions in Siteki. In each subdivision the salesman of the company chose tree lots that were similar in size, location, surrounding property and also had identical houses built on them. In each subdivision, he chose, at random, one property that was left without any landscaping, one for which some (but not much landscaping was done, and one for which extensive landscaping was done. The sales prices, minus the cost of landscaping follows. What conclusions can be drawn on the basis of these data?

Subdivision	Landscaping		
	None	Some	Extensive
1	43.1	2.3	45.6
2	27.6	29.3	35.1
3	27.0	26.5	29.3
4	31.0	32.3	34.5
5	21.3	20.2	25.6

(15 marks)**Question 2**

(a) State three assumptions for doing a valid ANOVA, and how you would check for their validity. **(6 marks)**

(b) List two reasons for doing a factorial experiment rather than a one-factor-at-a-time experiment. **(4 marks)**

(c) How do you decide that a factor in your experiment is a random factor? **(6 marks)**

(d) When do we say treatment effects are confounded with blocks? Explain. **(4 marks)**

Question 3

The response time in seconds was determined for four different types of circuits that could be used in an automatic valve shutoff mechanism. The results are shown in the following table:

Circuit type	Response Time					
1	13	9	12	10	8	15
2	25	20	21	23	17	30
3	10	6	5	8	16	7
4	14	18	12	17	15	13

- (a) Test the hypothesis that the four circuit types have the same average response time. Use 1% level of significance. **(10 marks)**
- (b) Assuming all assumptions are satisfied, conduct pair wise comparisons using Fisher's LSD test and state conclusions using $\alpha = 0.05$. **(10 marks)**

Question 4

A study was undertaken to investigate the water holding capacity of the soil in three different areas of Woodlands. In each area, a number of soil samples were collected randomly and sent to the same laboratory for analysis. The following table gives the water holding capacity (in millilitre per gram) of soil samples collected in each area.

Woodland A:	72	51	38	87	77	65	70	66	64	74
Woodlands B:	35	33	29	50	44	17	47	58		
Woodlands C:	54	62	88	65	80	53				

- (a) State and explain a linear model, which can be used for a one-way analysis of variance. Explain clearly what each term in the model represents and state any assumptions required for the analysis to be valid. **(10 marks)**
- (b) Carry out a suitable analysis of the data, stating the assumptions you have made and explaining what you conclude as a result of your analysis. **(10 marks)**

Question 5

Four chemists are asked to determine the percentage of methyl alcohol in a certain chemical compound. Each chemist makes three determinations and the results are the following:

Chemist	Percentage of Methyl Alcohol		
1	84.99	84.04	84.38
2	85.15	85.13	84.88
3	84.72	84.48	85.16
4	84.20	84.10	84.55

(a) Write out the model for this problem and explain clearly what each term in the model represents and state any assumptions required for the analysis to be valid.

(b) Set up the null and alternative hypotheses

(c) The following is part of the ANOVA table for this data, complete the table and state the appropriate conclusions at $\alpha = 0.05$. If appropriate, perform a Duncan's test on the treatment means.

Source	SS	DF	MS	F
Chemist	0.268			
Error				
Total	1.903			

(20 marks)