## UNIVERSITY OF SWAZILAND

## SUPPLEMENTARY EXAMINATION PAPER 2014

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TITLE OF PAPER : DESCRIPTIVE STATISTICS
COURSE CODE : ST 132
TIME ALLOWED : TWO (2) HOURS
REQUIREMENTS : CALCULATOR
INSTRUCTIONS : THIS PAPER HAS FIVE (5) QUESTIONS. AN-
    SWER ANY FOUR (4) QUESTIONS.
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## Question 1

(a) Consider the basic food items in the following table, with their unit price and per capita annual consumption:

|  | Unit price (in Emalangeni) |  | Consumption |  |
| :---: | :---: | ---: | ---: | ---: |
| Food Items | $\mathbf{2 0 0 8}$ | $\mathbf{2 0 0 9}$ | $\mathbf{2 0 0 8}$ | $\mathbf{2 0 0 9}$ |
| Milk (litres) | 7.29 | 7.89 | 117 | 98 |
| Bread (loaves) | 4.25 | 4.45 | 56 | 64 |
| Sugar (kg) | 2.19 | 2.45 | 28 | 20 |
| Maize meal (kg) | 5.59 | 5.25 | 58 | 64 |

(i) Compute the Laspeyre's price and consumption indices and interpret them.
(ii) Which food item showed the largest price change from 2008 to 2009?
(iii) Which food item showed the largest consumption change from 2008 to 2009?
(b) The following table shows Consumer Price Index (CPI) for the period 2005 to 2009.

| Year | CPI |
| :---: | :---: |
| 2005 | 95 |
| 2006 | 100 |
| 2007 | 104 |
| 2008 | 110 |
| 2009 | 120 |

(i) Compute CPI using 2008 as base year.
(ii) Compute the average annual percentage change in CPI during 2005 and 2009.
(c) Find the average price paid per share in an equity portfolio consisting of: 40 shares bought for SZL15 each; 10 shares bought for SZL20 each; 5 shares bought for SZL40 each; and 50 shares bought for SZL10 each.

## Question 2

(a) A private game park owner is interested in forecasting the number of visitors (in hundreds) for 2011 using the following data:

|  | Quarter |  |  |  |
| ---: | ---: | ---: | ---: | ---: |
| Year | I | II | III | IV |
| 2007 | 86 | 62 | 28 | 94 |
| 2008 | 106 | 82 | 48 | 114 |
| 2009 | 140 | 120 | 82 | 154 |
| 2010 | 162 | 140 | 100 | 174 |

(i) Compute the trend.
(ii) Deseasonalise the data.
(iii) What do the deseazonalized data show about the number of visitors to the park.
(b) Office rental agreements contain escalation clauses. For a particular office complex in Manzini, the escalation rates based on the previous year rentals over 4 years were $16 \%, 14 \%, 10 \%$ and $8 \%$ respectively. What was the average annual escalation rate in office rentals for this office complex over this 4 -year period?

## Question 3

[25 marks, $8+4+2+7+4]$
(a) The following are the daily numbers of cars rented by a car rental company in 90 business days.

| Car <br> rentals | Number of <br> days |
| :---: | :---: |
| $20-24$ | 3 |
| $25-29$ | 10 |
| $30-34$ | 21 |
| $35-39$ | 28 |
| $40-44$ | 14 |
| $45-49$ | 9 |
| $50-54$ | 5 |

(i) Calculate the coefficient of skewness.
(ii) Estimate the quartile deviation.
(b) The following table shows the number of guests registered weekly at a health spa and the weekly wage expense for general maintenance workers of the spa's buildings and grounds during the eightweek period.

| Week | Number of guests <br> (in hundreds) | Weekly wage expense <br> (in thousands of Emalangeni) |
| :---: | :---: | :---: |
| 1 | 3.2 | 6.8 |
| 2 | 2.9 | 7.0 |
| 3 | 3.7 | 7.1 |
| 4 | 2.5 | 7.8 |
| 5 | 3.3 | 6.3 |
| 6 | 2.7 | 7.6 |
| 7 | 2.9 | 5.8 |
| 8 | 3.4 | 7.2 |

You can use these given results: $\sum x^{2}=76.74, \quad \sum y^{2}=389.42, \quad \sum x y=170.44$
(i) Identify the dependent variable ( $y$ ) and the independent variable $(x)$.
(ii) Determine the regression equation. Interpret the regression coefficients.
(iii) Estimate the weekly wage expense if there were 300 guests.

## Question 4

[25 marks, $4+4+4+4+4+5]$
(a) Consider the following two-way pivot table of brand preference for digital cameras and their primary usage (professional and personal).

| Usage | Digital Camera Brand Preference |  |  |
| :---: | :---: | :---: | :---: |
|  | Canon | Nikon | Pentax |
| Professional | 48 | 15 | 27 |
| Personal | 30 | 95 | 65 |

(i) What is the probability of selecting a professional user?
(ii) Find the probability that a user prefers the Pentax brand given that their usage is primarily for personal use?
(iii) What is the likelihood that a randomly selected user prefers the Canon brand and is a professional user?
(iv) Find the probability of randomly selecting either a professional user or a user who prefers the Nikon brand of digital camera?
(b) Two groups of bank trainees wrote a banking exam with the following results:

|  | Mean | Variance | Sample Size |
| :---: | :---: | :---: | :---: |
| Group 1 | 76 | 110 | 34 |
| Group 2 | 64 | 88 | 26 |

(i) Compute the mean of the combined exam scores.
(ii) Which group showed greater consistency in exam scores? Why?

## Question 5

[25 marks, $4+2+8+3+8$ ]
The Chamber of Commerce conducted a survey amongst 17 furniture retailers to identify the percentage of bad debts in each of the company's debtors' book. The bad debts percentages are as follows:

| 2.2 | 4.7 | 6.3 | 5.8 |
| :--- | :--- | :--- | :--- |
| 5.7 | 7.2 | 2.6 | 2.4 |
| 6.1 | 6.8 | 2.2 |  |
| 5.7 | 3.4 | 6.6 |  |
| 1.8 | 4.4 | 5.4 |  |

(a) Construct a stem and leaf diagram of the data.
(b) Find the average $\%$ of bad debts amongst the 17 furniture retailers.
(c) Compute the first quartile and the third quartile of the $\%$ of bad debts amongst the 17 furniture retailers surveyed. Interpret these quartiles.
(d) The chamber of commerce monitors bad debts levels based on samples of companies. It will advise an industry to take corrective action if the $\%$ of bad debts, on average, exceeds $5 \%$. Should the chamber of commerce send out an advisory note to all furniture retailers based on these sample findings? Justify your answer.
(e) Calculate the coefficient of skewness. Interpret this result.

