# UNIVERSITY OF SWAZILAND 

## DEPARTMENT OF STATISTICS AND DEMOGRAPHY

FINAL EXAMINATION 2017

| TITLE OF PAPER | : INDIRECT TECHNIQUES OF DEMOGRAPHIC ESTIMATION |
| :---: | :---: |
| COURSE CODE | : DEM 303 |
| TIME ALLOWED | : THREE (3) HOURS |
| INSTRUCTIONS | : ANSWER FOUR QUESTIONS |
| $1$ | : SHOW ALL YOUR FORMULAE AND WORKINGS. |
| REQUIREMENTS | : CALCULATOR |

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THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION HAS BEEN GRANTED BY THE INVIGILATOR

## Question 1

A demographer assessing parity data for a certain developing country observed its poor quality and decided to apply an el-Badry technique. Given this information:
a. Briefly explain three possible errors that could have generated poor parity data;
b. State any two reasons that could have justified the demographer's application of the el-Badry technique on the observed data?
c. What are the data requirements for the el-Badry technique?
d. State one assumption of the el-Badry technique;

After using the el-Badry technique, the demographer decided to use the Brass $\mathrm{P} / \mathrm{F}$ ratio method to estimate fertility.
e. Which assumptions are required to apply the $\mathrm{P} / \mathrm{F}$ ratio method?
f. The demographer obtained a decreasing trend in the $\mathrm{P} / \mathrm{F}$ ratios with age of the women. Explain what the derived $\mathrm{P} / \mathrm{F}$ ratios for this developing country imply;
g. Explain two advantages of using the Brass $\mathrm{P} / \mathrm{F}$ ratio method.

## Question 2

Table 2.1 presents the data needed to compute Coale's indices for Country A in year 1984. The estimated total number of births in Country A in 1984 was $3,789,050$ and there was a negligible amount of illegitimacy.

Table 2.1 Data for calculating Coale's indices for Country A, 1984

| Age <br> group | Hutterite marital <br> ASFRs, 1921-30 | Natural fertility <br> $n(a)$ | Deviation from <br> fertility $v(a)$ | Estimated population (000s) |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | All women | Married women |  |  |  |
| $15-19$ | 0.300 | 0.411 | 0.000 | 3899 | 2490 |
| $20-24$ | 0.550 | 0.460 | 0.000 | 3201 | 2938 |
| $25-29$ | 0.502 | 0.431 | -0.279 | 2737 | 2481 |
| $30-34$ | 0.447 | 0.395 | -0.667 | 2221 | 2001 |
| $35-39$ | 0.406 | 0.322 | -1.042 | 1901 | 1621 |
| $40-44$ | 0.222 | 0.167 | -1.414 | 1432 | 1997 |
| $45-49$ | 0.061 | 0.024 | -1.671 | 1200 | 821 |

Using the data provided in Table 2.1:
a. Compute Coale's Indices of $I_{g}, I_{g}$ and $I_{m}$;
b. Comment on your answers in part b);
c. Without any computation or derivation, write down the two formulae to estimate the CoaleTrussell fertility schedule of M and m scale parameters;
d. Compute the M and m scale parameters using your formulae shown in part c ).

## Question 3

a. State three uses of the Brass logit life table system;
b. What is the advantage of using a logit life table system rather than an empirical model life table?;
c. The Brass logit life table system is expressed as follows:

$$
\begin{equation*}
\lambda\left(l_{x}\right)=\alpha+\beta \lambda\left(l_{x}^{s}\right) \tag{2}
\end{equation*}
$$

i. Explain in brief what is meant by the mathematical expression above?
ii. Write down the formula for computing $\lambda\left(l_{x}\right)$.
d. The values of $\alpha$ and $\beta$ in the logit model life table are obtained after fitting a straight line in some way.
i. State the procedure on how to obtain that straight line;
ii. Which commands in excel would you write to obtain $\alpha$ and $\beta$ values?
iii. Give the formulae for $\alpha$ and $\beta$ you would use to get the same answers as in part d(ii) when using a calculator;
iv. Using your formulae in d (iii) and data given in table below, calculate $\alpha$ and $\beta$

| age | standard logits | observed logits |
| ---: | ---: | :---: |
| 1 | -1.70593 | -2.05952 |
| 5 | -1.5524 | -1.83178 |
| 55 | -1.05987 | -0.95938 |
| 65 | -0.7579 | -0.69315 |

e. Provide a formula you would use to derive a fitted life table using the parameters derived above.

## Question 4

Describe in detail ANY ONE of the following indirect estimation methods:
a. Widowhood method; OR
b. Orphanhood method.

Note: Your answer should be arranged to describe the method in terms of the following:
i) Purpose or rationale;
ii) Data required;
iii) Brass procedure computational steps, formulae may not be provided; AND
iv) Assumptions; OR
v) Limitations, any two needed.

