## UNIVERSITY OF SWAZILAND



MAIN EXAMINATION PAPER 2016
TITLE OF PAPER : DESCRIPTIVE STATISTICS
COURSE CODE : STA131/ST132
TIME ALLOWED : 2 HOURS
INSTRUCTIONS ANSWER ANY THREE (3) QUESTIONS.
REQUIREMENTS SCIENTIFIC CALCULATOR ANDGRAPH PAPER.

## Question 1

The following scores represent the final examination grade for an elementary statistics course:

> 236079325774527082365598884869807681628474775267749081104143 1580954165928564757825807183546472607889768479346717828561
a) Construct a stem-and-leaf plot for the examination grades in which the stems are $1,2,3, \ldots$. 9.
b) Construct a relative frequency histogram, draw an estimate of the graph of the distribution and discussthe skewness of the distribution.
(5 Marks)
c) Compute the sample mean, sample median, and sample standard deviation from the frequency distribution table.

(12 Marks)

## Question 2

In a study conducted by the Department of Mechanical Engineering at a univesrsity, the steel rods supplied by two different companies were compared. Ten sample springs were made out of the steel rods supplied by each company and a measure of flexibility was recorded for each. The data are as follows:

Company A: $9.38 .8 \quad 6.8 \quad 8.78 .5 \quad 6.78 .0 \quad 6.5 \quad 9.27 .0$
Company B: $11.0 \quad 9.8 \quad 9.9 \quad 10.2 \quad 10.1 \quad 9.711 .011 .110 .29 .6$
a) Calculate the sample mean, median, and variance for the data for the two companies.
(3+3+4 Marks)
b) Calculate the coefficient of variation for the two companies and comment.

## Question 3

The Table below gives the unemployment rate and the total personal income for the United States for various years.

| Year | Unemployment <br> rate (percent) | Total Personal <br> Income(\$billions) |
| :---: | :---: | :---: |
| 1975 | 8.5 | 1.3 |
| 1980 | 7.1 | 2.3 |
| 1985 | 7.2 | 3.4 |

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| 1990 | 5.6 | 4.8 |
| :---: | :---: | :---: |
| 1995 | 5.6 | 6.1 |
| 2000 | 4.0 | 8.3 |

a) Use linear regression to predict the total personal income of the United States if the unemployment rate is $5.0 \%$.
b) Use linear regression to predict the unemployment rate if the total personal income of the United States is $\$ 10$ billion.
c) Are the predictions in parts (a) and (b) reliable? Why or why not?

## Question 4

a) The country X's trade deficit with country Y (billions of Emalangeni) from 2007 through 2014 is reported as shown below.

| Year: | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Deficit: | 15.5 | 16.6 | 32.1 | 51.9 | 52.8 | 48.2 | 51.7 | 66.5 |

Using exponential smoothing and the smoothing constant $\alpha=0.7$, what deficit would have been forecast for 2015?
(12Marks)
b) The quarterly seasonal indices for a firm's electricity consumption are 115, 92, 81, and 112 for quarters $1-4$. It has forecast that electricity consumption will be 850,000 kilowatt-hours during 2017. Forecast electricity consumption for each quarter of 2017.
(8 Marks)

## Question 5

The Table below reports the prices, and the number of units of each consumed by a typical family for several food items for the years 2005 and 2015.

| Item | 2005 |  | 2015 |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Price (E) | Quantity | Price (E) | Quantity |
| Bread white (loaf) | 7.70 | 50 | 19.80 | 55 |
| Eggs(dozen) | 10.50 | 26 | 29.80 | 20 |
| Milk (litre) | 8.80 | 102 | 19.80 | 130 |
| Apples, red (500g) | 14.60 | 30 | 17.50 | 40 |
| Orange juice (300 ml concentrate) | 15.80 | 40 | 17.00 | 41 |
| Coffee, instant (400g) | 44.00 | 12 | 47.50 | 12 |

Calculate Laspeyres', Paasche's, and Fisher's Ideal indexes, and recommend the best index.

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(6+6+4+4 \text { Marks })
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